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# **NLO corrections to heavy Higgs boson decays in 2HDM**

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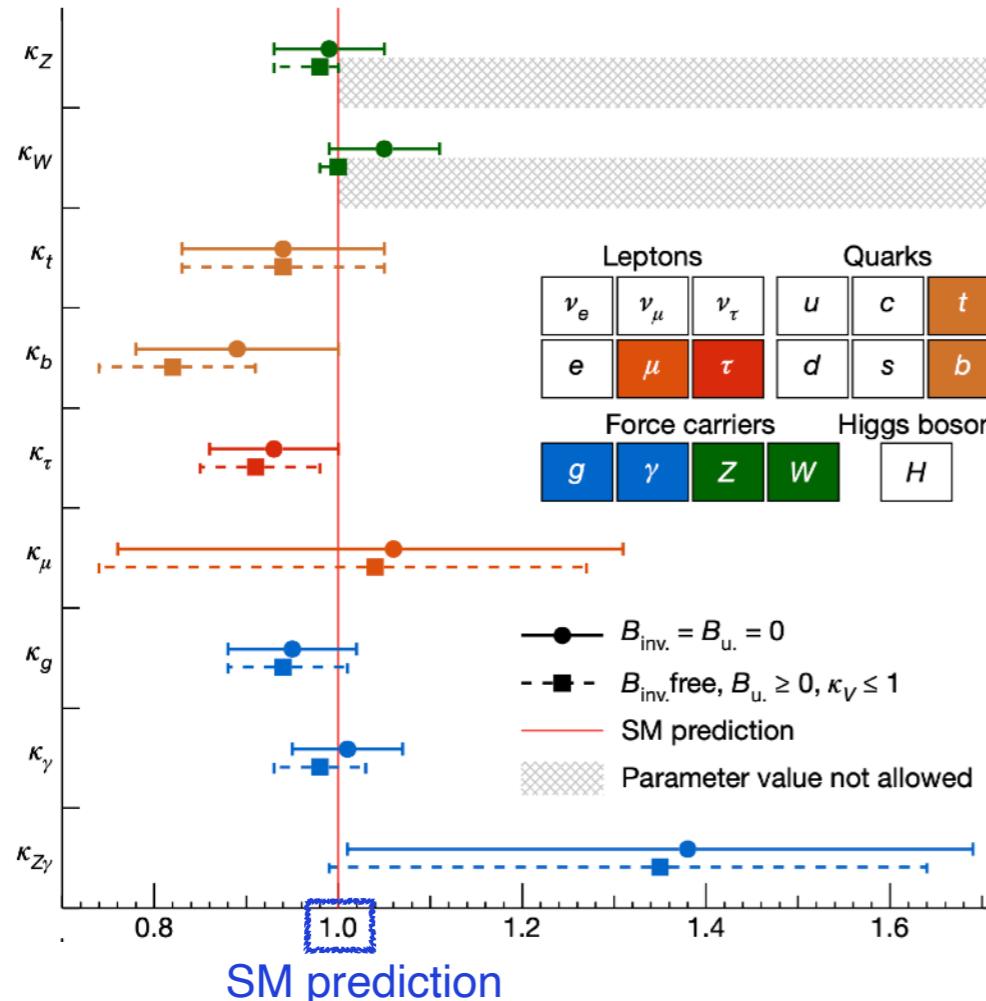
# Contents

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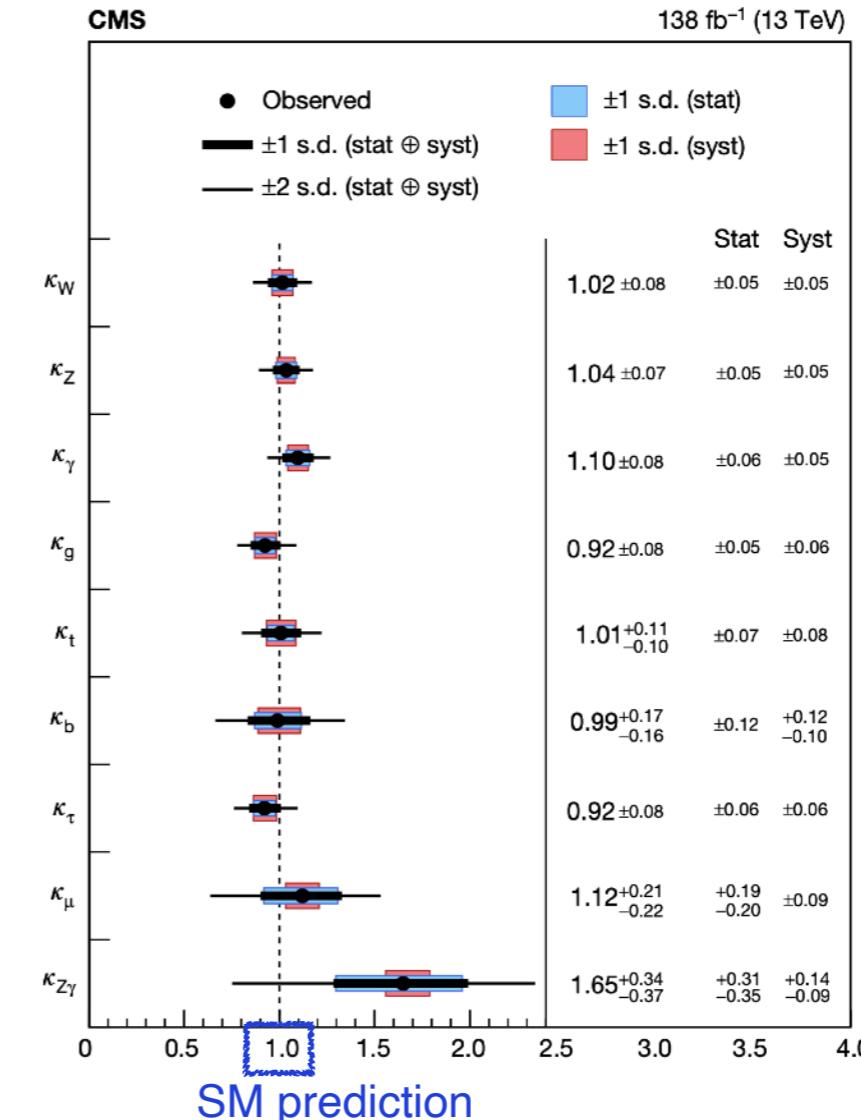
- Introduction
  - 2HDM, motivations.
- Detail of calculations
  - renormalization, scheme difference
- Results for  $A \rightarrow Z h$  and  $H \rightarrow hh$
- Summary

# Current status of Higgs measurements

[ATLAS, Nature 607,60–68 (2022)]



[CMS, Nature 607,60–68 (2022)]



$$\kappa_X = g_{hXX}^{\text{EX.}} / g_{hXX}^{\text{SM.}}$$

- Discovered Higgs boson is consistent with the prediction of the SM.
- This does not mean that Higgs sector of the SM is confirmed.

# Extended Higgs sector [1/2]

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- Many models can take SM-like limit.

$$\xrightarrow{M^2 \gg v} \mathcal{L}_{\text{eff}}^{NP} \simeq \mathcal{L}_{\text{SM}} + \frac{1}{M^2} (\Phi^\dagger \Phi)^3 + \dots$$

$$\kappa_X \sim 1$$

- Mystery of extended Higgs sector

- Number of Higgs, its representation

- Decoupling feature (Nondecoupling/decoupling)

$$m_\Phi^2 \simeq M^2 + \lambda_i v^2$$

- Symmetries



- Shape of the Higgs potential

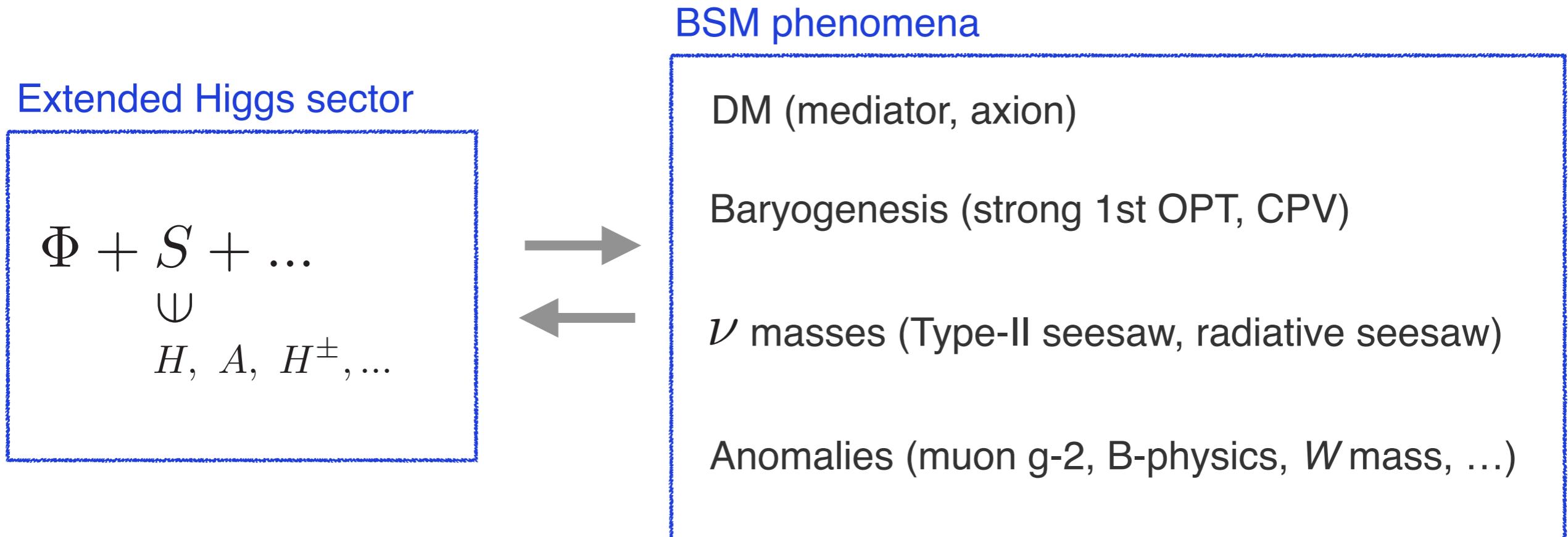


- Decoupling limit

- etc.

# Extended Higgs sector [2/2]

- Relation between Higgs sector and BSM.



- Relating with structure of Higgs sectors, decoupling features

Probe of Higgs sector is a key to pursue NP beyond the SM

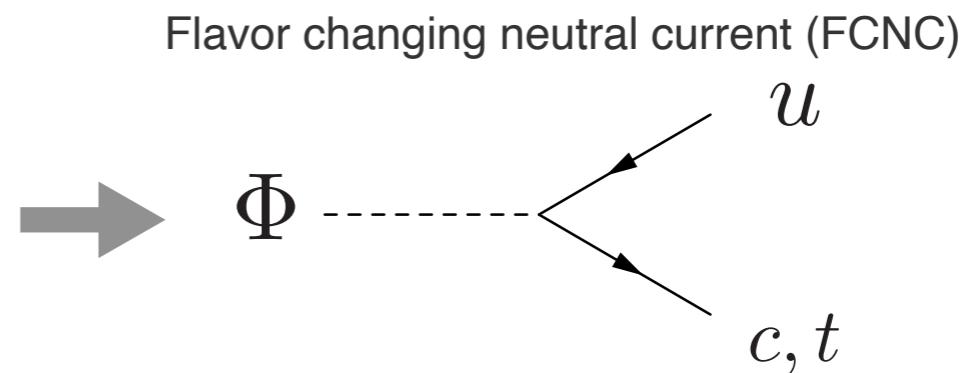
# Two Higgs doublet models (2HDMs) [1/2]

- Two Higgs doublet fields:  $\Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}w_1^+ \\ v_1 + h_1 + iz_1 \end{pmatrix}$   $\Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}w_2^+ \\ v_2 + h_2 + iz_2 \end{pmatrix}$
- Originally prosed by T.D. Lee to introduce CPV. [T.D. Lee, PRD 8 (1973) 1226]
- Restrictions for the shape of Higgs sector

-  $\rho$  parameter  $\rho \equiv \left( \frac{m_W^2}{m_Z \cos \theta_W} \right)^2 = \frac{\sum v_i^2 (I_{3,i}(I_{3,i} + 1) - \frac{1}{4} Y_i^2)}{\sum \frac{1}{2} v_i^2 Y_i^2} = 1$

- FCNC

$$\begin{aligned} \mathcal{L}^Y \ni & \bar{Q} (Y_{u,1} \Phi_1^c + Y_{u,2} \Phi_2^c) u_R \\ & + \bar{Q} (Y_{d,1} \Phi_1 + Y_{d,2} \Phi_2) d_R \\ & + \bar{L} (Y_{e,1} \Phi_1 + Y_{e,2} \Phi_2) \ell_R \end{aligned} \quad \boxed{\quad}$$



→ We impose softly broken  $Z_2$  symmetry  $\Phi_1 : +, \Phi_2 : -$

→ 4 types of Yukawa interactions: Type I, Type II, Type X, Type Y

$$(u_R, d_R, \ell_R) = (-, -, -) \quad (-, +, +) \quad (-, -, +) \quad (-, +, -)$$

# Two Higgs doublet models (2HDMs) [2/2]

$$V = m_1^2 |\Phi_1|^2 + m_2^2 |\Phi_2|^2 - m_3^2 (\Phi_1^\dagger \Phi_2 + \text{h.c.}) \\ + \frac{1}{2} \lambda_1 |\Phi_1|^4 + \frac{1}{2} \lambda_2 |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{1}{2} \lambda_5 [(\Phi_1^\dagger \Phi_2)^2 + \text{h.c.}],$$
$$\Phi_i = \begin{pmatrix} w_i^\pm \\ \frac{1}{\sqrt{2}}(v_1 + h_i + z_i) \end{pmatrix} \quad (i = 1, 2)$$

- Physical fields

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = R(\alpha) \begin{pmatrix} H \\ h \end{pmatrix}, \quad \begin{pmatrix} z_1 \\ z_2 \end{pmatrix} = R(\beta) \begin{pmatrix} G^0 \\ A \end{pmatrix}, \quad \begin{pmatrix} w_1^\pm \\ w_2^\pm \end{pmatrix} = R(\beta) \begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix}$$

$H, A, H^+, H^-$  :additional Higgs bosons,  $h$  : SM-like Higgs boson

- Input parameters:  $m_H, m_A, m_{H^\pm}, \sin(\beta-\alpha), \tan\beta, M^2 (=m_3^2/c_\beta s_\beta)$

# Alignment limit and decoupling limit

## Alignment limit

Higgs boson couplings :  $\kappa_V = \sin(\beta - \alpha)$   $\kappa_f = \sin(\beta - \alpha) + \xi_f \cos(\beta - \alpha)$

$$\boxed{\sin(\beta - \alpha) \rightarrow 1} \quad \longleftrightarrow \quad \kappa_V, \kappa_f \rightarrow 1$$
$$\left[ \quad \longleftrightarrow \quad \alpha = \beta - \frac{\pi}{2} \quad \text{All Higgs states are diagonalized by } \beta. \right]$$

## Decoupling limit

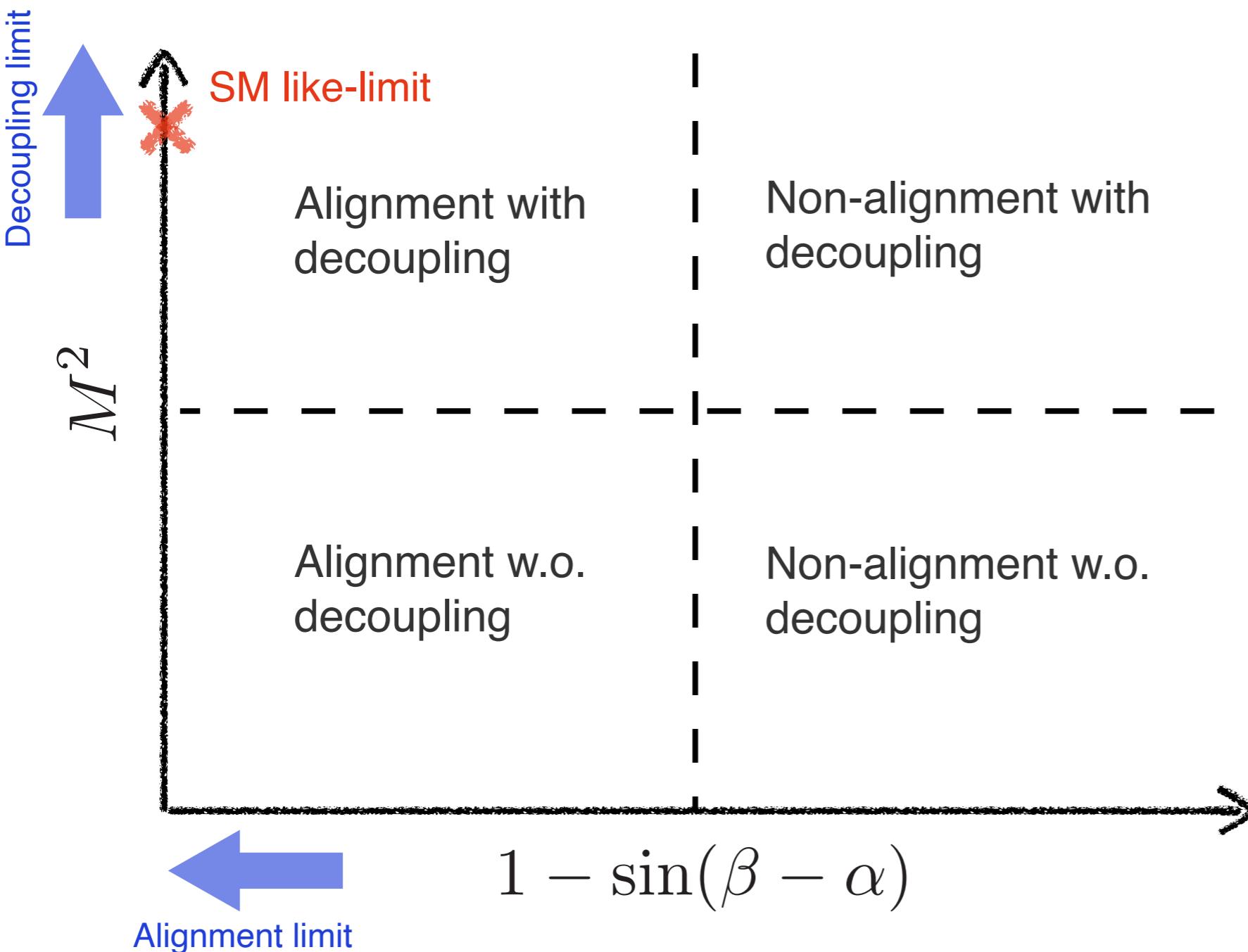
Mass of additional Higgs :  $m_\Phi^2 \simeq M^2 + \lambda_i v^2$

$$\boxed{M^2 \rightarrow \infty}$$

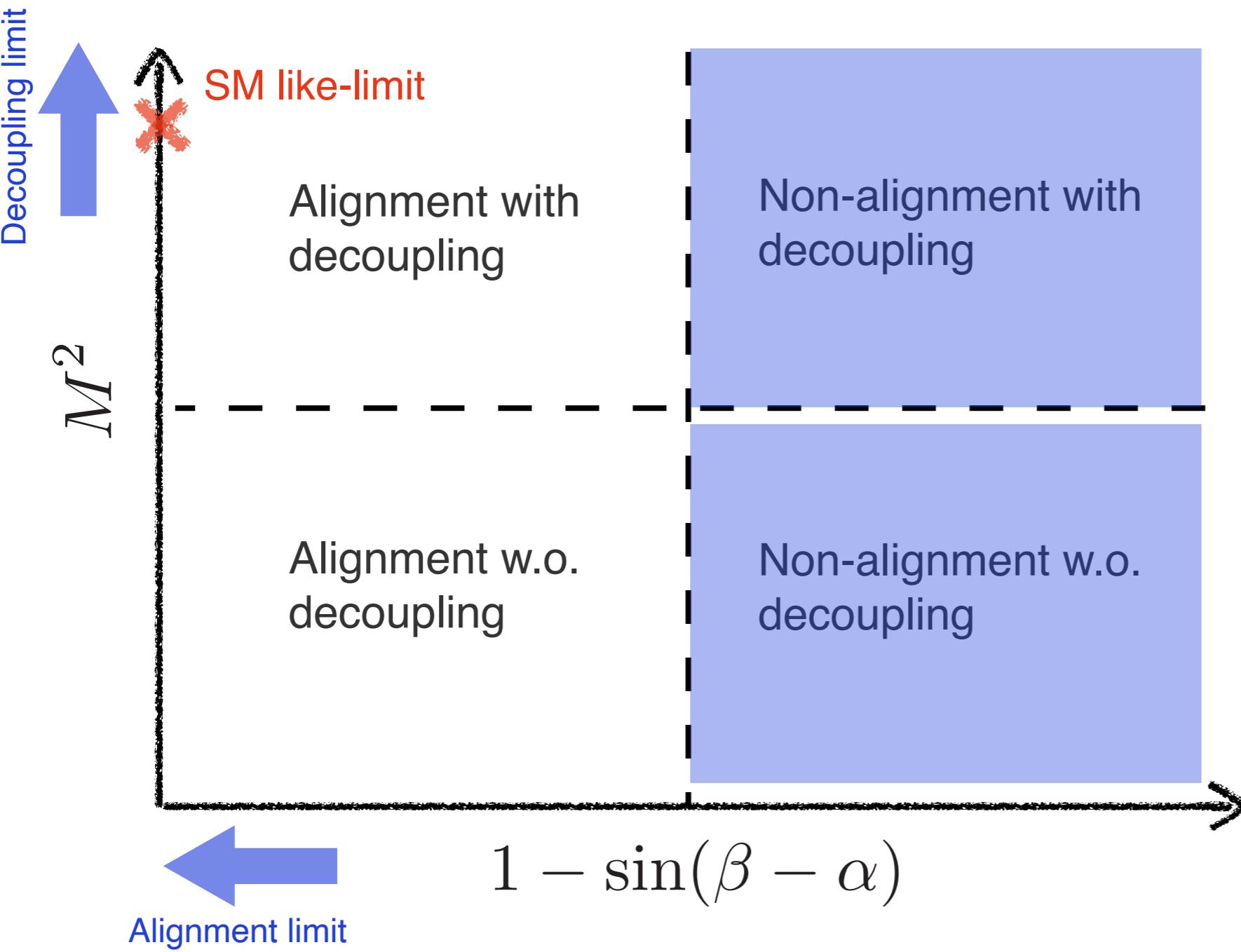
Definition of  $\alpha$ :  $\tan 2(\beta - \alpha) = \frac{\sum_i c_i \lambda_i v^2}{\sum_i c_i \lambda_i v^2 + M^2} \rightarrow 0$

Alignment limit is automatically satisfied by decoupling limit.

# Distinct scenarios



# Distinct scenarios



- $\sin(\beta - \alpha) \neq 0, M^2 \gg v^2$

$$\tan 2(\beta - \alpha) = \frac{\sum_i c_i \lambda_i v^2}{\sum_i c_i \lambda_i v^2 + M^2}$$

$$\rightarrow \lambda_i \gg 1$$

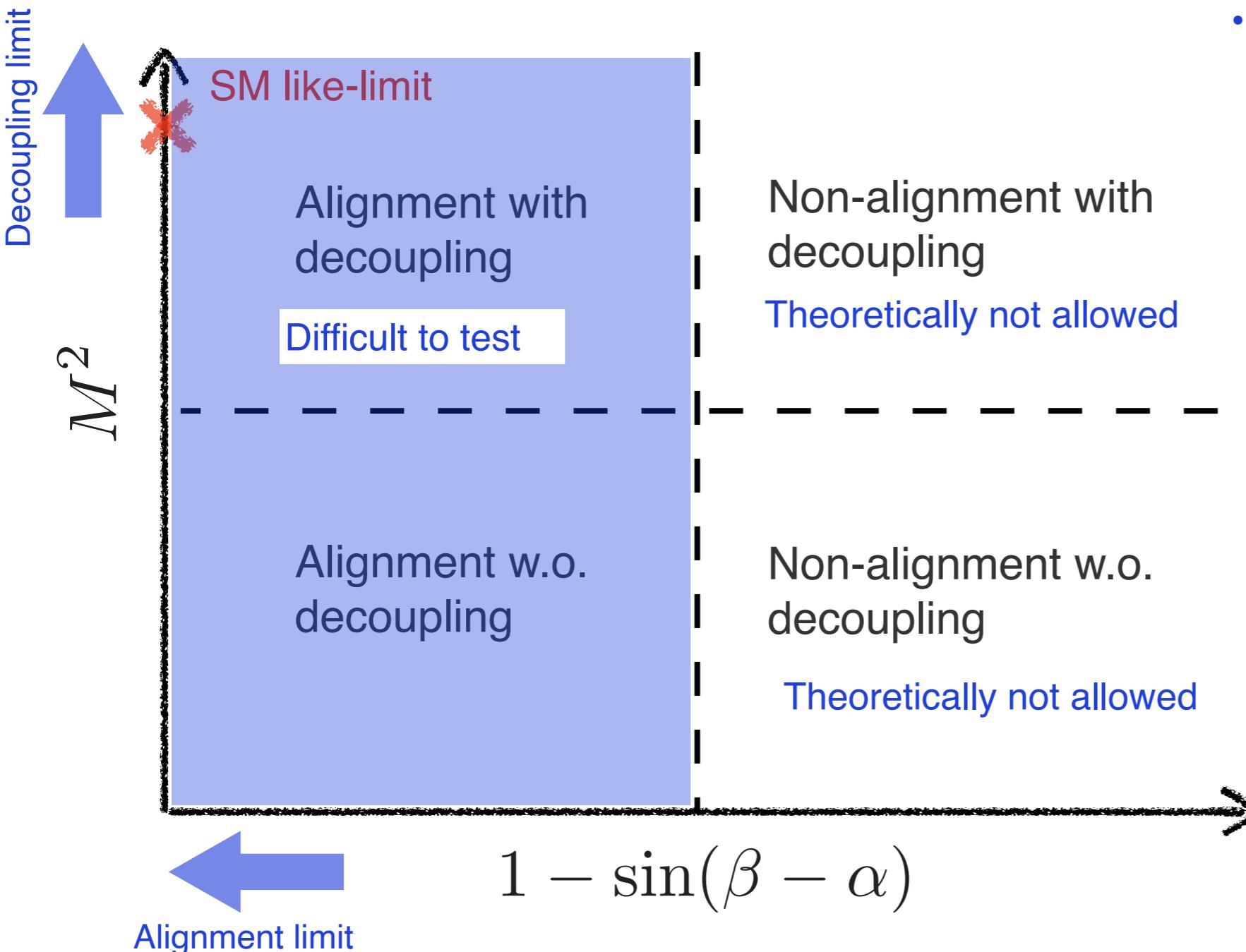
- $\sin(\beta - \alpha) \neq 0, M^2 \sim v^2$

$$\lambda_3 \sim t_\beta (1 - \lambda_{\text{SM}}) s_{2(\beta-\alpha)} + \lambda_{\text{SM}} c_{2(\beta-\alpha)}$$

$$\rightarrow \lambda_i \gg 1 \quad (\text{if } t_\beta \gg 1)$$

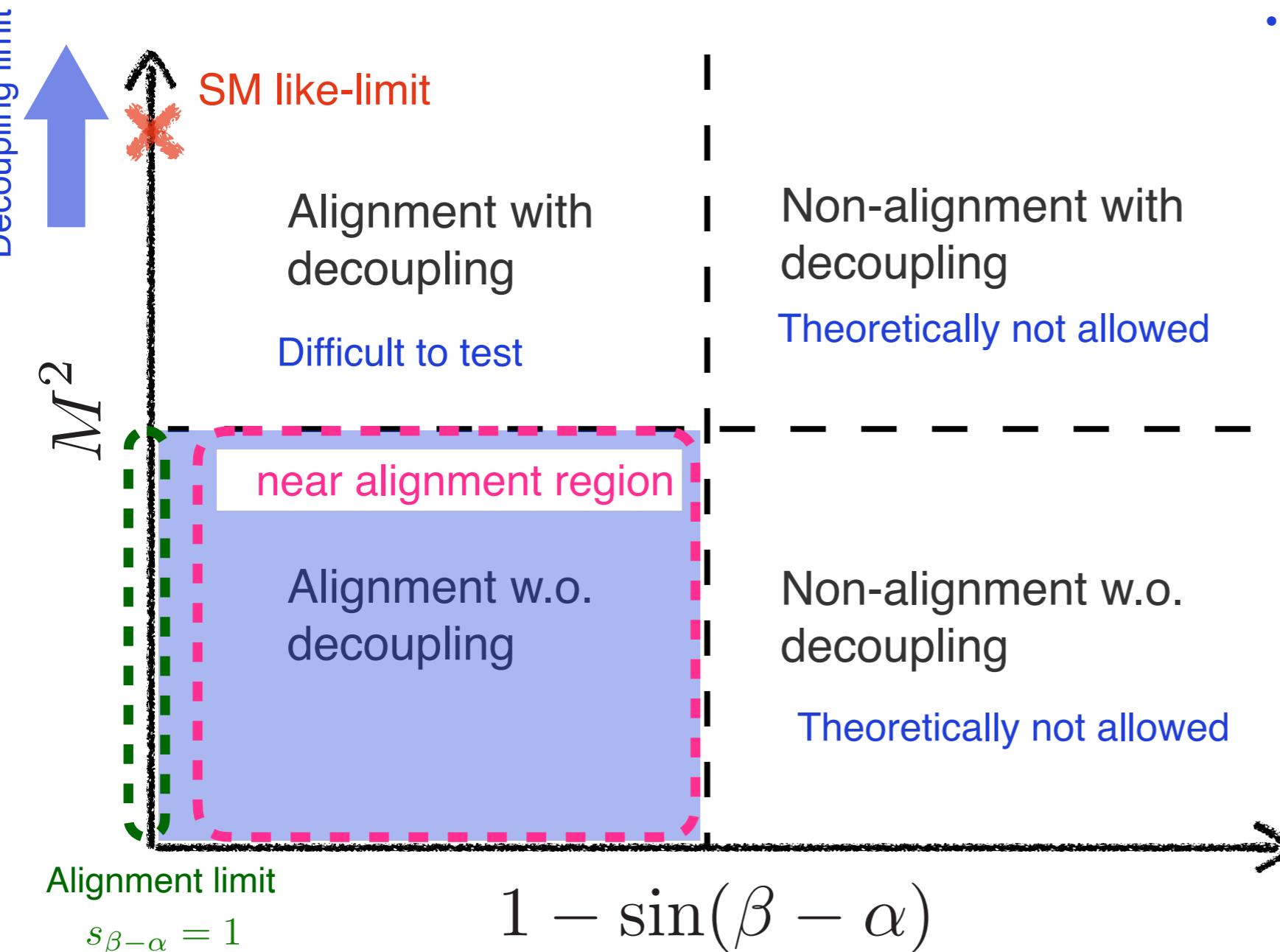
These are excluded by theoretical arguments (e.g. perturbativity)

# Distinct scenarios



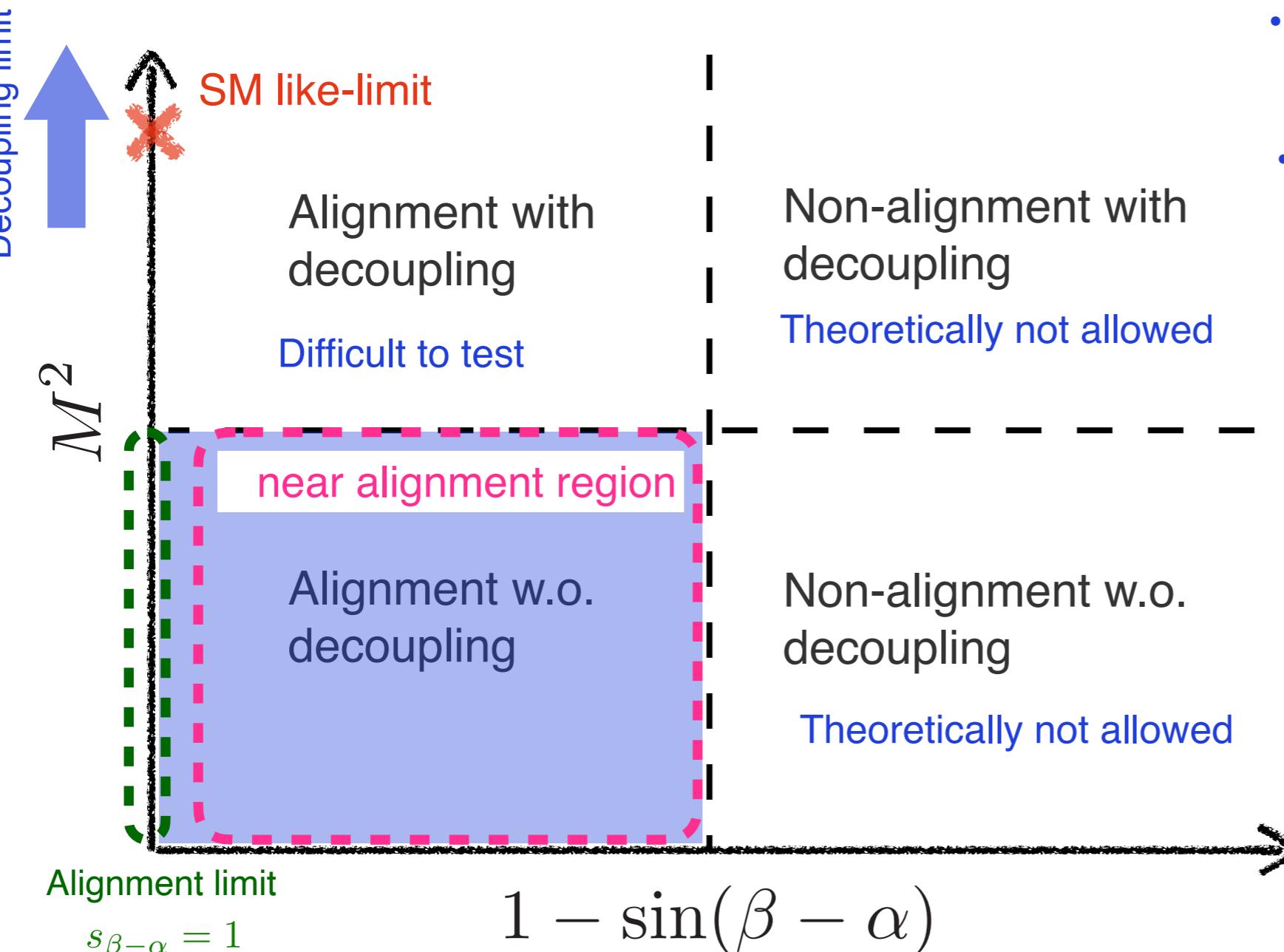
- Alignment w.o. decoupling is accessible by collider experiments.

# Distinct scenarios



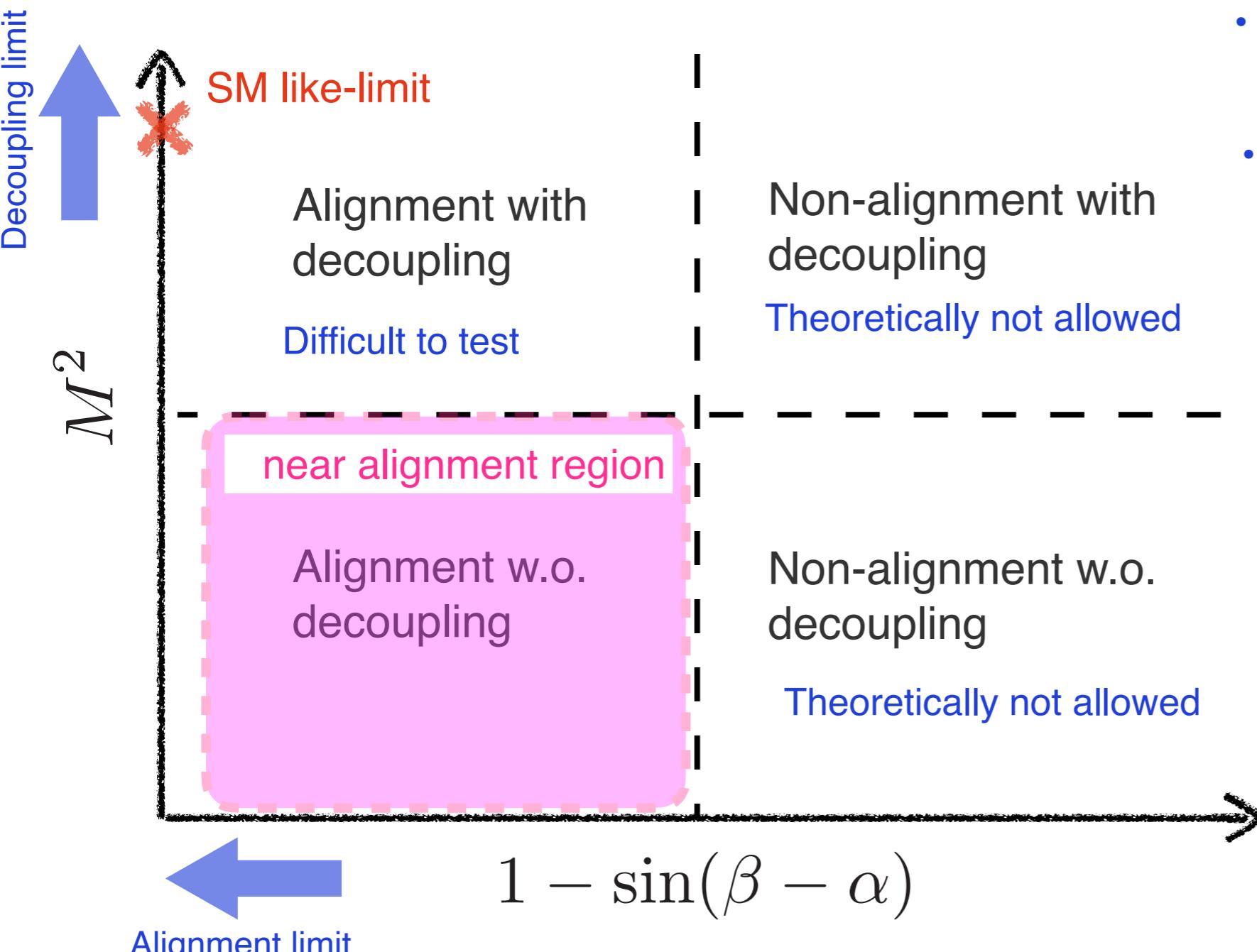
- Alignment w.o. decoupling is accessible by collider experiments.

# Distinct scenarios



- Alignment w.o. decoupling is accessible by collider experiments.
- It is favored by measurements of the signal strength of  $h$  :  
 $c_{\beta-\alpha} \lesssim 0.3$  (0.1) for Type I (II)  
[ ATLAS collaboration, PRD 101, 012002 (2020) ]

# Distinct scenarios

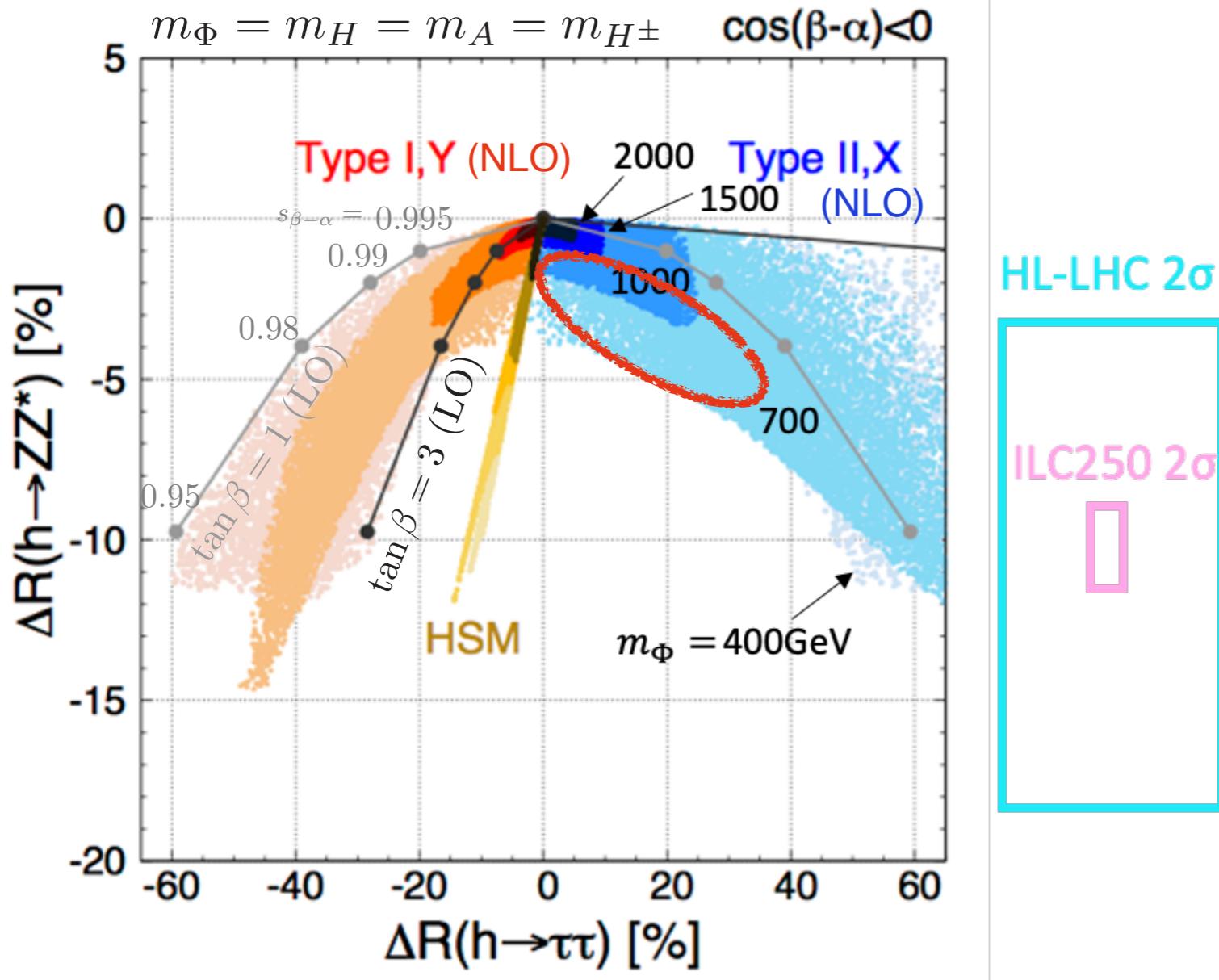


- Alignment w.o. decoupling is accessible by collider experiments.
- It is favored by measurements of the signal strength of  $h$  :  
 $c_{\beta-\alpha} \lesssim 0.3$  (0.1) for Type I (II)  
[ATLAS collaboration, PRD 101, 012002 (2020)]
- In near alignment region  
 $\kappa_X \neq 1$
- The scenario can be tested by future precision measurements of  $\kappa_X$ .
- Importantly, non-decoupling effects can be comparable with the precision measurements.

NLO corrections should be included to compare the experiments.

# Fingerprinting by Higgs boson decays

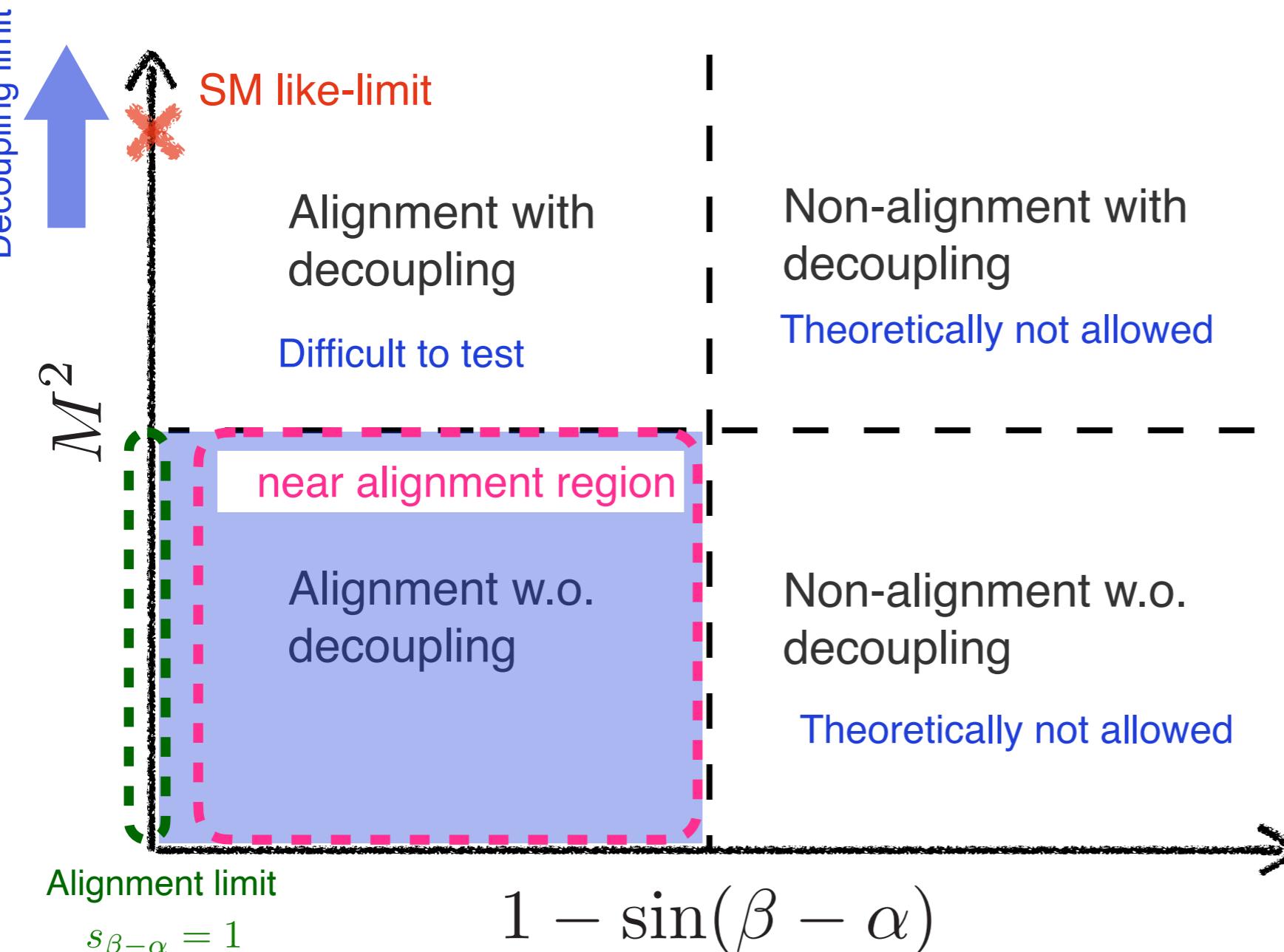
[Kanemura,Kikuchi,Mawatari,KS,Yagyu]



- We can distinguish the type of 2HDM.
- The size of deviation determine the upper bounds of  $m_\Phi$ .
- Theoretical predictions can be changed by loop effects within several %.
  - Future precision measurements is needed to detect the loop effect.

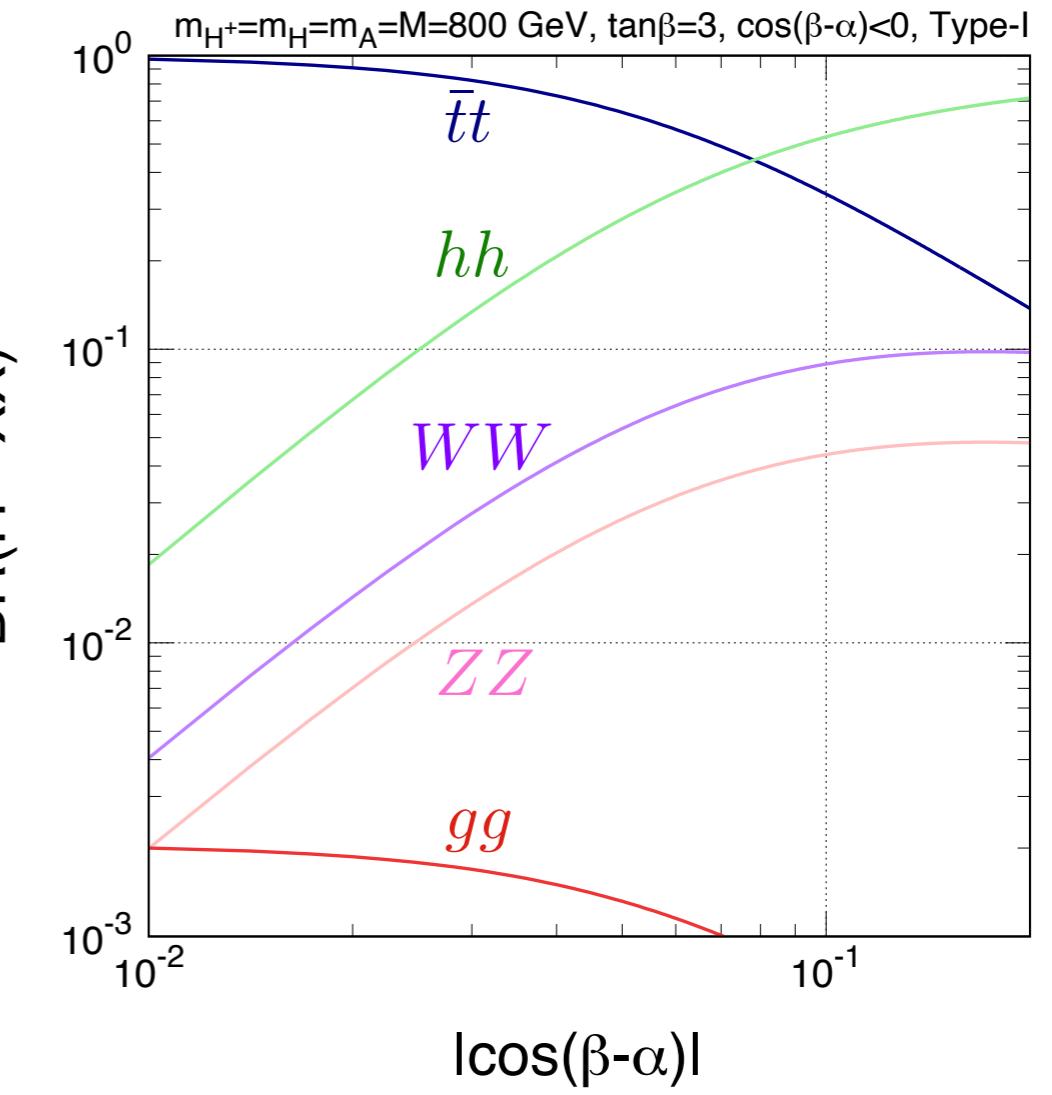
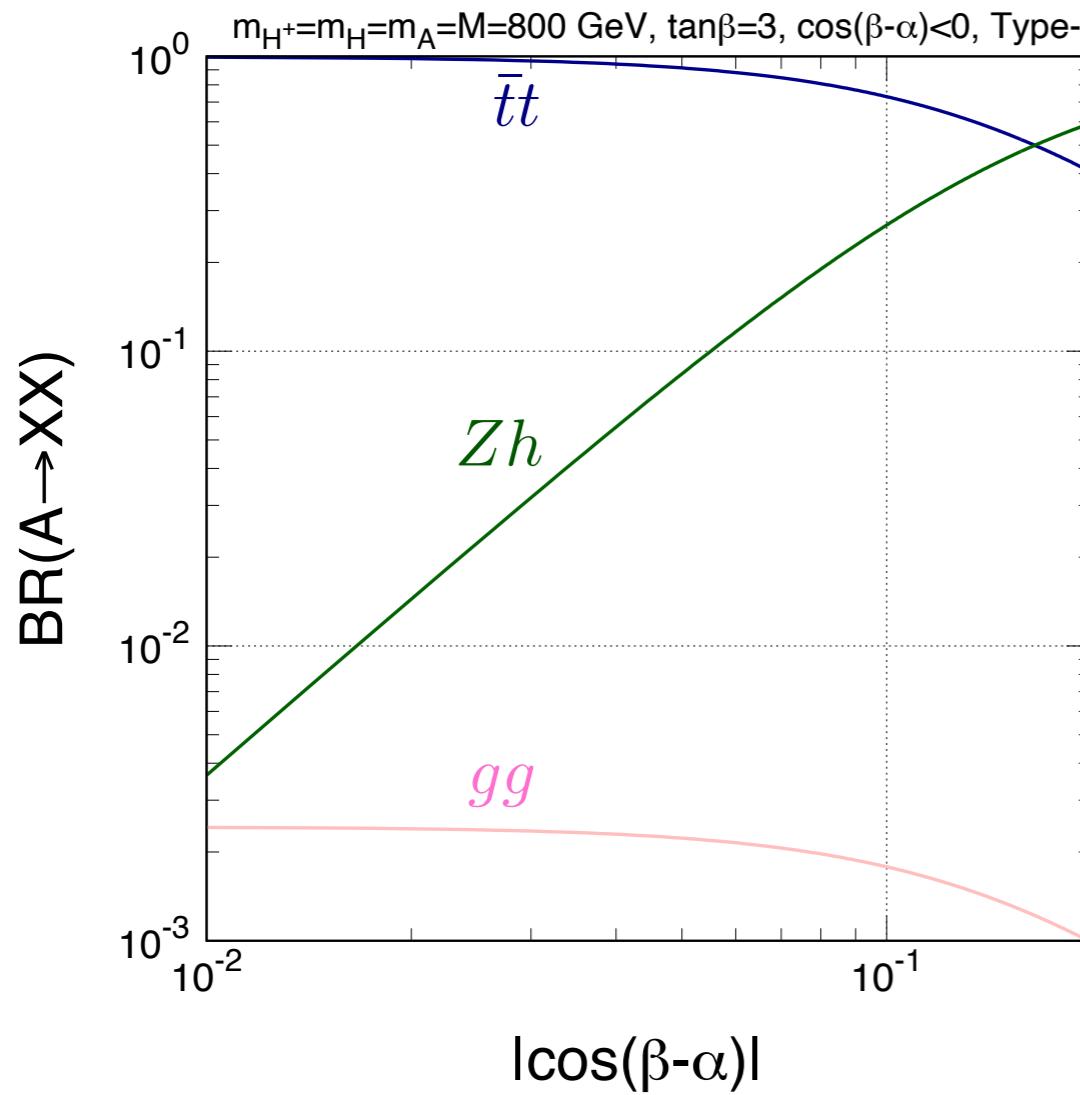
$$\Delta R(h \rightarrow XX) = \frac{\Gamma(h \rightarrow XX)}{\Gamma(h \rightarrow XX)_{\text{SM}}} - 1$$

# Distinct scenarios



- Heavy Higgs boson is relatively light.
- Large parameter regions can be probed by a synergy between direct searches of  $\Phi$  and the indirect searches.

# Branching ratios for the Heavy Higgs bosons



- $\sin(\beta - \alpha) = 1 : A, H \rightarrow \bar{t}t$  are dominant process.

$$\Gamma(A \rightarrow Zh) \propto \cos(\beta - \alpha)^2 \frac{m_A^3}{16\pi v^2}$$

- $\sin(\beta - \alpha) \neq 1$ : Scalar to scalar decays are important

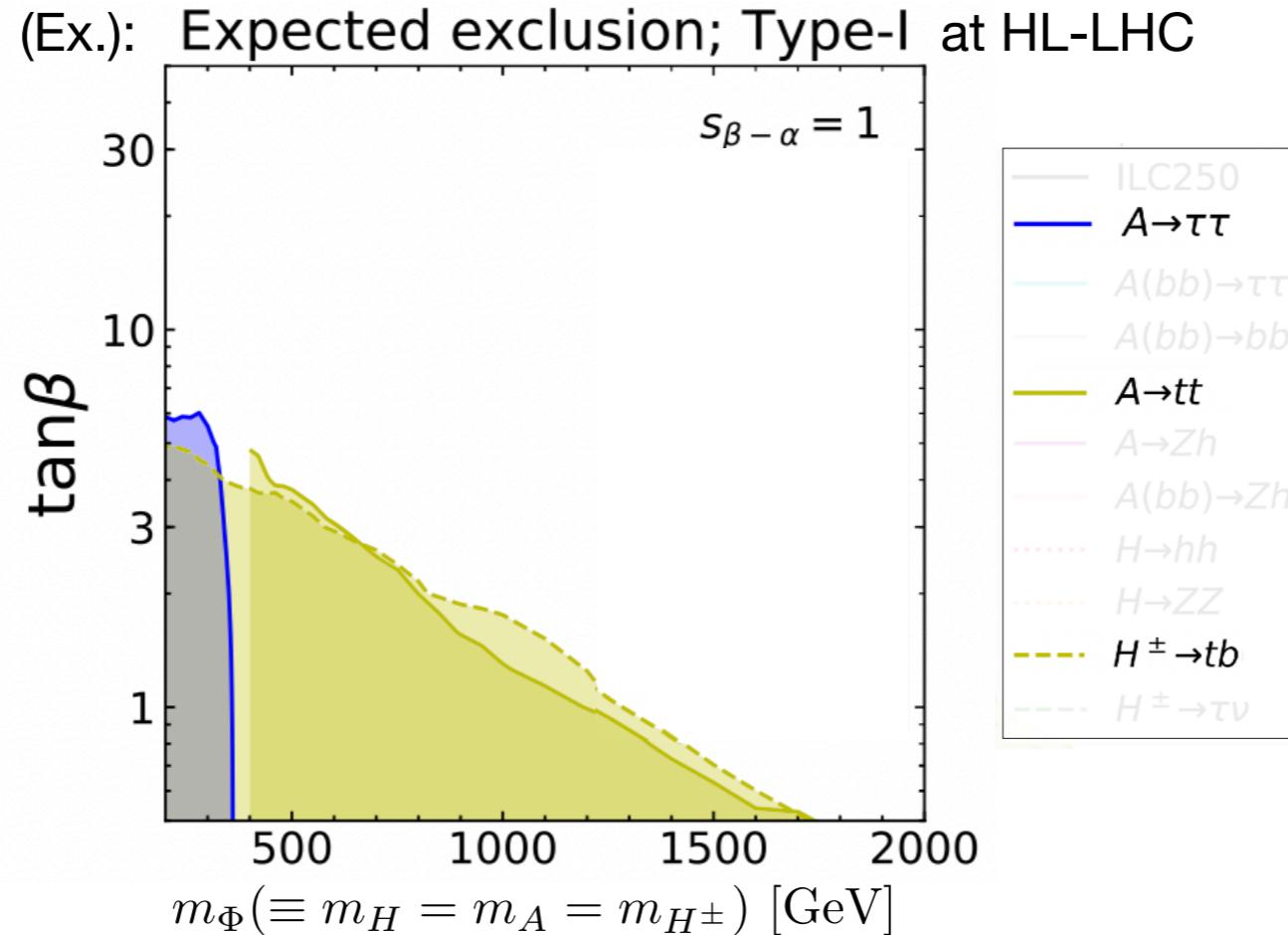
$$\Gamma(H \rightarrow hh) \sim \cos(\beta - \alpha)^2 \frac{m_H^3}{16\pi v^2}$$

→ Behaviors of BRs strongly depend on the alignment parameter.

# Synergy between direct and indirect searches[1/3]

Alignment limit:  $\sin(\beta - \alpha) = 1$

[M. Aiko, S. Kanemura, M. Kikuchi, K. Mawatari, KS, K. Yagyu, NPB 966 (2021) 115375]



$$s_{\beta - \alpha} : \sin(\beta - \alpha)$$

$$c_{\beta - \alpha} : \cos(\beta - \alpha)$$

$$\Gamma(A \rightarrow f\bar{f}) \propto \frac{m_A}{\tan^2 \beta}$$

$$\Gamma(H^+ \rightarrow t\bar{b}) \propto \frac{m_{H^\pm}}{\tan^2 \beta}$$

Direct searches : Lower bounds for  $m_\Phi$  and  $\tan\beta$  are given.

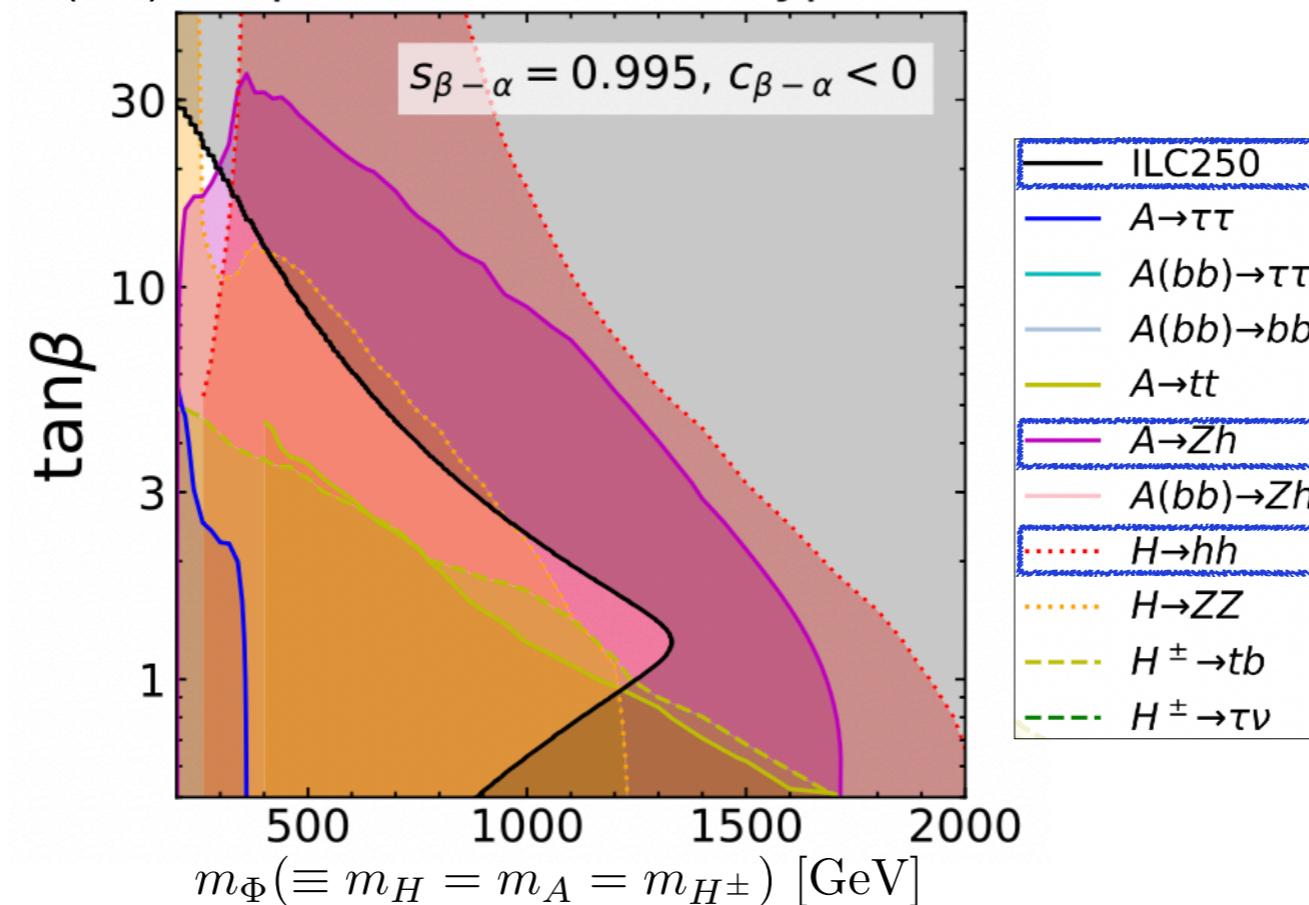
Indirect searches : No sensitivity since Higgs couplings do not deviate.

# Synergy between direct and indirect searches[2/3]

Near alignment scenario:  $\sin(\beta - \alpha) = 0.995$

[M. Aiko, S. Kanemura, M. Kikuchi, K. Mawatari, KS, K. Yagyu, NPB 966 (2021) 115375]

(Ex.): Expected exclusion; Type-I at HL-LHC



$$s_{\beta-\alpha} : \sin(\beta - \alpha)$$

$$c_{\beta-\alpha} : \cos(\beta - \alpha)$$

$$\Gamma(A \rightarrow Zh) \propto \cos(\beta - \alpha)^2 \frac{m_A^3}{16\pi v^2}$$

$$\Gamma(H \rightarrow hh) \sim \cos(\beta - \alpha)^2 \frac{m_H^3}{16\pi v^2}$$

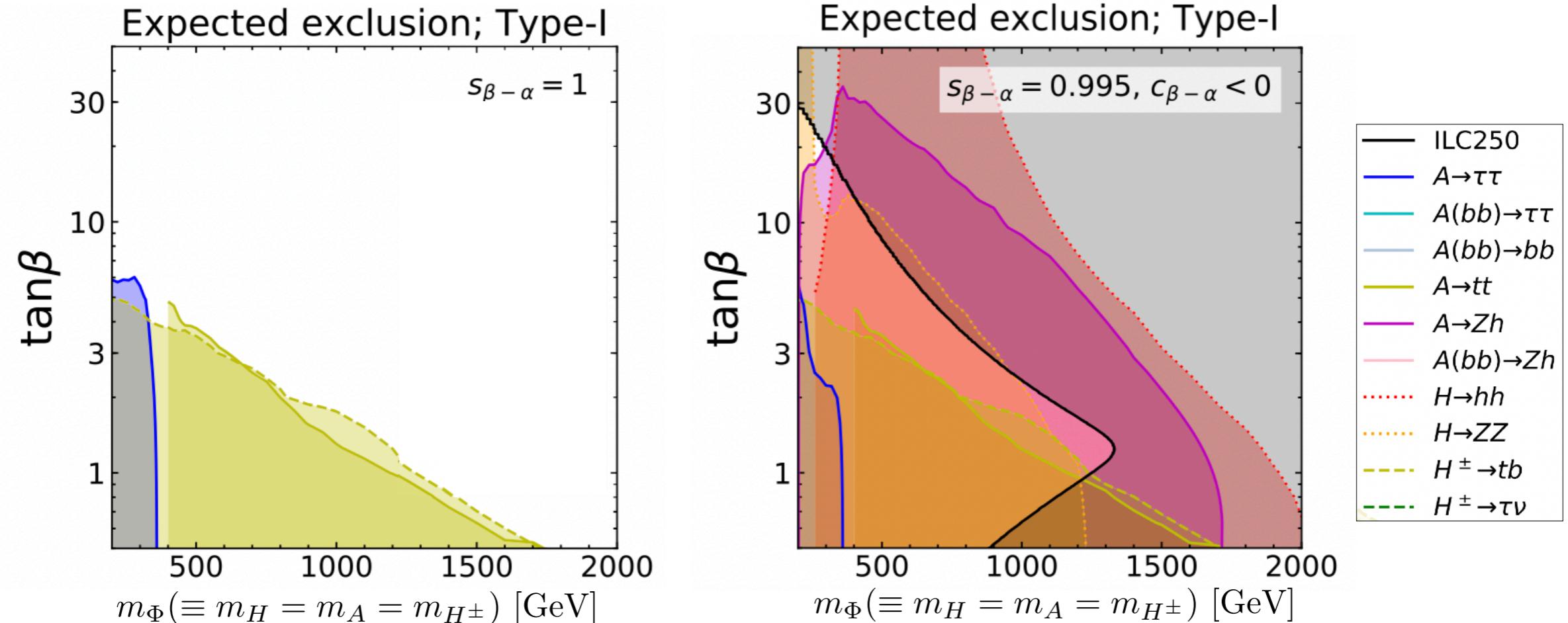
Direct searches :  $A \rightarrow Zh$  and  $H \rightarrow hh$  give wider sensitivity regions for  $(m_\Phi, \tan\beta)$  plane.

Indirect searches : If a deviation in  $hZZ$  founds, the upper bounds for  $m_\Phi$  are given.

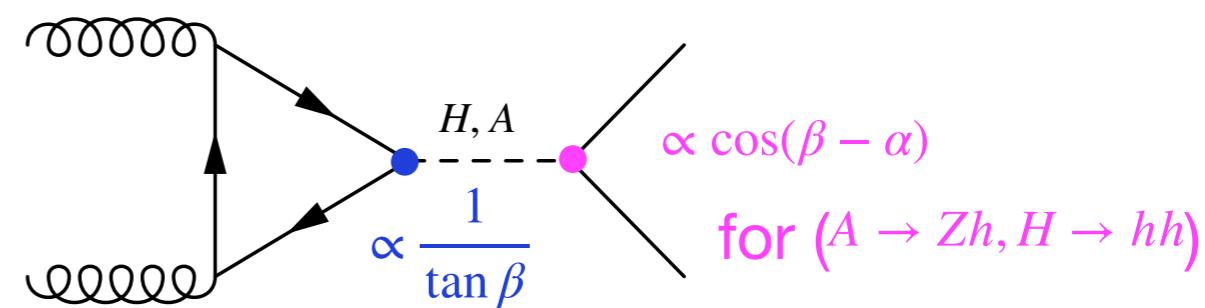
→ Most parameter space can be surveyed by the combination of Scalar-to scalar decays and precision measurements of the Higgs coupling.

# Importance of NLO corrections to heavy Higgs

[M. Aiko, S. Kanemura, M. Kikuchi, K. Mawatari, KS, K. Yagyu, NPB 966 (2021) 115375]



Sensitivity regions by direct searches are drastically changed by  $\sin(\beta - \alpha)$ , especially for BRs.



→ Loop effect to heavy Higgs decays can be significant. We should include it in alignment w/o the decoupling scenario.

# H-COUP

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We have calculated full NLO corrections to two-body decays of  $H, A, H^\pm$ .  
They will be implemented in H-COUP ver. 3.

## H-COUP

Fortran program to evaluate loop-corrected Higgs observables  
in the improved on-shell scheme.

[Kanemura, Kikuchi, KS,  
Mawatari, Yagyu]  
  
[Aiko, Kanemura, Kikuchi,  
KS, Yagyu]

Observables (NLO EW+NNLO QCD)

(v2.0):  $\text{BR}(h \rightarrow ff), \text{BR}(h \rightarrow VV^*), \lambda_{hhh}$

(v3.0):  $\text{BR}(\Phi \rightarrow ff), \text{BR}(\Phi \rightarrow SV/VV), \text{BR}(\Phi \rightarrow SS)$

Model

- Higgs Singlet model
- Two Higgs doublet models
- Inert doublet model

- Heavy Higgs decays for all models

Predictions for each model are evaluated in the same scheme

# Open questions

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## Impact of NLO corrections to scalar-to-scalar decays (e.g, $A \rightarrow Zh, H \rightarrow hh$ )

- How large is the size of NLO corrections?  
What is the origin of sizable corrections?
- Correlation between heavy Higgs boson decays and observables for  $h_{125}$  at 1-loop level.

Definition of Alignment limit:  $\kappa_V = 1$

(tree):  $\kappa_V = \sin(\beta - \alpha)$

(loop):  $\kappa_V = \sin(\beta - \alpha) + (\text{loop corrections})$

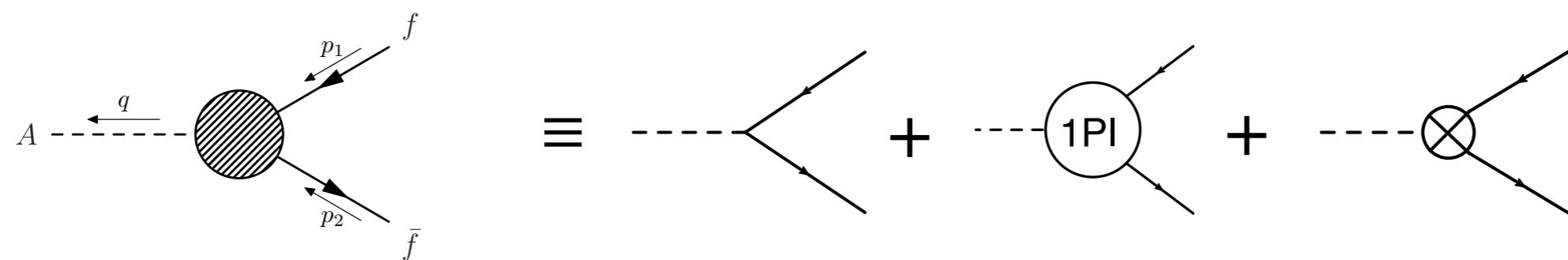
The dependence of  $\Gamma_{A \rightarrow Zh, H \rightarrow hh}$  on  $\kappa_V$  may change from the tree-level analysis.

## Detail of calculations

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# Details of the calculations of NLO EW corrections

Ex).  $A \rightarrow ff$



Renormalization scheme : on-shell scheme

$\delta m_\phi, \delta Z_{\phi_1\phi_2} :$  } On-shell    ← The CTs are renormalized by  $\hat{\Pi}_{ij}(p^2)$   
 $\delta \alpha, \delta \beta :$  }

$\delta M^2 : \overline{\text{MS}}$  scheme

Another choice:  $\hat{\Gamma}_{\Phi \rightarrow SS} = 0$

- Limit for parameter space by kinematics
- Numerical instability [M. Krause, M. Muhlleitner, R. Santos, H. Ziesche]

$\delta T_h, \delta T_H$ : standard tadpole scheme, alternative tadpole scheme

# Renormalization of tadpoles

- Standard tadpole scheme (STS) [W.F.L. Hollik, Fortschr. Phys. 38 (1990) 165.]

$$\left[ \begin{array}{l} t_i^B = t_i^R + \delta t_i \quad (i = h, H) \\ \hat{\Gamma}_i = t_R + \delta t_i + \Gamma_i^{1\text{PI}} \end{array} \right] \xrightarrow{(t_i^R = 0, \hat{\Gamma}_i = 0)} \delta t_i = -\Gamma_i^{1\text{PI}}$$

- Alternative tadpole scheme (ATS) [J. Fleischer and F. Jegerlehner, PRD23, 2001 (1981)]

$$\left[ \begin{array}{l} \Phi_m \rightarrow \Phi_m + \Delta v_m \quad (m = 1, 2) \\ \hat{\Gamma}_i = t^B + f(\Delta v_m) + \Gamma_i^{1\text{PI}} \end{array} \right] \xrightarrow{(t_i^B = 0, \hat{\Gamma}_i = 0)} \Delta v_m = \sum_i R_{mi} \Gamma_i^{1\text{PI}} / m_i^2$$

- Difference between STS and ATS

- While in STS tadpole affects only scalar self-energy, in ATS all self-energy has tadpole contributions.

- This makes self-energy gauge-independent at on-shell mass.

Gauge invariant CTs can be obtained in ATS.

$$\hat{\Pi}_{ij}^{\text{ATS}} = \hat{\Pi}_{ij} + \frac{1\text{PI}}{\text{---}}$$

# Gauge dependence in mixing angles

- In renormalization of mixing angle, there is a technical issue, namely, gauge dependence appears.  
[ Yamada, PRD64(2001)036008 ]
- We can check gauge dependence from Nielsen identify:

$$\partial_\xi \Pi_{ij} = (2p^2 - m_i^2 - m_j^2) \tilde{\Pi}_{ij}$$

$i, j = h, H, A, H^\pm$   
 $\tilde{\Pi}_{ij}$  : function of loop functions

- $i = j = h$  :  $\delta m_h^2 = \Pi_{hh}^{1\text{PI}}(m_h^2)$   
 $\partial_\xi \Pi_{hh}(p^2) = 0$  at  $p^2 = m_h^2$   $\rightarrow$   $\delta m_h^2$  is gauge-independent.
- $i = h, j = H$  :  $\delta\alpha = \{\Pi_{hH}^{1\text{PI}}(m_h^2) + \Pi_{hH}^{1\text{PI}}(m_H^2)\}/(m_H^2 - m_h^2)$   
 $\partial_\xi \Pi_{Hh} \neq 0$  at  $p^2 = m_H^2 = m_h^2$ ,  $\rightarrow$  Gauge dependence for  $\delta\alpha$

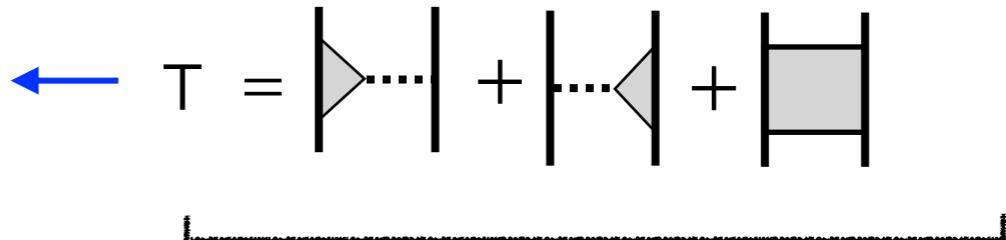
- Though this, the decay amplitudes are also gauge-dependent.

$$\begin{aligned}\frac{\partial \mathcal{M}_{A \rightarrow Z h}}{\partial \xi} &= \frac{\partial}{\partial \xi} \left( \mathcal{M}_{A \rightarrow Z h}^{\text{tree}} + \mathcal{M}_{A \rightarrow Z h}^{1\text{PI}} + \delta \mathcal{M}_{A \rightarrow Z h} \right) \\ &= \frac{\partial}{\partial \xi} \left( \underline{\mathcal{M}_{A \rightarrow Z h}^{1\text{PI}}} + f(\delta Z_i) + g(\delta\alpha, \delta\beta) + h(\delta m_i) \right) = \frac{\partial}{\partial \xi} g(\delta\alpha, \delta\beta) \neq 0 \\ &= 0\end{aligned}$$

# Gauge independent renormalization of mixing angles

- In order to remove the gauge dependence in  $\delta\alpha$ ,  $\delta\beta$ , we utilize pinch technique.

Basic idea:  $\Pi_{Hh} \rightarrow \Pi_{Hh} + \Pi_{Hh}^{\text{Pinch}}$



$$\rightarrow \partial_\xi \delta\alpha = 0, \partial_\xi \delta\beta = 0$$

This should arise from the full NLO amp.  
e.g.,  $gg \rightarrow A/H \rightarrow \bar{f}f$

$$\mathcal{M}_{gg \rightarrow h/H \rightarrow \bar{f}f}^{\text{NLO}} \ni \mathcal{M}_{gg \rightarrow h/H \rightarrow \bar{f}f}^{\text{SE-like}}$$

- Another scheme for mixing angles in gauge invariant way

-  $p_*$  scheme :  $\hat{\Pi}_{Hh}(p^2 = [m_H^2 + m_h^2]/2) = 0$  [ Espinosa, Yamada, PRD67(2003) 036003 ]

- On-shell conditions with S matrix (THDM+  $\nu_{Ri}$  ( $i=1,2$ ),  $y_{\nu i} \rightarrow 0$ ) [ Denner, Dittmaier, Lang, JHEP 1811(2018)104 ]

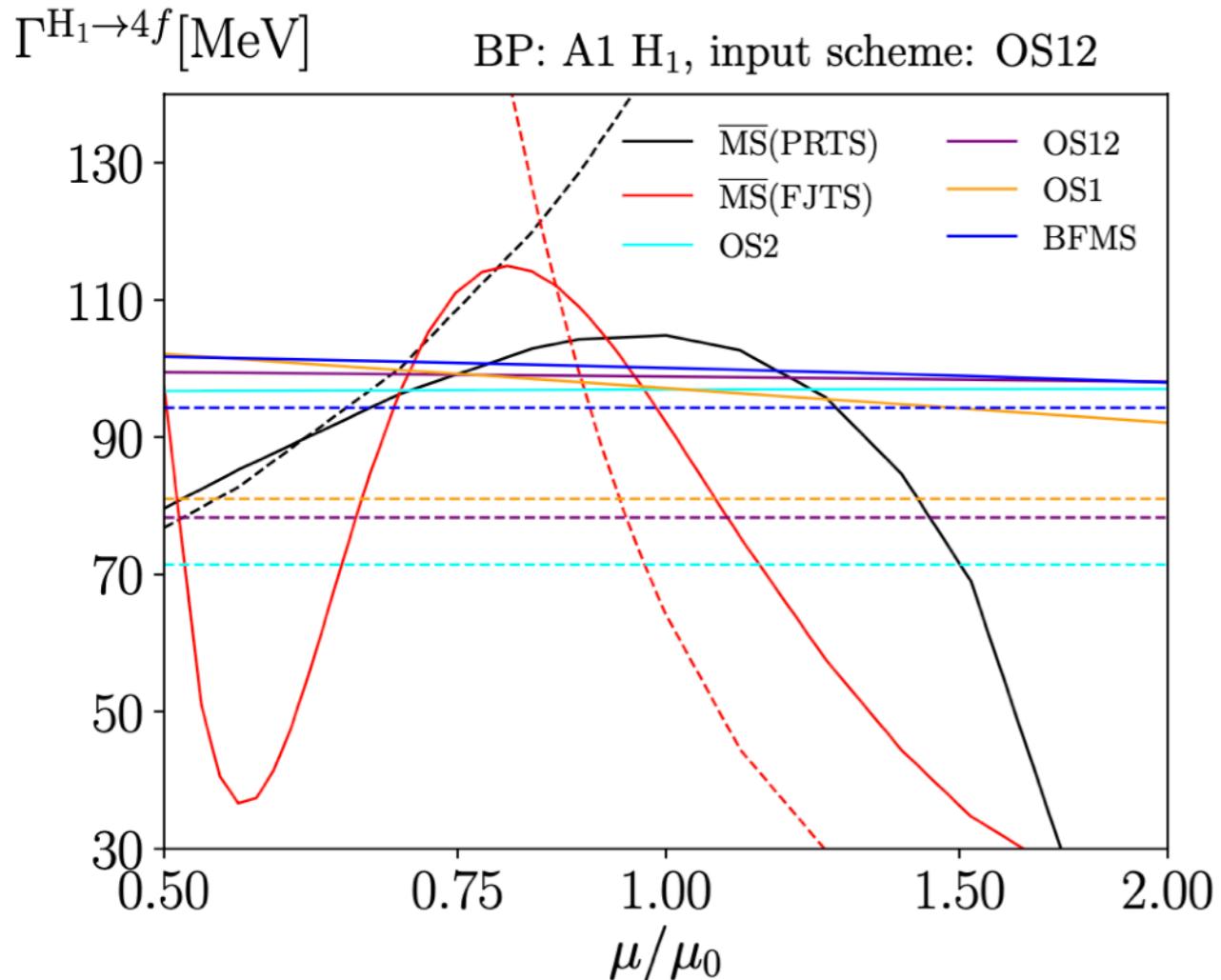
$$\frac{\mathcal{M}_{H \rightarrow \nu_{R1}\nu_{R1}}^{\text{loop}}}{\mathcal{M}_{h \rightarrow \nu_{R1}\nu_{R1}}^{\text{loop}}} = \frac{\mathcal{M}_{H \rightarrow \nu_{R1}\nu_{R1}}^{\text{tree}}}{\mathcal{M}_{h \rightarrow \nu_{R1}\nu_{R1}}^{\text{tree}}} = \frac{c_\alpha}{s_\alpha}$$

$$h \ (H) \quad \cdots \begin{array}{l} \nearrow \nu_{Ri} \\ \searrow \nu_{Ri} \end{array} = y_{\nu_i} c_\alpha (s_\alpha)$$

# Scheme difference in counterterms of mixing angles

[A. Denner, S. Dittmaier, J.N. Lang, 1808.03466]

BP: A1     $M_{H_2} = 125\text{GeV}$ ,  $M_{H_1} = 300\text{GeV}$ ,  $M_{A,H^\pm} = 460\text{GeV}$ ,  
 $\lambda_5 = -1.9$ ,  $t_\beta = 2$ ,  $c_{\beta-\alpha} = 0.1$ ,  $\mu_0 = (m_{H_2} + m_{H_1} + M_A + 2M_{H^\pm})/5$



Scheme	A1	
	LO	NLO
$\overline{\text{MS}}(\text{PRTS})$	$147.102(4)^{+100\%}_{-47.8\%}$	$104.86(2)^{-100\%}_{-24.1\%}$
$\overline{\text{MS}}(\text{FJTS})$	$64.096(2)^{-86.9\%}_{>+100\%}$	$92.17(1)^{-81.4\%}_{+5.6\%}$
OS1	$80.992(2)$	$97.145(7)^{-5.2\%}_{+5.1\%}$
OS2	$71.429(2)$	$96.95(1)^{+0.1\%}_{-0.2\%}$
OS12	$78.304(2)$	$98.812(8)^{-0.8\%}_{+0.7\%}$
BFMS	$94.265(2)$	$100.117(5)^{-2.2\%}_{+1.6\%}$

OS1,2,12: On shell with  $H, h \rightarrow \nu_{Ri}\bar{\nu}_{Ri}$   
BFMS: On-shell with  $\hat{\Pi}_{Hh}$  and the PT

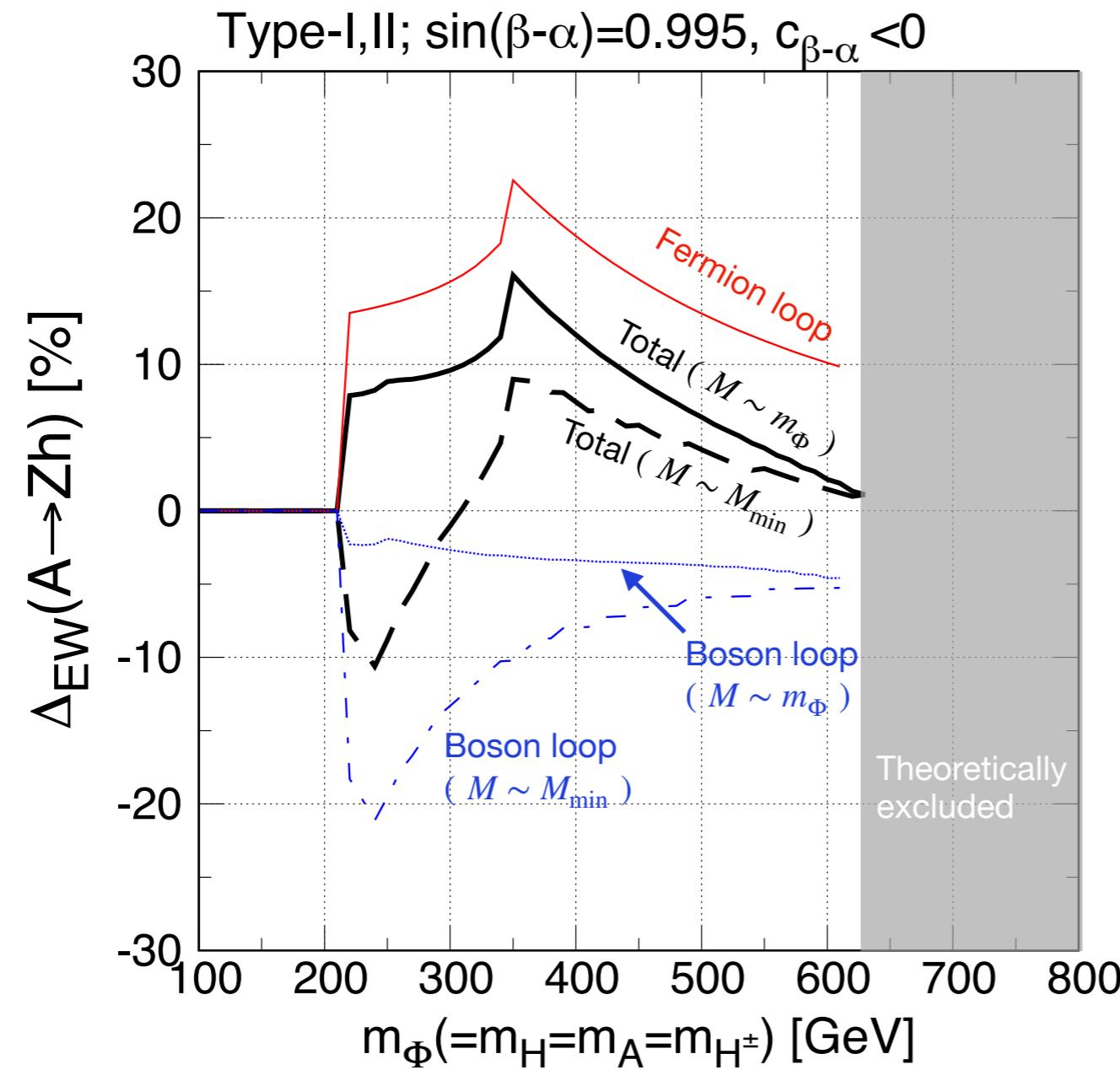
Theoretical uncertainty (scheme difference) for on-shell scheme is a few %.

## Results for $A \rightarrow Z h$ and $H \rightarrow hh$

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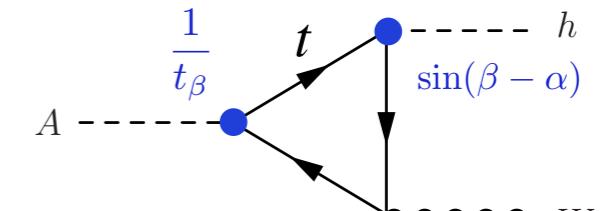
# Non-decoupling effects in $\Gamma_{A \rightarrow Zh}$

[M. Aiko, S. Kanemura, KS]



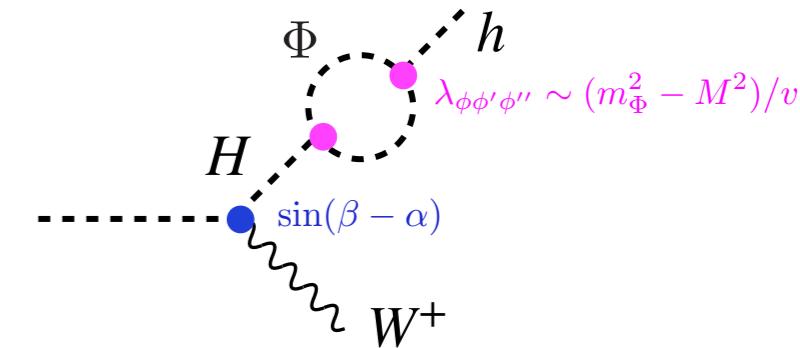
Typical graph :

fermion loop      Suppression by  $t_\beta$ ,  $m_\Phi^2$



$$\mathcal{M}_{A \rightarrow Zh}^F \sim -\frac{1}{16\pi^2} \frac{s_{\beta-\alpha}}{t_\beta} \frac{m_t^4}{v^2 m_\Phi^2} \quad (m_t \ll m_\Phi)$$

Boson loop      Nondecoupling effects

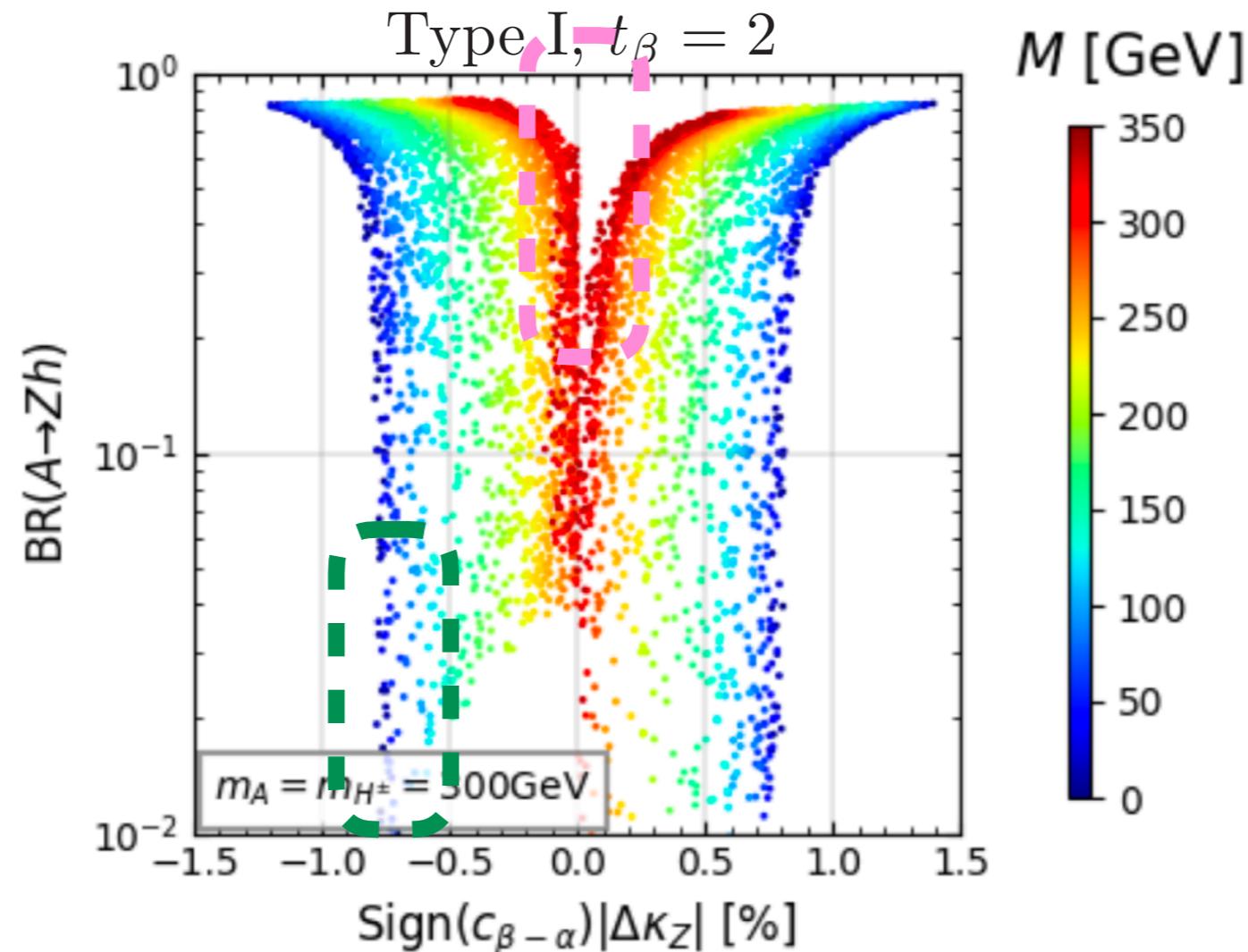


$$\mathcal{M}_{A \rightarrow Zh}^B \sim \begin{cases} \frac{1}{16\pi^2} s_{\beta-\alpha} \frac{m_\Phi^2}{v^2} & (M \sim v) \\ \frac{1}{16\pi^2} s_{\beta-\alpha} \frac{m_h^4}{v^2 m_\Phi^2} & (M \gg v) \end{cases}$$

- Some diagrams are not suppressed by  $c_{\beta-\alpha}$ .
- Fermion loop and Boson loop are destructive. → Total corrections reach ~15%.

# BR(A → Zh) vs $\Delta\kappa_Z$

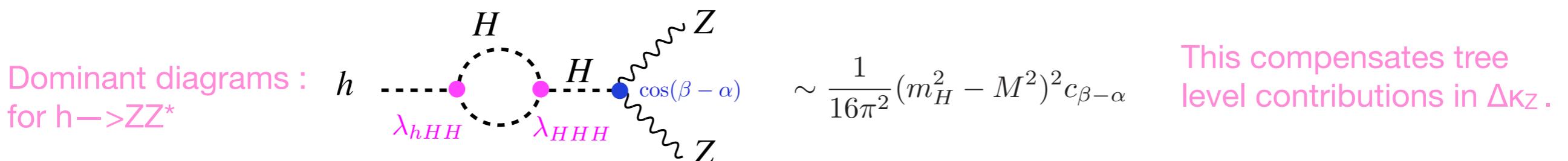
[M. Aiko, S. Kanemura, KS]



$$\Delta\kappa_Z = \frac{\Gamma_{h \rightarrow ZZ^*}^{2\text{HDM}}}{\Gamma_{h \rightarrow ZZ^*}^{\text{SM}}} - 1$$

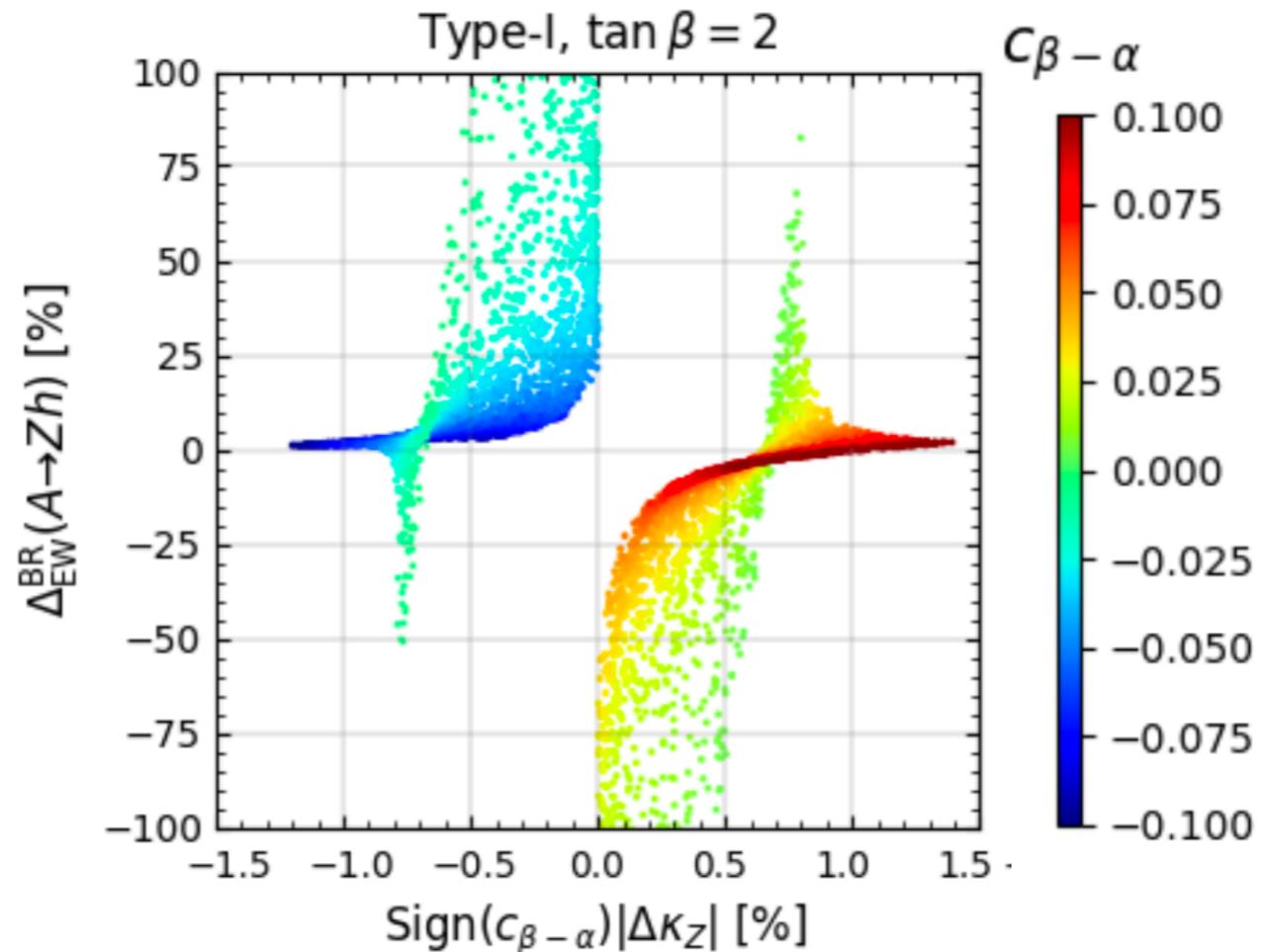
$M^2 \simeq 0, c_{\beta-\alpha} \simeq 0$  : Nondecoupling effect of  $H, A, H^\pm$  enhances  $\Delta\kappa_Z \rightarrow \Delta\kappa_Z \neq 0$  but  $\text{BR} \sim 1\%$

$M^2 \simeq m_A^2, |c_{\beta-\alpha}| \sim 0.1$  : Nondecoupling effect of  $H$  can affect  $\rightarrow \Delta\kappa_Z \sim 0$  but  $\text{BR} \sim O(10)\%$



# NLO corrections for $\text{BR}(A \rightarrow Zh)$

[M. Aiko, S. Kanemura, KS]



$$\Delta_{\text{EW}}^{\text{BR}} = \frac{\text{BR}_{A \rightarrow Zh}^{\text{NLO}}}{\text{BR}_{A \rightarrow Zh}^{\text{LO}}} - 1$$

$|c_{\beta-\alpha}| \sim 0.1$  :  $\Delta^{\text{BR}}$  is close to 0%

$$\Delta_{\text{EW}}^{\text{BR}} = \frac{1 + \Delta_{A \rightarrow Zh}^{\text{EW}}}{1 + \Delta_{\text{tot}}^{\text{EW}}} - 1 \simeq 0$$

$\sim \Delta_{A \rightarrow Zh}^{\text{EW}}$

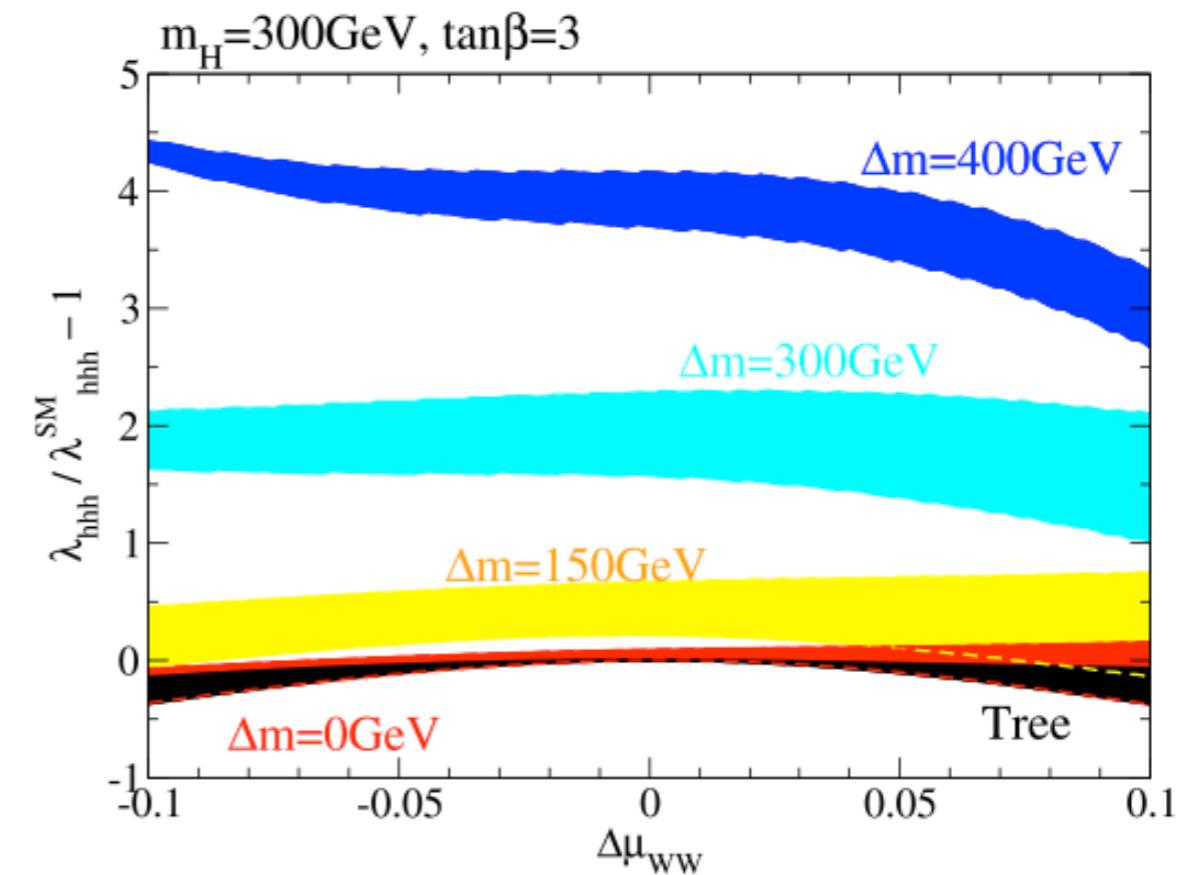
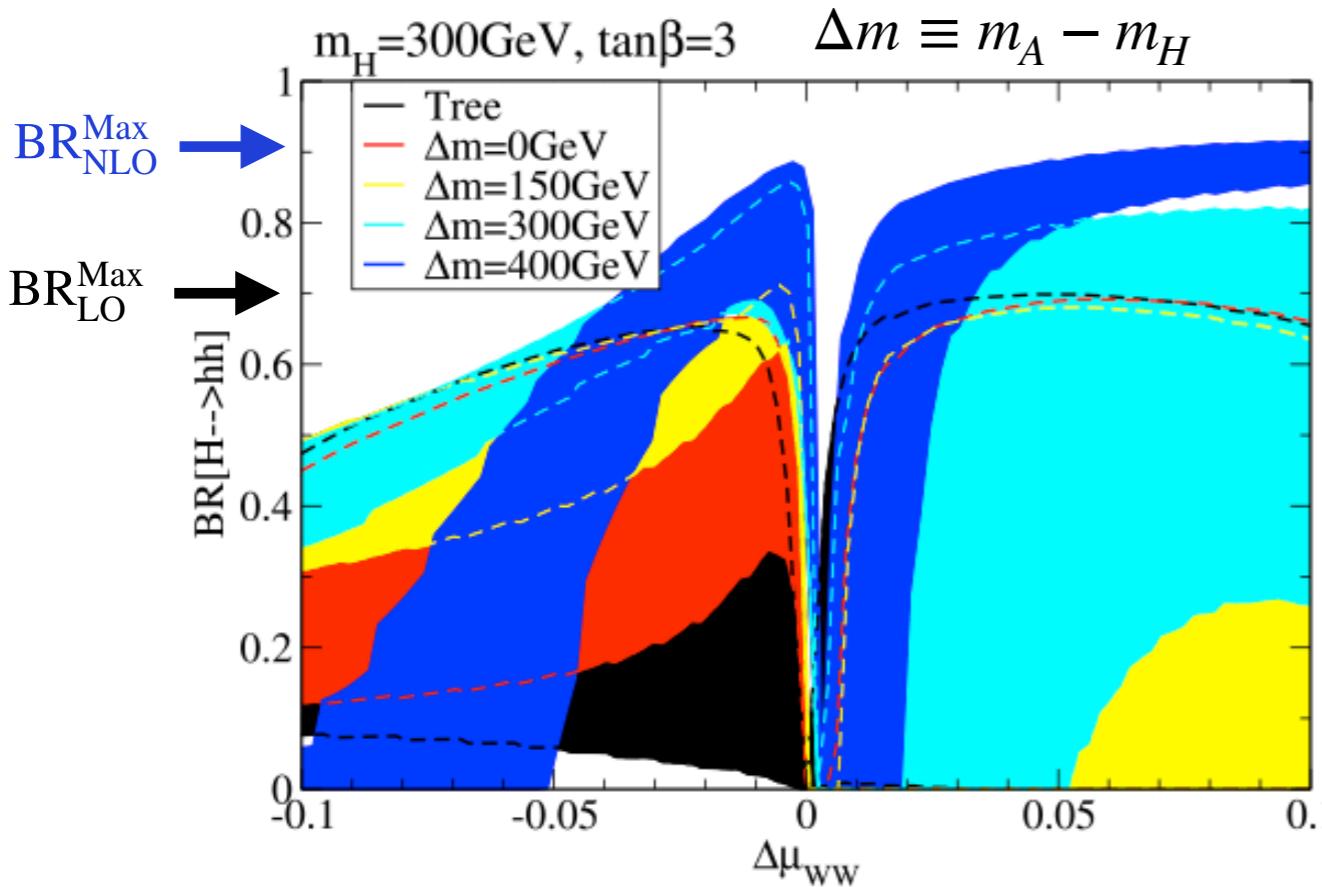
$|\Delta\kappa_Z| \lesssim 0.5\% :$   $\Delta^{\text{BR}}$  can exceed 100%

$$|\mathcal{M}(A \rightarrow Zh)|^2 = C_{AZh} \left( \frac{g_Z^2}{4} c_{\beta-\alpha}^2 + g_Z c_{\beta-\alpha} \text{Re}\Gamma_{AZh}^{\text{loop}} + |\Gamma_{AZh}^{\text{loop}}|^2 \right)$$

Tree                  1-loop

# Correlation between $\Gamma_{H \rightarrow hh}$ and $\lambda_{hhh}$

[Kanemura, Kikuchi, Yagyu]



Nondecoupling effect in  $\Gamma_{H \rightarrow hh}$  predicts sizable deviation in  $\lambda_{hhh}$ .

→ if  $H$  is discovered and the BRs are precisely determined, the scenario of EWBG can be tested.

$$\boxed{\text{Realization of strong 1st OPT} \iff \frac{\lambda_{hhh}}{\lambda_{hhh}^{\text{SM}}} - 1 \gtrsim 10\%}$$

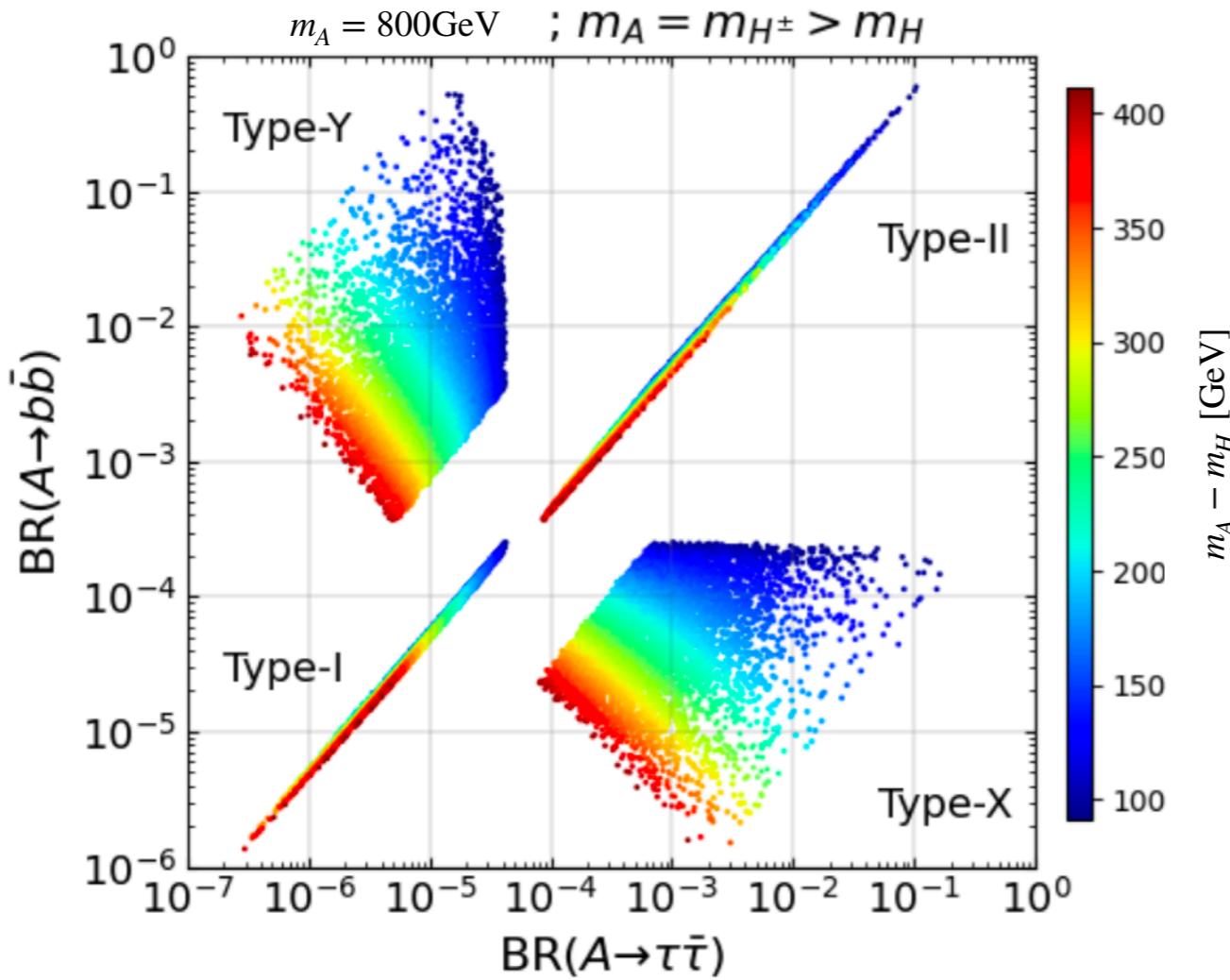
[S. Kanemura, Y. Okada, E. Senaha,  
*Phys.Lett.B* 606 (2005) 361]

# How can we discriminate types of 2HDMs?

Near alignment regions ( $\sin(\beta - \alpha) \neq 1$ )  $\rightarrow$  precise measurements of  $h$  (ILC, CLIC, FCC-ee, etc.)

Exact alignment regions ( $\sin(\beta - \alpha) = 1$ )  $\rightarrow$  Decay pattern of  $A$  (HL-LHC, FCC-hh,  $\mu$  collider, etc.)

[M. Aiko, S. Kanemura, KS]



- Different  $\tan \beta$  dependence.  
$$\Gamma_{A \rightarrow f\bar{f}} \propto \begin{cases} \frac{m_A}{t_\beta^2} & (\text{type I}) \\ m_A t_\beta^2 & (\text{type II}) \end{cases}$$
- Suppression by  $\Gamma_{A \rightarrow ZH} \propto (m_A - m_H)^2$
- $\Gamma_{A \rightarrow f\bar{f}}$  does not depends on  $\sin(\beta - \alpha)$   
 $\rightarrow$  Characteristic decay pattern of  $A$  even in alignment limit

→ Direct search of  $A$  and precision measurements of  $h$  are complimentary to determine Type.

# Summary

- Scalar-to-scalar decays (e.g.,  $A \rightarrow Z h, H \rightarrow hh$ ) are proportional to  $\cos(\beta - \alpha)$ . In near alignment region ( $\sin(\beta - \alpha) \neq 1$ ), loop corrections to those processes can be significant.
- We calculated NLO corrections to two-body decays of heavy Higgs in 2HDMs.
- We discussed the correlation between heavy Higgs decays and observables for  $h_{125}$  at the 1-loop level.

Loop corrections can affect both of them. Correlations at loop level are changed from the tree-level analysis.

