

Measurement of the W boson mass at Tevatron

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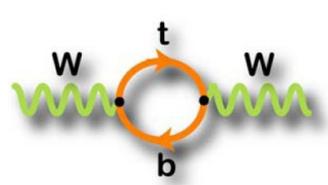


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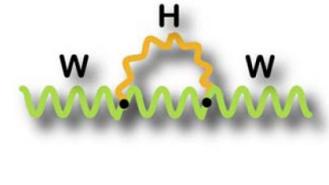
Motivation for precise W mass

- Precise measurements of m_W and m_t can constrain SM Higgs mass

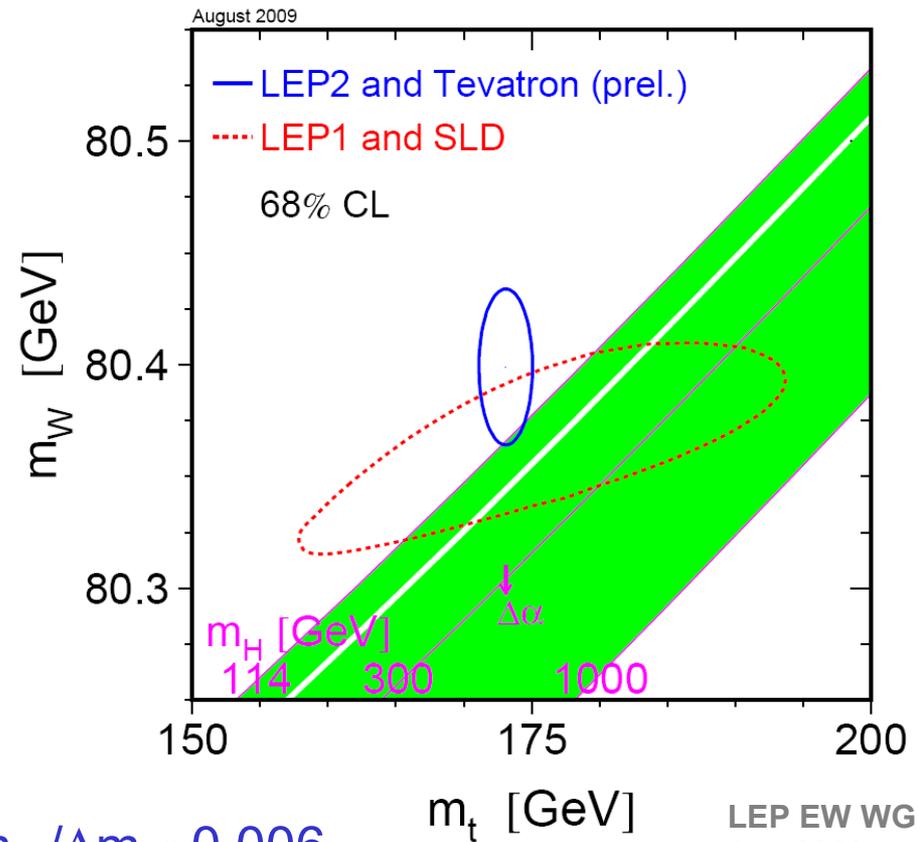
$$m_W = \sqrt{\frac{\pi\alpha}{\sqrt{2}G_F}} \cdot \frac{1}{\sin\theta_W \sqrt{1 - \Delta r}}$$



$$\Delta r \propto m_t^2$$



$$\Delta r \propto \log m_H$$



- Δm_W has same impact on Δm_H for $\Delta m_W / \Delta m_t \approx 0.006$
 - for recent $\Delta m_t = 1.3$ GeV would need: $\Delta m_W = 8$ MeV (0.01%)
 - current world average: $\Delta m_W = 23$ MeV (0.03%)

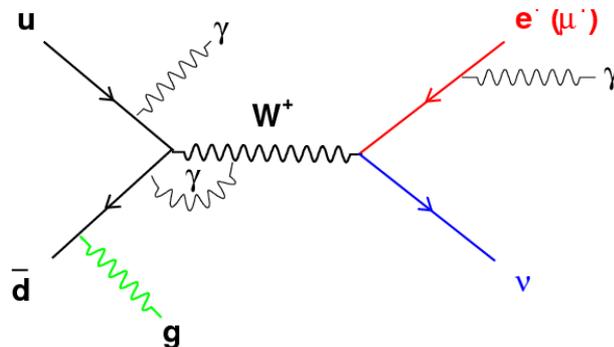
- Additional contributions to Δr arise in SM extensions...



Signatures & observables

- **Signature of W:**

- isolated, high p_T lepton (e or μ)
- missing E_T



- **Use 3 kinematic variables:** (Jacobian edge)

$$m_T = \sqrt{2 E_T^\ell \cancel{E}_T (1 - \cos \Delta\phi_{\ell\nu})}$$

→ affected by detector resolution (MET)

$$p_T^\ell$$

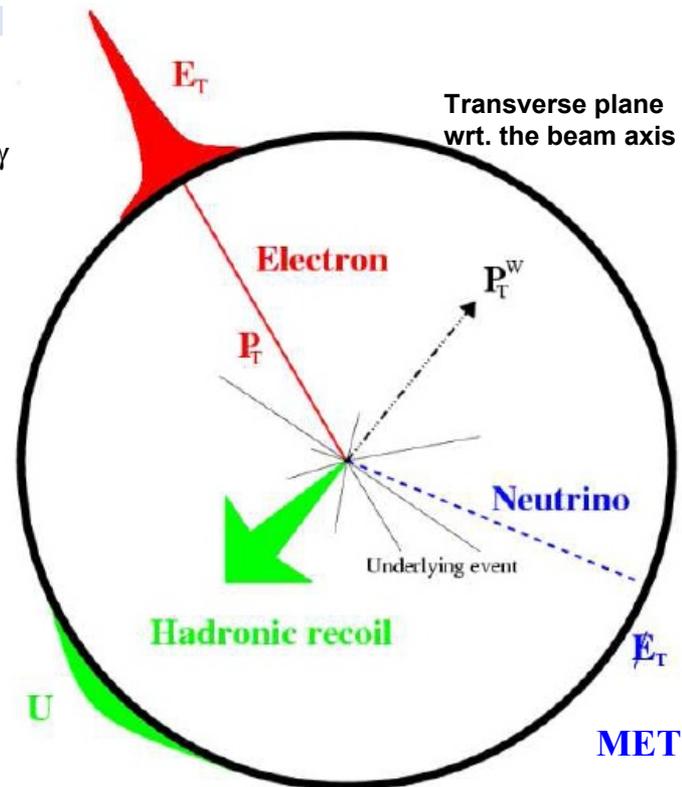
→ affected by motion of W boson (p_T^W)

$$p_T^\nu = \cancel{E}_T$$

→ sensitive to both effects, but is not 100% correlated with other 2 measurements

- **25 MeV precision on m_W requires :**

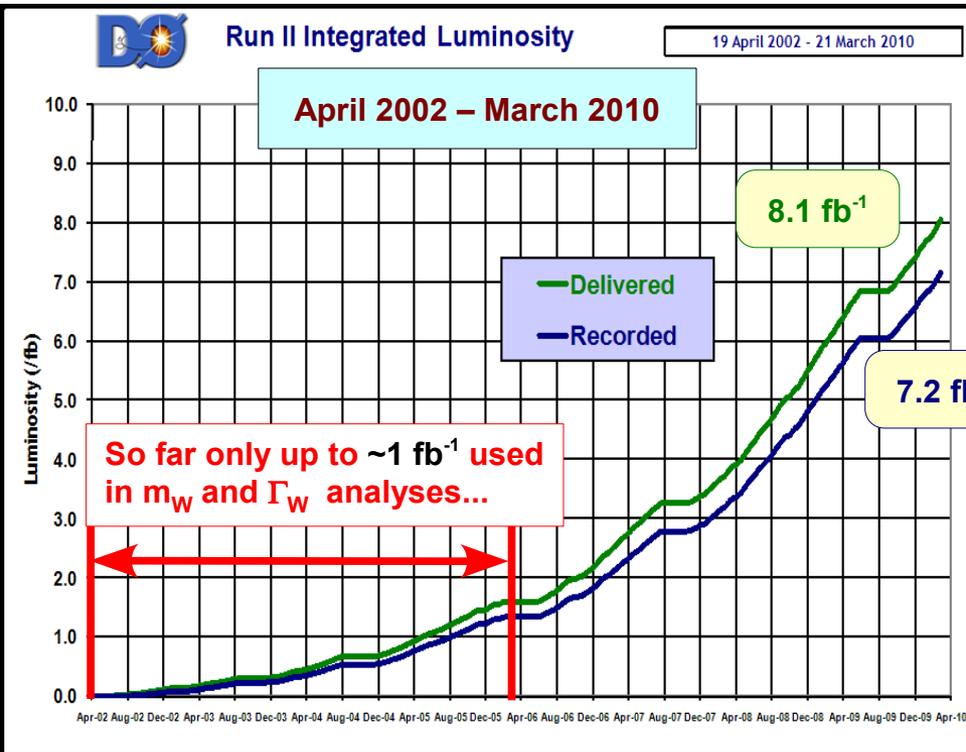
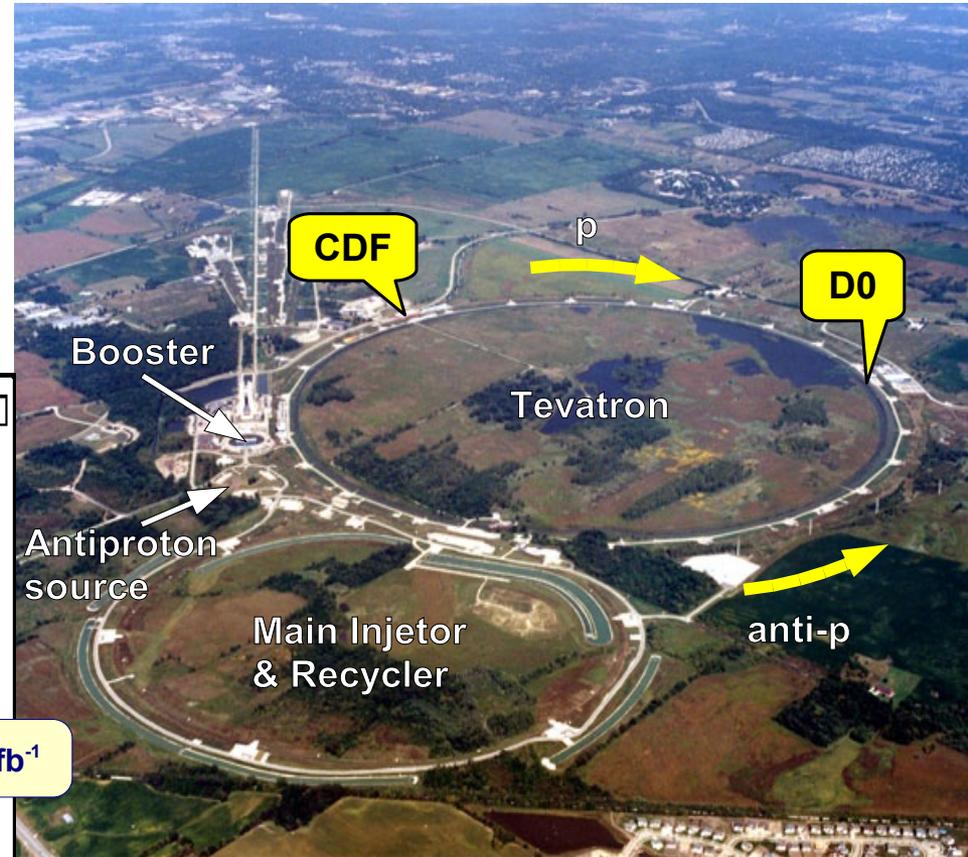
- accuracy of lepton (e or μ) energy scale: **~0.02%**
- accuracy of hadronic recoil scale: **~1%**



Tevatron at Fermilab



- Proton-antiproton @ $\sqrt{s}=1.96$ TeV
every 396 ns, 36x36 bunches
- Peak luminosity: $3.5 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
- Recorded: $\sim 7 \text{ fb}^{-1}$ / experiment



- By end of 2010: 9 fb^{-1} / experiment
- Running in 2011 is considered



Tevatron m_W analyses

	CDF	DØ
Luminosity	0.2 fb ⁻¹	1.0 fb ⁻¹
W decay channels	electron, muon	electron
Lepton Energy Scale	tracker information	Z→ee calorimeter data
Interpretation	absolute m_W	m_W/m_Z ratio
MC closure test	–	full analysis performed first on Monte Carlo
Beyond m_W	$M(W^+)$ and $M(W^-)$ comparison	–

PRL **99**, 151801 (2007)

PRL **103**, 141801 (2009)

+ their combination: arXiv:0908.1374v1 [hep-ex]



Analysis overview (DØ)

- The DØ analysis exploits **W→ev channel** only
electron energy resolution ~4%, muon momentum scale ~10% @ $p_T=50$ GeV
- Compare m_T, p_T^e, \cancel{E}_T **data spectra** with **template spectra** from **MC**
- Fast **Monte Carlo** for templates generation:
 - ResBos** – **W and Z/ γ^* boson production, decay kinematics**
perturbative NLO at high boson p_T , gluon resummation at low boson p_T
 - PHOTOS** – **FSR radiation of ≤ 2 photons**
effect of full QED corrections assessed from WGRAD and ZGRAD
 - Parametric MC Simulation (PMCS)** – **detector efficiencies, energy response & resolution for electrons and hadronic recoil**
parametric functions and binned look-up tables based on detailed GEANT simulation and fine-tuned from control data samples: Z→ee, Zero Bias, Minimum Bias
- **Blind analysis** – m_W returned by fits was deliberately shifted by **some unknown offset before the final fitting**
results were unblinded after completing all consistency checks for W and Z events



Event selection (DØ)

- **1 fb⁻¹ of data (Run IIa, 2002-2006)**
- **W → ev** sample – **499,830** evts:
 - Electron: $|\eta| < 1.05$, spatial track match, $p_T^e > 25$ GeV
 - Missing $E_T > 25$ GeV
 - Recoil $u_T < 15$ GeV
 - $50 < m_T < 200$ GeV

} cuts preserve
the Jacobian edge

96% purity, main backgrounds: $Z \rightarrow ee$, QCD multijet, $W \rightarrow \tau\nu \rightarrow ev\nu$

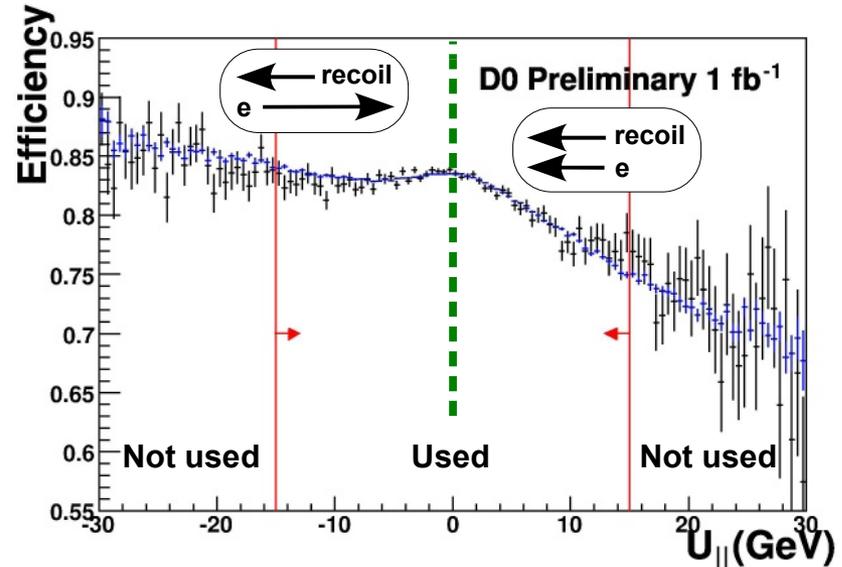
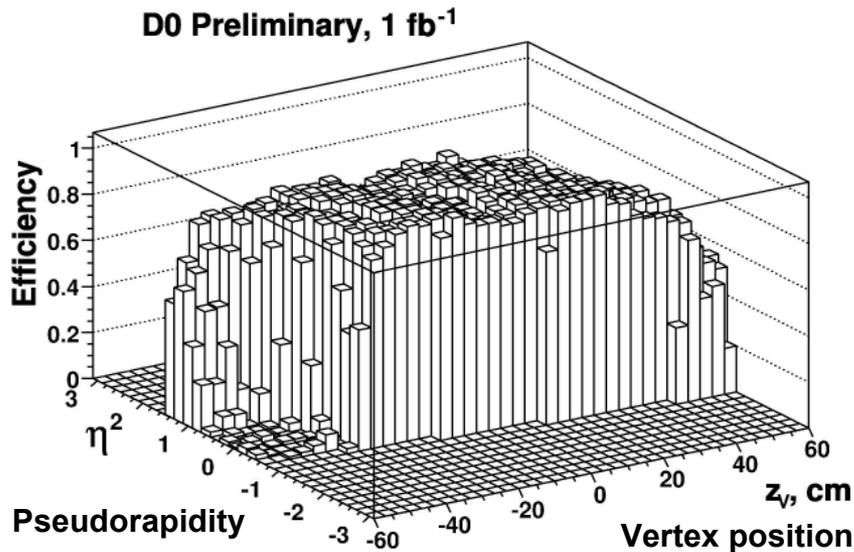
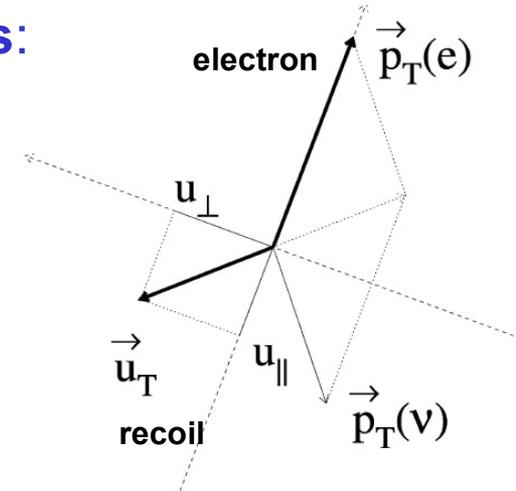
- **Z → ee** sample for calibration – **18,725** evts:
 - calibrate EM energy scale from Z pole
 - tune fast PMCS



Electron efficiency (DØ)

Fast MC models various **electron selection efficiencies**:

- **Electron-only**: trigger, CAL-based ID, tracking
from Z data; tag & probe; parameterized using: η^e , p_T^e , z_{vtx}
- **W event topology**: spatial proximity recoil \leftrightarrow electron
from Z data; parameterized using: p_T^e , u_{\parallel}
- **Additional hadronic energy** in CAL at high luminosity
from full MC + ZB data; parameterized using: Scalar E_T , u_{\parallel}



Electron model (DØ)

- Fit amount of **uninstrumented** material in front of the calorimeter with $0.01X_0$ precision
- Use precise Z mass from LEP to calibrate absolute EM energy scale
- **Simulate measured electron energy as:**

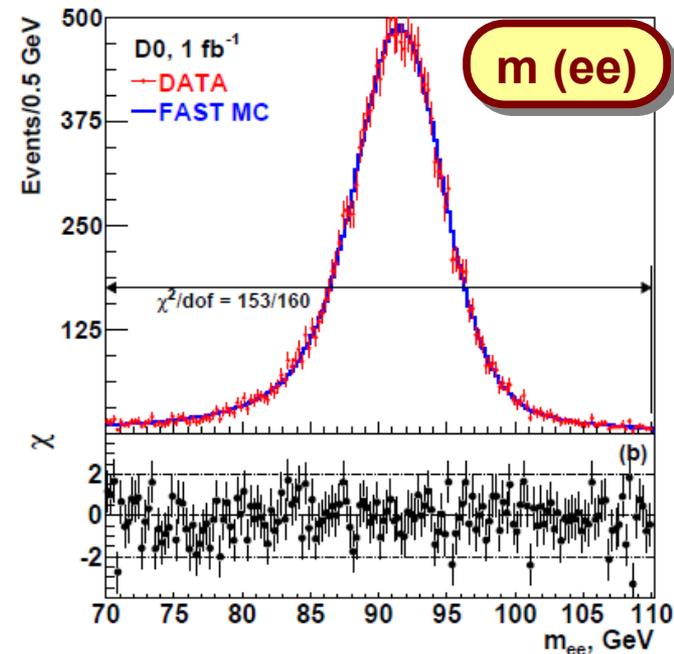
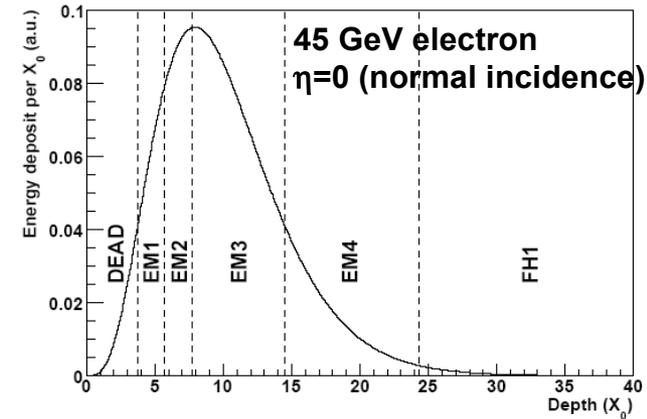
$$E(\text{smear}) = R_{EM}(E) \otimes \sigma_{EM}(E) + \Delta E(\mathcal{L}, u_{\parallel})$$

Energy response: $R_{EM}(E) = \alpha \cdot E + \beta$

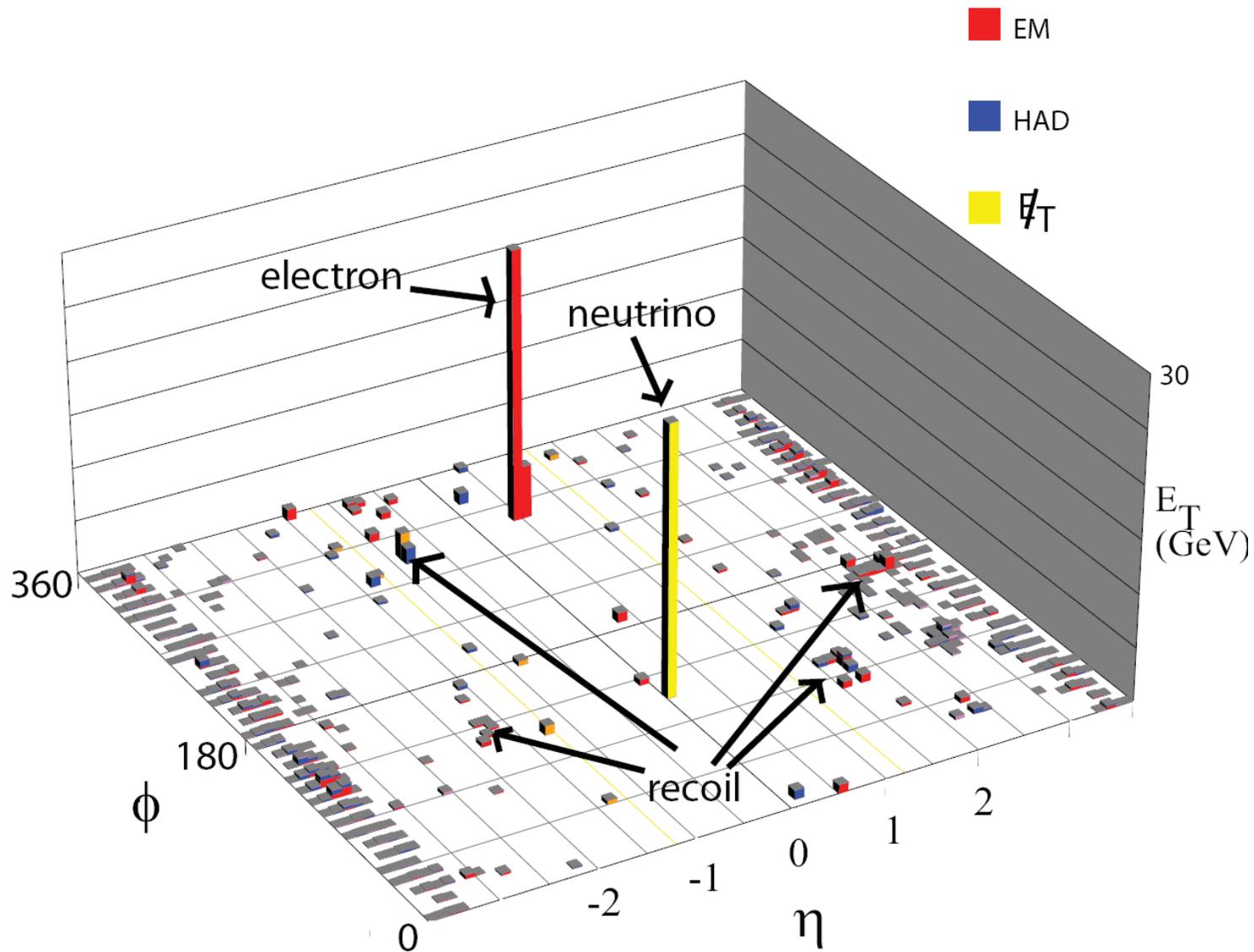
- **dominant source in m_W systematics: 34 MeV**
- **fitted from electron energy spread in $Z \rightarrow ee$ data**

Energy resolution: $\frac{\sigma_{EM}(E)}{E} = \sqrt{C_{EM}^2 + \frac{S_{EM}(E, \theta)^2}{E}}$

- **S_{EM} depends on energy and incidence angle, from improved full GEANT simulation featuring: lower energy cut offs, updated interaction x-sections**
- **$C_{EM} = 2.05\% \pm 0.10\%$; from fit to the m_{ee} distribution from $Z \rightarrow ee$ data**



$W \rightarrow e\nu$ candidate event ($D\emptyset$)



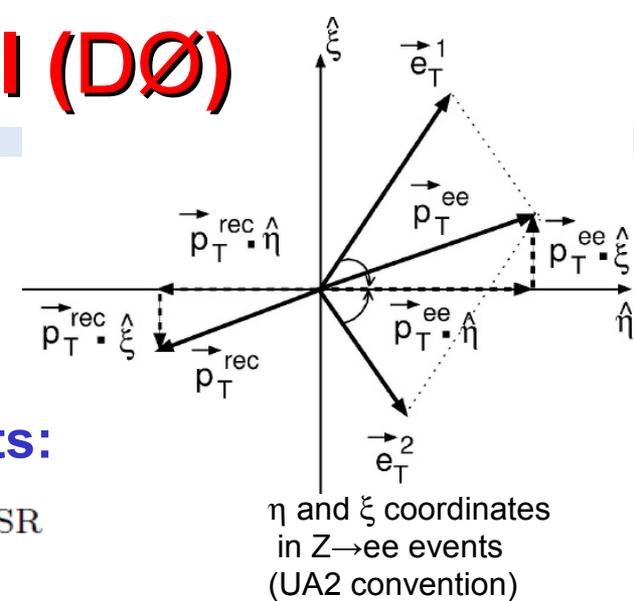
Hadronic recoil model (DØ)

- Neutrino p_T is simulated as:

$$\vec{E}_T = -\vec{p}_T^e - \vec{u}_T$$

- Recoil model has HARD and SOFT components:

$$\vec{u}_T (smear) = \vec{u}_T^{HARD} + \vec{u}_T^{SOFT} + \vec{u}_T^{ELEC} + \vec{u}_T^{FSR}$$

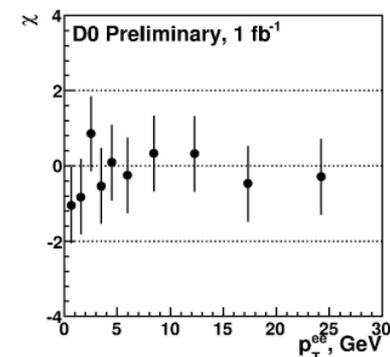
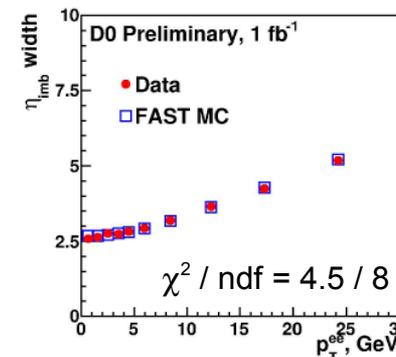
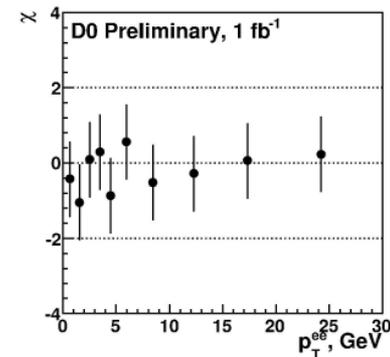
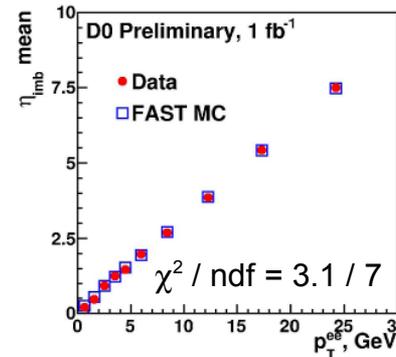


- Model is derived from detailed GEANT simulation ($Z \rightarrow \nu\nu$) and control data samples ($Z \rightarrow ee$, Zero Bias, Minimum Bias)

- Recoil response and resolution are fine-tuned from $Z \rightarrow ee$ data:

- require balancing of u_T and $p_T(ee)$
- mean and width of η_{imb} distribution depend on hadronic recoil response and resolution

- Scalar E_T is also modeled for electron selection efficiencies



Hadronic recoil - details (DØ)

HARD COMPONENT:

- hard component balancing q_T of the vector boson
- from Z→nn full MC
- fine-tuned from Z→ee data

$$\vec{u}_T^{\text{HARD}} = \vec{f}(\vec{q}_T)$$

$$\vec{u}_T^{\text{SOFT}} = -\sqrt{\alpha_{MB}} \cdot \vec{E}_T^{\text{MB}} - \vec{E}_T^{\text{ZB}}$$

$$\vec{u}_T^{\text{ELEC}} = -\sum_e \Delta u_{\parallel} \cdot \hat{p}_T^e$$

- correction for energy leakage outside electron cones
- from W data (azimuthally separated window)

$$\vec{u}_T^{\text{FSR}} = \sum_{\gamma} \vec{p}_T^{\gamma}$$

- FSR photons far away from electron(s) are reconstructed as recoil energy

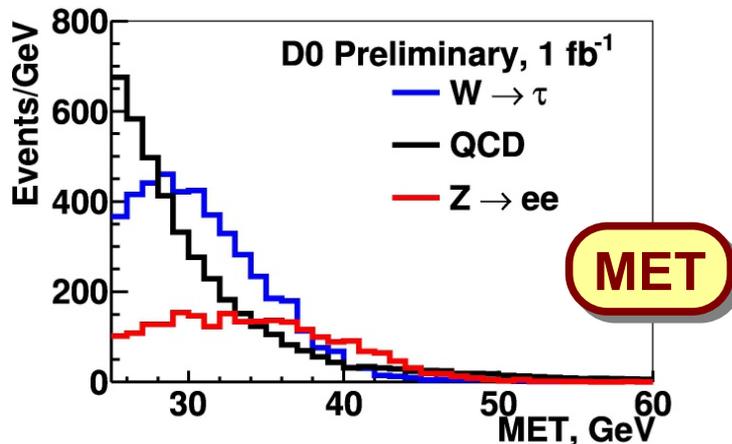
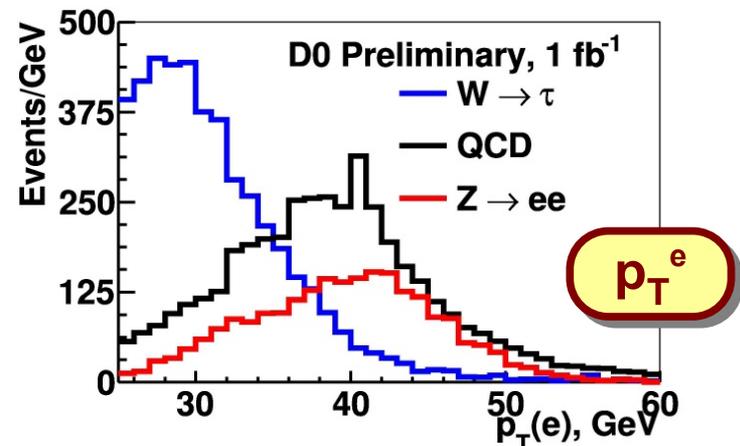
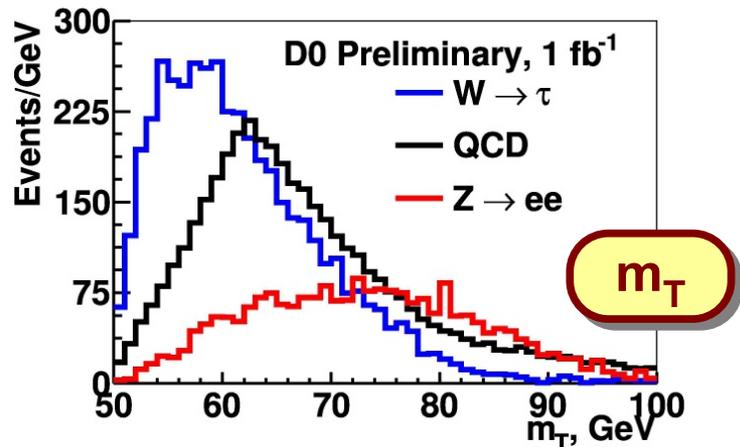
SOFT COMPONENT:

- energy not correlated with the vector boson (additional interactions in same BX, spectator partons, detector noise)
- uses ZB & MB event libraries
- fine-tuned from Z→ee data



Backgrounds (DØ)

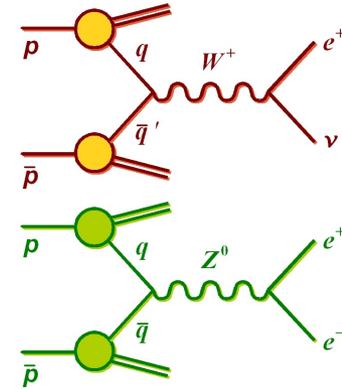
- **Purity of W sample : 96%**
- Backgrounds:
 - **Z → ee** : 0.80% (Data)
 - **QCD multijet** : 1.49% (Data)
 - **W → τν → evνν** : 1.60% (GEANT)
- For 3 observables: estimated backgrounds are added to the simulated signal from W (PMCS)



W production & decay models (DØ)

- Generators for W and Z processes at hadron colliders:

Tool	Process	QCD	EW
RESBOS	W,Z	NLO	-
WGRAD	W	LO	complete $\mathcal{O}(\alpha)$, Matrix Element, ≤ 1 photon
ZGRAD	Z	LO	complete $\mathcal{O}(\alpha)$, Matrix Element, ≤ 1 photon
PHOTOS			QED FSR, ≤ 2 photons



- ResBos+Photos** as main generator

- reasonable $p_T^{W,Z}$ spectra
- leading EWK effects (1st and 2nd FSR photon)

Balazs, Yuan; Phys Rev D56, 5558
Barbiero, Was; Comp Phys Com 79, 291

- WGRAD & ZGRAD** to estimate effects of full EWK corrections

Baur, Wackerroth; Phys. Rev D70, 073015

- Final QED m_W uncertainties are 7,7,9 GeV for m_T, p_T^e, \cancel{E}_T

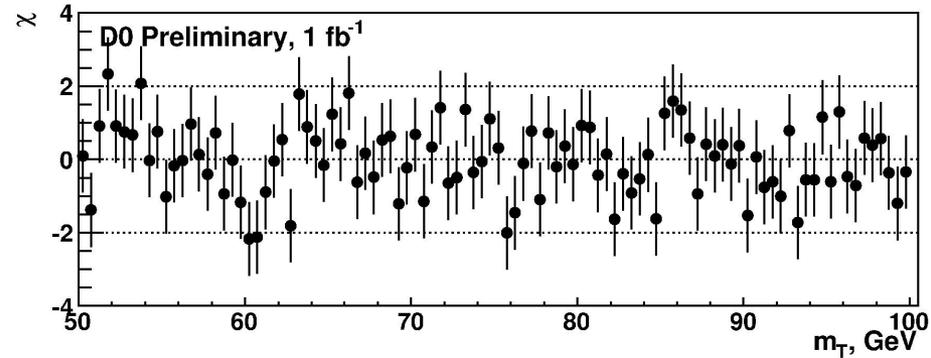
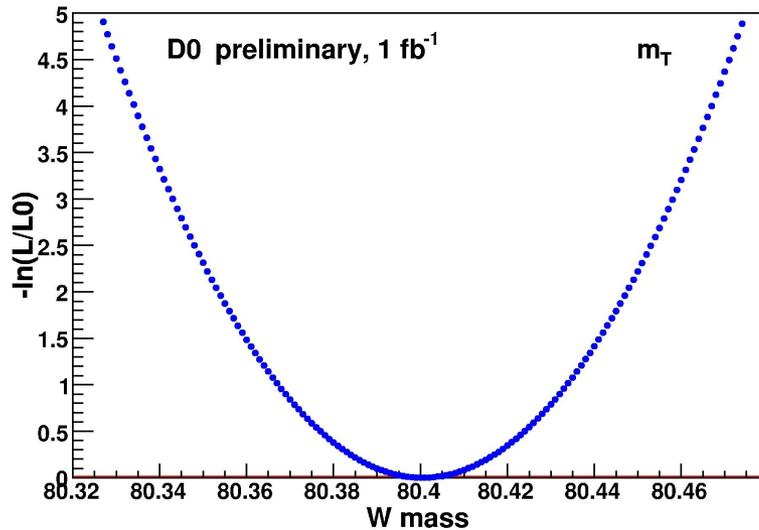
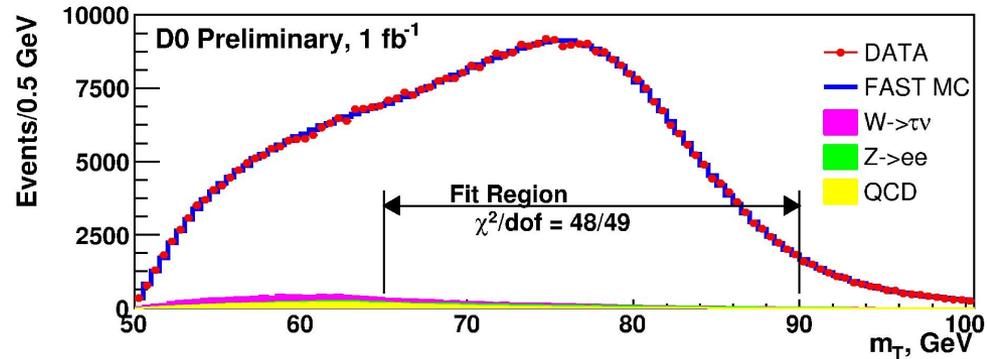
- comparison of “FSR only” and “full EWK” from W/ZGRAD
- comparison of “FSR only” W/ZGRAD and Photos



W mass fits (DØ)

m_T method

- Templates for different m_W hypotheses at 10 MeV intervals: **W signal (PMCS) + background**
- Compute binned likelihood between data and template
- Fit m_W for each of 3 observables



$m_W = 80.401 \pm 0.023 \text{ GeV (stat)}$

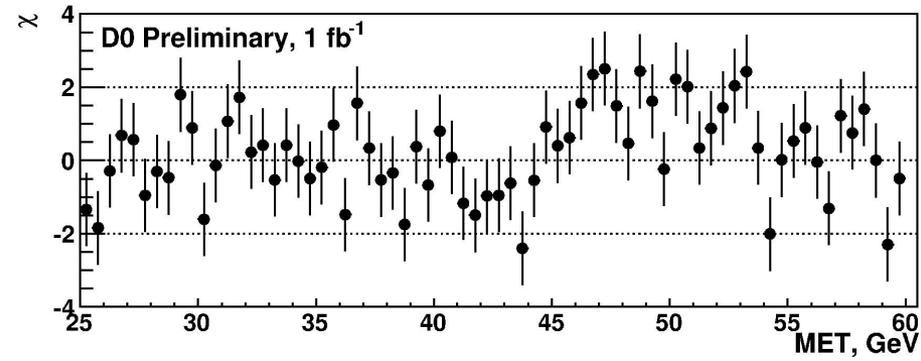
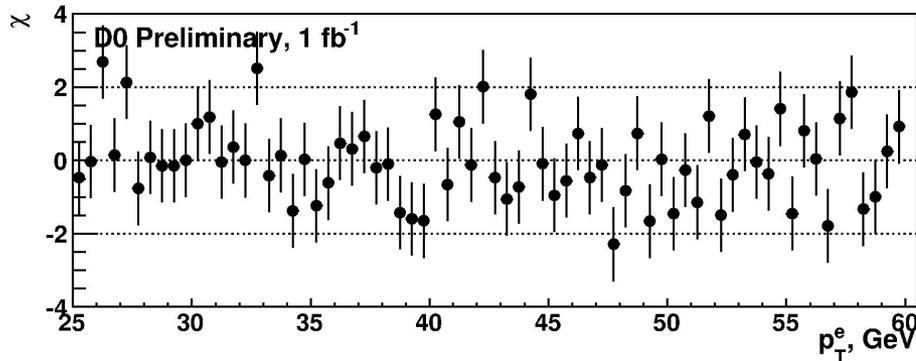
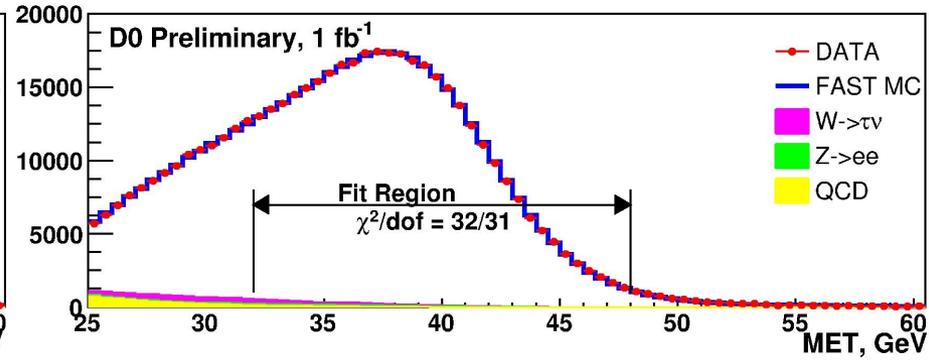
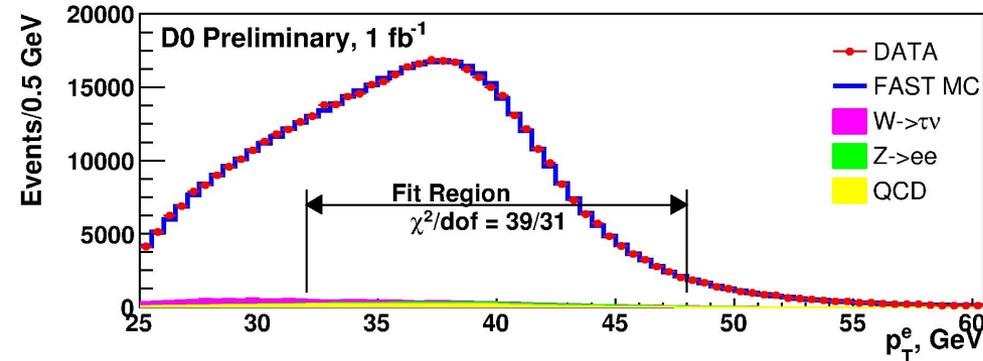
Fit range: $65 < m_T < 90 \text{ GeV}$



W mass fits (DØ)

Electron p_T method

Neutrino p_T method



$$m_W = 80.400 \pm 0.027 \text{ GeV (stat)}$$

$$m_W = 80.402 \pm 0.023 \text{ GeV (stat)}$$

$$\text{Fit range: } 32 < p_T^e < 48 \text{ GeV}$$

$$\text{Fit range: } 32 < \cancel{E}_T < 48 \text{ GeV}$$



Uncertainties (DØ)

		m_W uncertainty [MeV]		
Source		m_T	$p_T(e)$	Missing E_T
EXPERIMENT	Electron energy response	34	34	34
	Electron energy resolution	2	2	3
	Electron energy non-linearity	4	6	7
	Electron energy loss differences for W and Z	4	4	4
	Electron efficiencies	5	6	5
	Recoil model	6	12	20
	Backgrounds	2	5	4
	Subtotal Experimental	35	37	41
THEORY	PDF CTEQ6.1M	10	11	11
	QED	7	7	9
	Boson p_T	2	5	2
	Subtotal Theory (W/Z production & decay)	12	14	14
	Total Systematics	37	40	43
Total Statistics		23	27	23
TOTAL		44	48	50



Combined DØ m_W result

PRL **103**, 141801 (2009)

- **Correlation matrix of the three methods:**

- Partially correlated:

*Statistics, Electron response,
Recoil model, PDF*

- Other sources: 100% correlated

	m_T	$p_T(e)$	MET
m_T	1	0.83	0.82
$p_T(e)$		1	0.68
MET			1

- **DØ Run II combination:**

$$m_W = 80.401 \pm 0.021 \text{ (stat)} \pm 0.038 \text{ (syst)} \text{ GeV}$$

$$\Delta m_W \text{ (total)} = 0.043 \text{ GeV}$$



Combined Tevatron m_W result

- Combination performed with B.L.U.E. method:

CDF Run II (200 pb^{-1})

→ PRL **99**, 151801 (2007)

DØ Run II (1 fb^{-1})

→ PRL **103**, 141801 (2009)

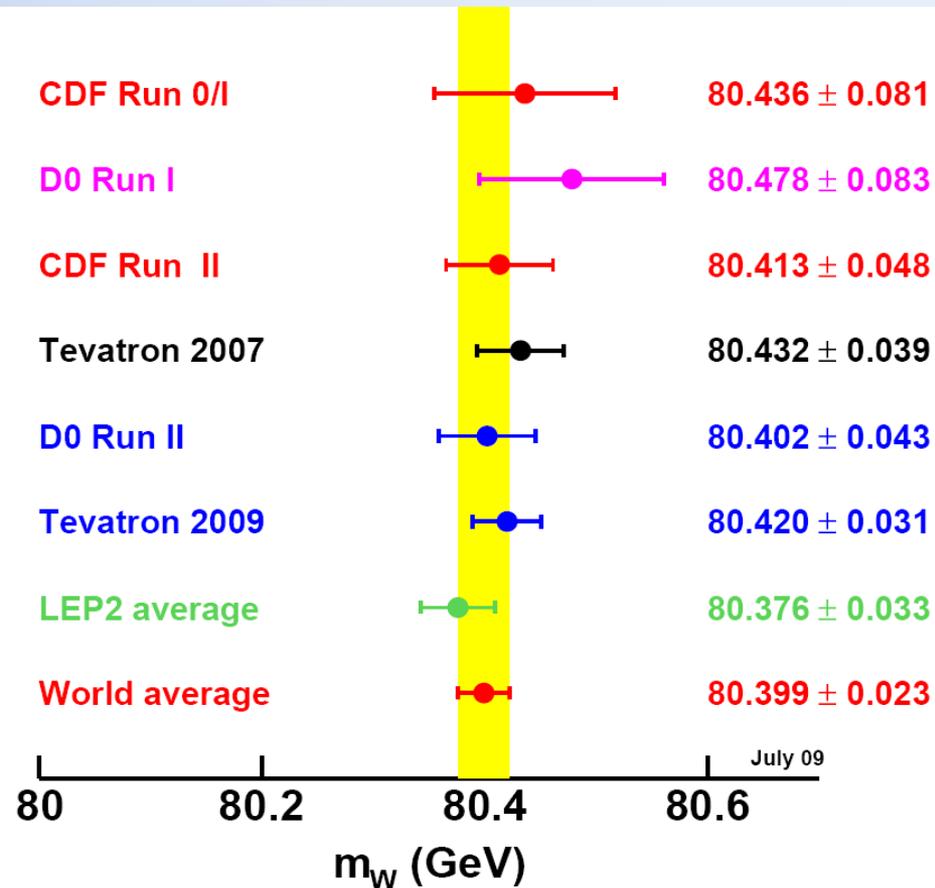
CDF Run 0/I, DØ Run I, LEP2

- For the first time Tevatron average is more precise than LEP2 direct measurement**

arXiv:0908.1374v1 [hep-ex]

Tevatron 2009: $m_W = 80.420 \pm 0.031 \text{ GeV}$

World average: $m_W = 80.399 \pm 0.023 \text{ GeV}$



Improved by:

20 %

8 %



Combined Tevatron Γ_W result

- Combination performed with B.L.U.E. method:

CDF Run II (350 pb⁻¹)

→ PRL **100**, 071801 (2008)

DØ Run II (1 fb⁻¹)

→ PRL **103**, 231802 (2009)

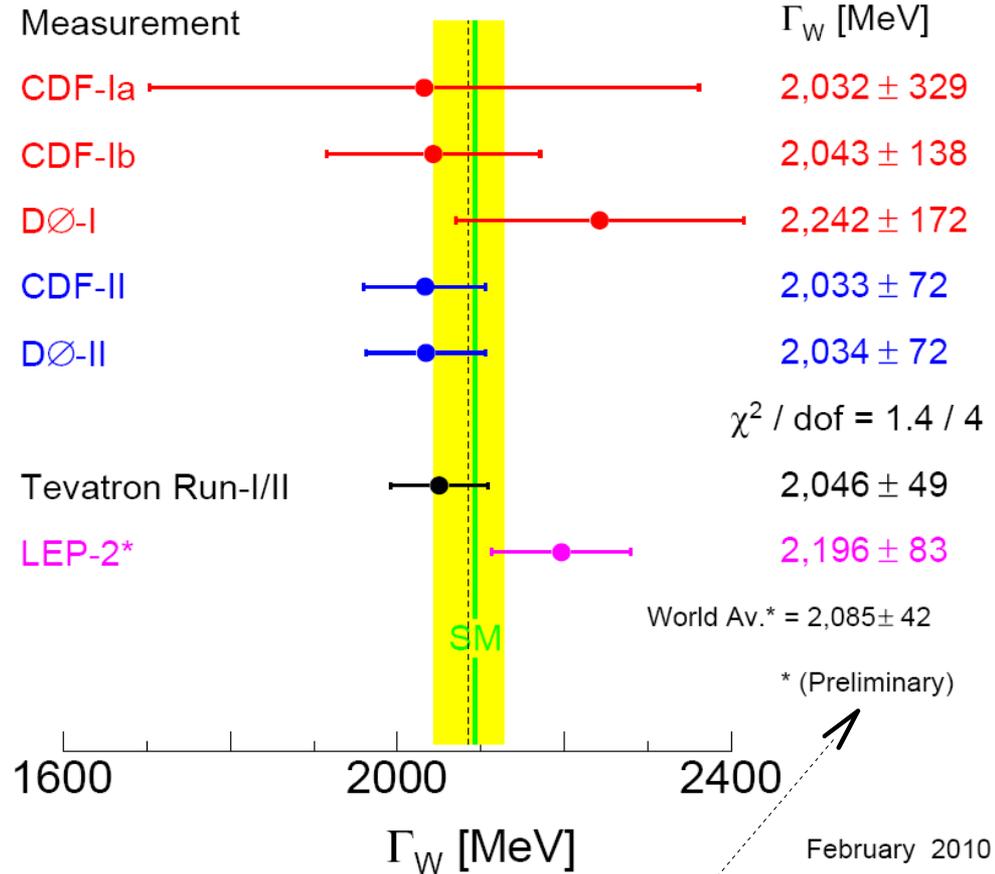
CDF Run I, D0 Run I, LEP2

- New world average agrees with SM prediction of $\Gamma_W = 2.093 \pm 0.002$ GeV**

arXiv:1003.2826v1 [hep-ex]

Tevatron 2009: $\Gamma_W = 2.046 \pm 0.049$ GeV

World average: $\Gamma_W = 2.085 \pm 0.042$ GeV



For consistency the published Γ_W values have been corrected for the world averaged m_W value from Dec 2009

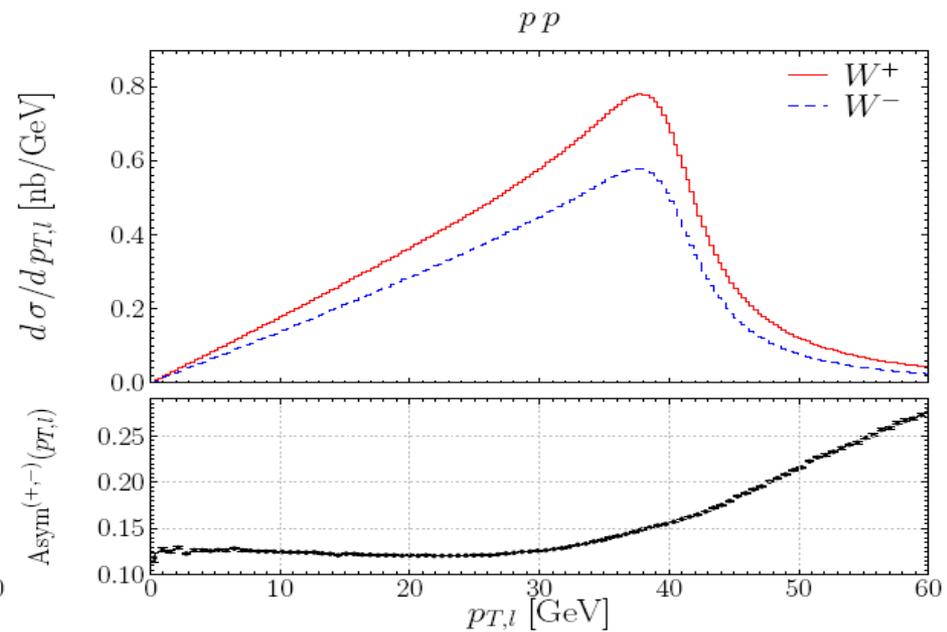
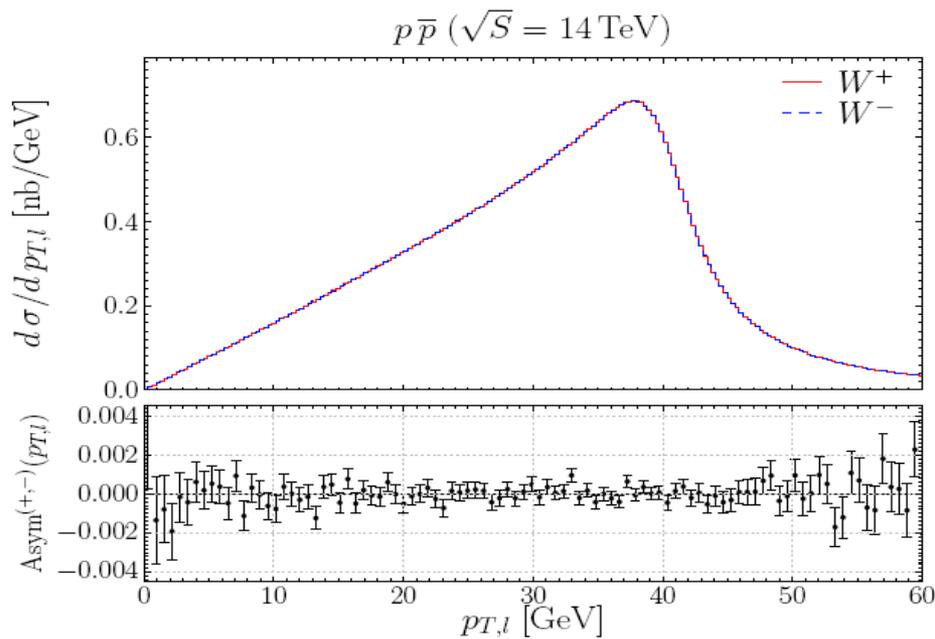


M_W prospects for Tevatron

- **Expected total (stat) uncertainty:**
 - **CDF (2.3 fb^{-1}) : 25 (15) MeV** per channel
 - **DØ (4.4 fb^{-1}) : 25 (11) MeV**
- **Systematics:**
 - Some experimental sources will be reduced after collecting more data (DØ: larger Z sample \Rightarrow electron energy scale 34 \rightarrow 16 MeV)
 - Different techniques used by CDF & DØ for lepton energy scale are good for combination and cross checks
 - Theory errors are 100% – correlated between CDF and DØ
 - Controlling systematics at ~ 10 MeV level requires:
 - including higher order QED radiation
 - better constrained PDFs



M_W prospects for LHC



- **In p-p collisions:**

- Loss of charge symmetry $W^+ \leftrightarrow W^-$
- Stronger dependencies from PDFs
- Need to measure: m_{W^+} & m_{W^-} or: $(m_{W^+} - m_{W^-})$ & $(m_{W^+} + m_{W^-})$

- **Ultimately expect <10 MeV precision from the LHC era**

F.Fayette talk at EPS 2009



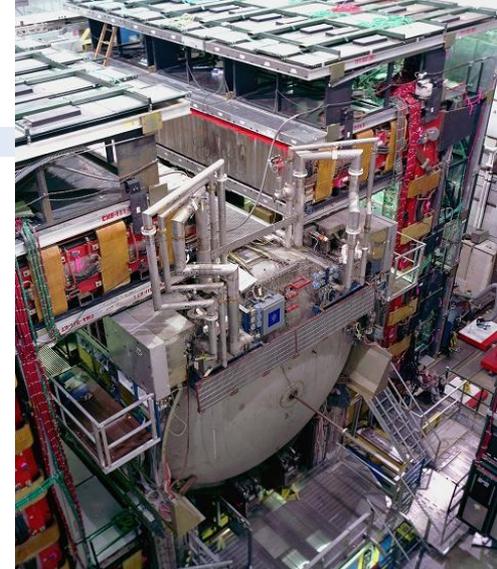
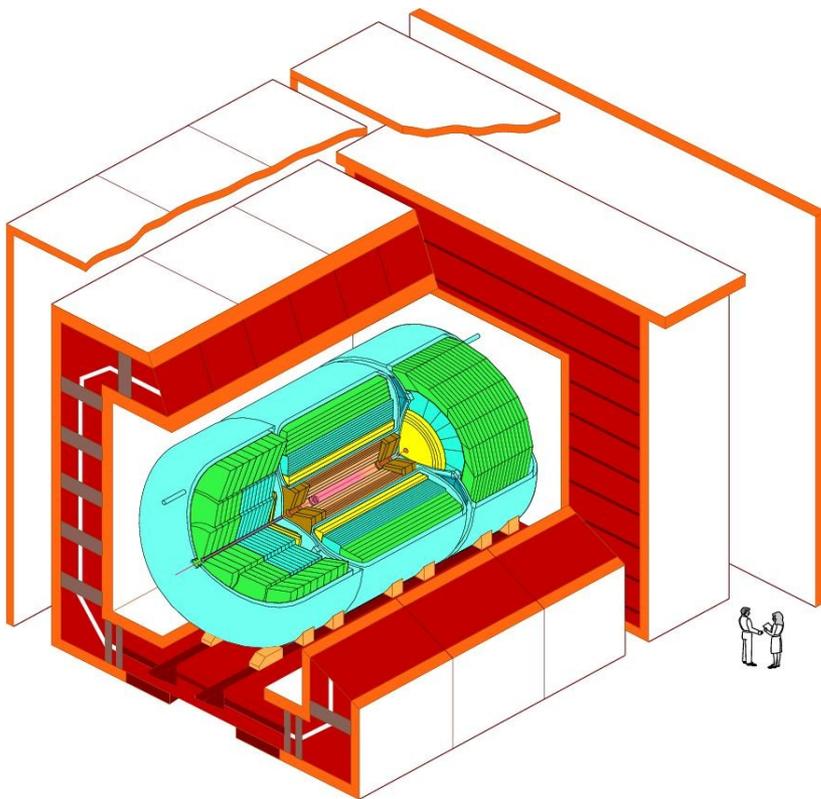
BACKUP Slides



DØ detector

- **Tracker:**

- silicon microstrips + scintillating fibers
- covers $|\eta| < 2.5$ inside 2T superconducting solenoid



- **Calorimeter:**

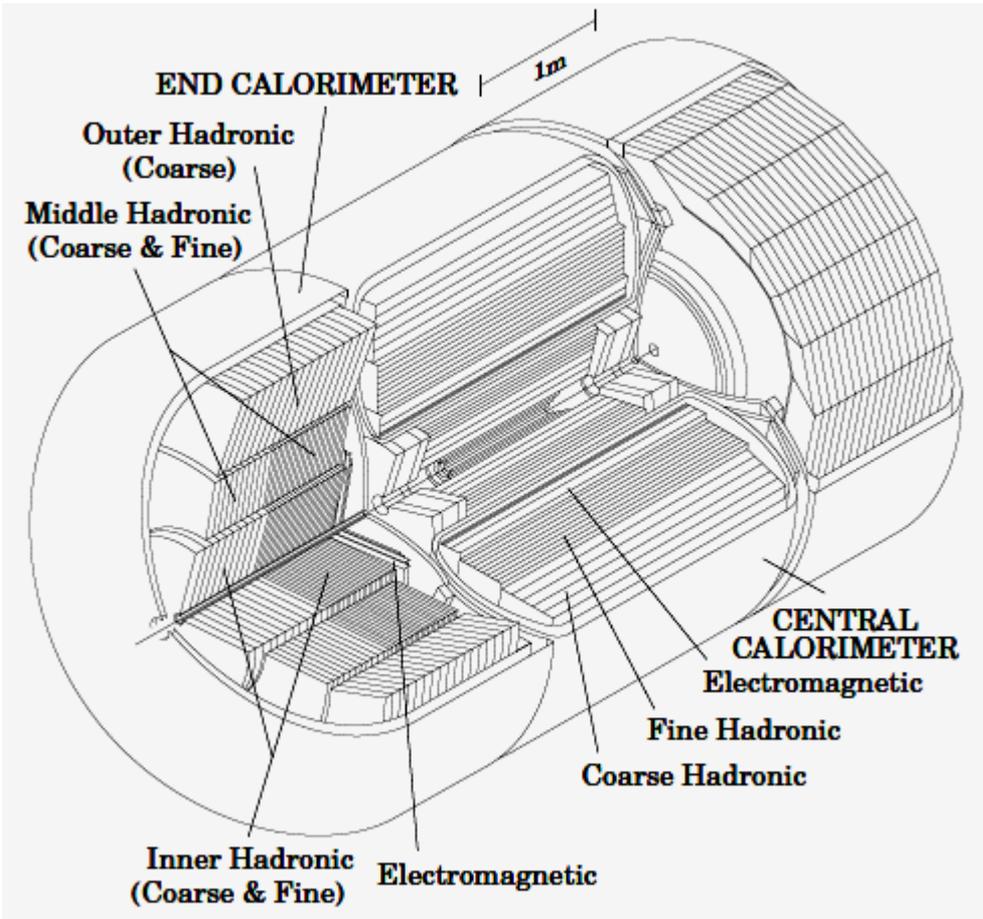
- sampling U/LAr
- hermetic coverage: $|\eta| < 4.2$

- **Muon system:**

- wire chambers + scintillators
- covers $|\eta| < 2$ before and after 1.8T toroid

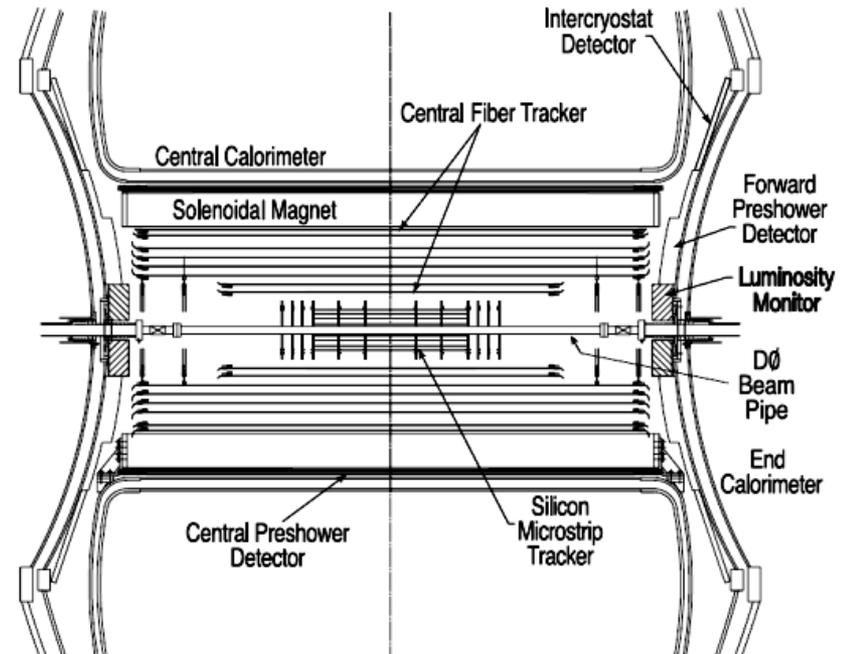


DØ LAr calorimeter



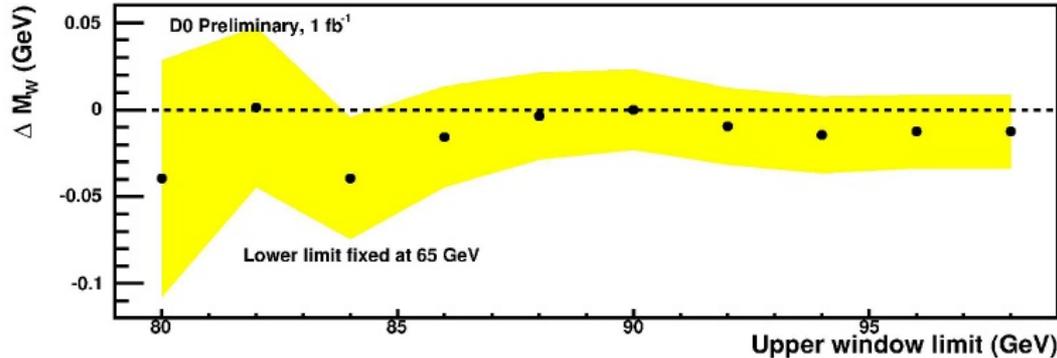
- 46,000 cells
- Segmentation (towers): $\Delta \eta \times \Delta \phi = 0.1 \times 0.1$
(0.05 x 0.05 in third EM layer,
near shower maximum)

- Active medium: Liquid argon
- Absorber: Uranium (mostly)
- 3 cryostats: Central CAL (CC) and two End CALs (EC)
- Hermetic with full coverage: $|\eta| < 4.2$
- In Run II there is more uninstrumented material in front of the CAL than in Run I



Consistency checks (DØ)

- Vary fitting ranges for all 3 observables



e.g. upper m_T limit
(yellow = stat. uncert.)

- Split W & Z data samples into statistically independent **categories** or **vary the cuts** and compare relative change in m_Z/m_W ratio:
 - Different electron η ranges
 - Different EM calorimeter ϕ fiducial cuts
 - High and low instantaneous luminosity
 - Different data taking periods
 - High and low scalar E_T
 - Different recoil u_T cuts
 - Negative and positive $u_{||}$

**Result is stable within
one standard deviation !**

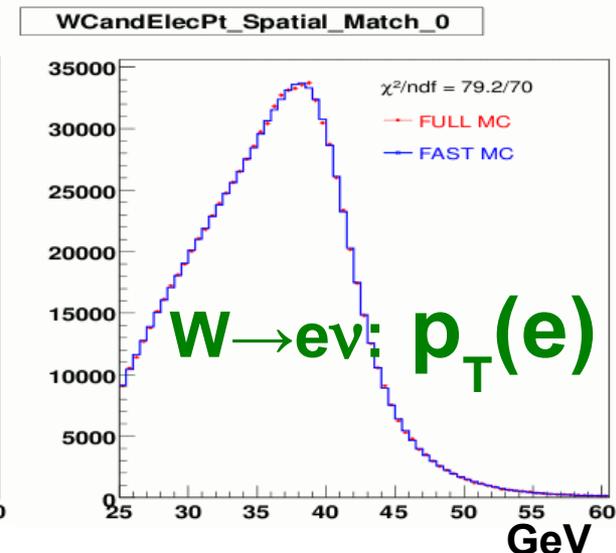
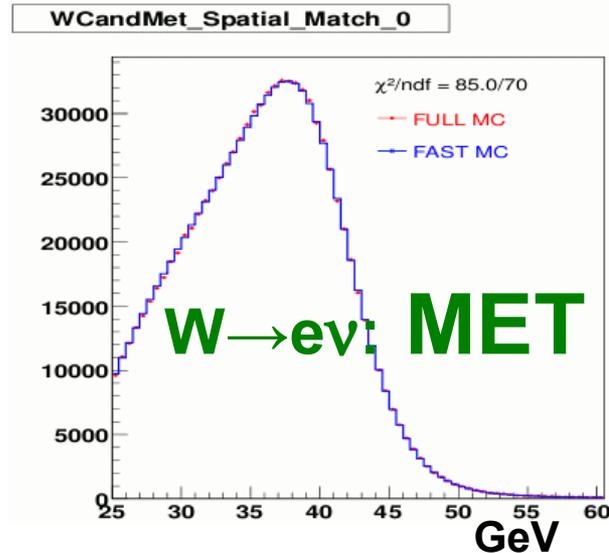
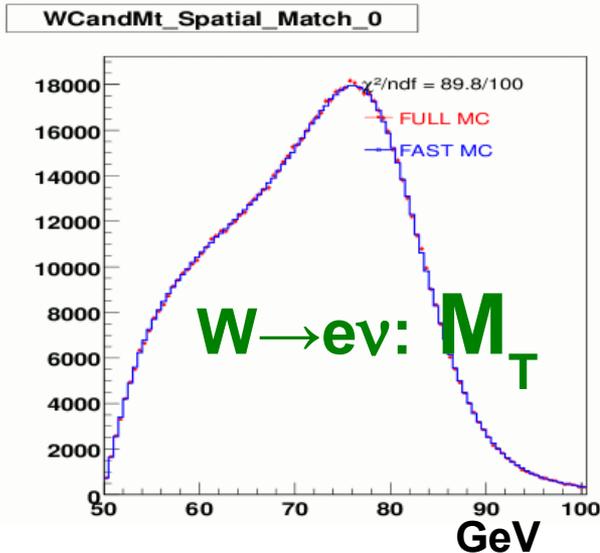
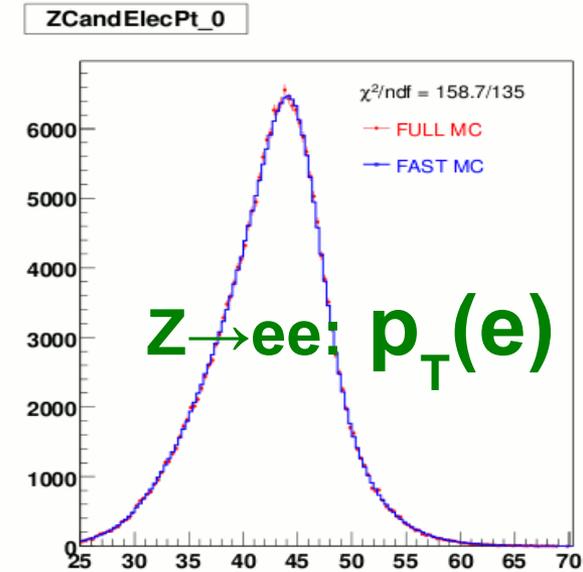
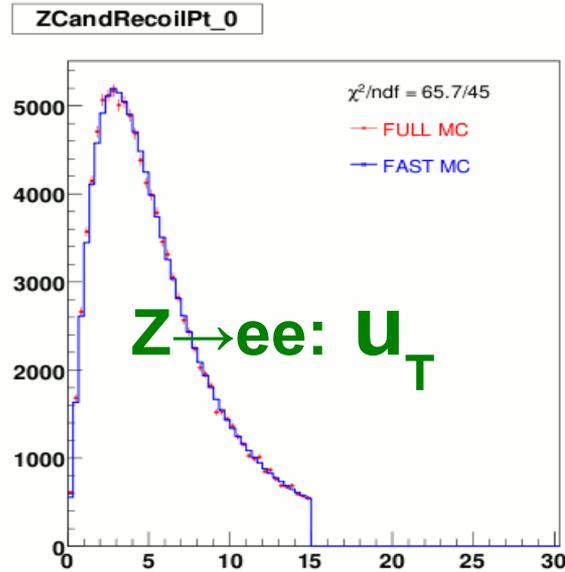


MC closure test (DØ)

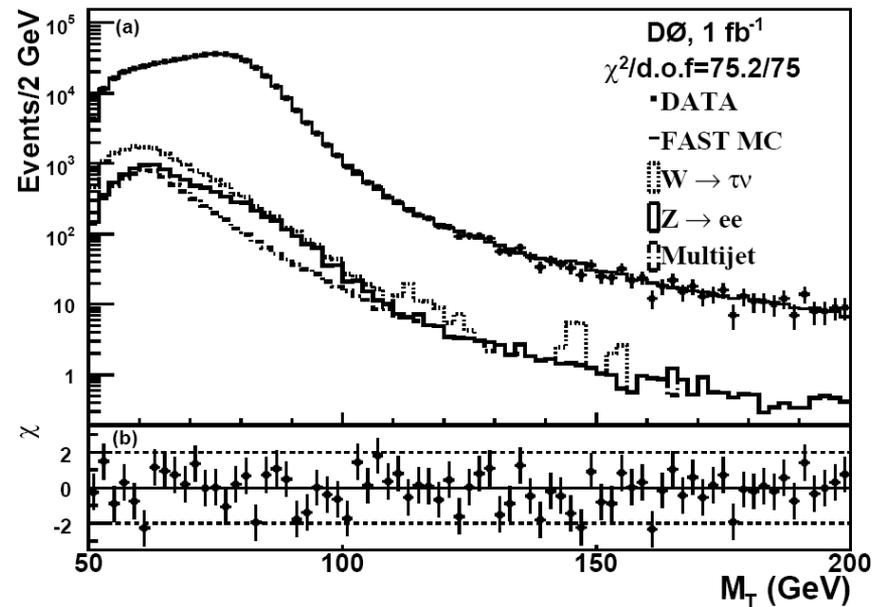
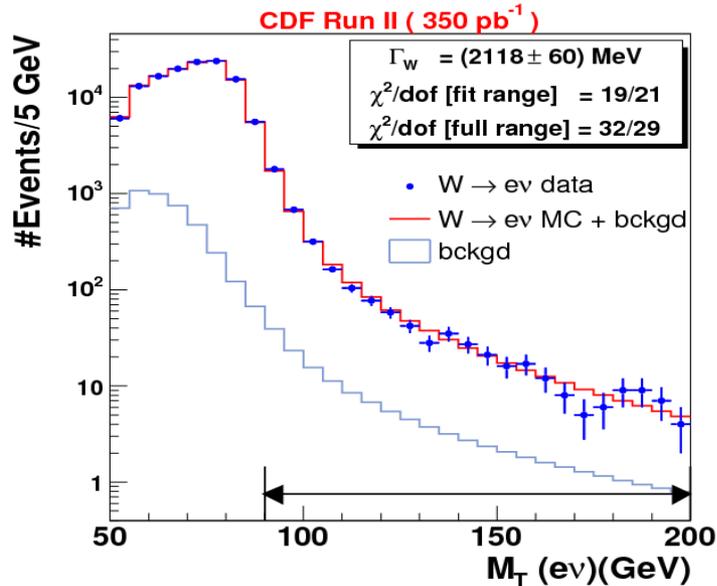
Test analysis methodology with Full GEANT MC treated as the collider data

Good agreement between Full MC and Fast MC (PMCS)

Fitted W mass and width agree with input values



Tevatron Γ_W analyses



- Use high-end tail of the transverse mass peak

- CDF Run II (350 pb⁻¹) : $\Gamma_W = 2.033 \pm 0.072 \text{ GeV}$
- DØ Run II (1 fb⁻¹) : $\Gamma_W = 2.034 \pm 0.072 \text{ GeV}$
- using world average of $m_W = 80.399 \pm 0.023 \text{ GeV}$ from Dec 2009

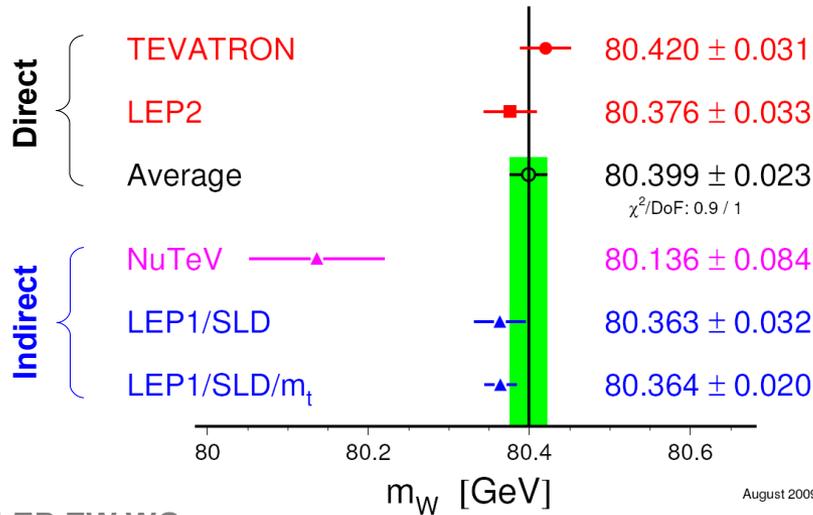
- Combined Tevatron Run I/II result: $\Gamma_W = 2.046 \pm 0.049 \text{ GeV}$

- surpassed average LEP2 direct measurements ($\delta\Gamma_W = 83 \text{ MeV}$)
- far less precise than EWK fit using Z-pole data + m_{top} measurement ($\delta\Gamma_W = 2 \text{ MeV}$)



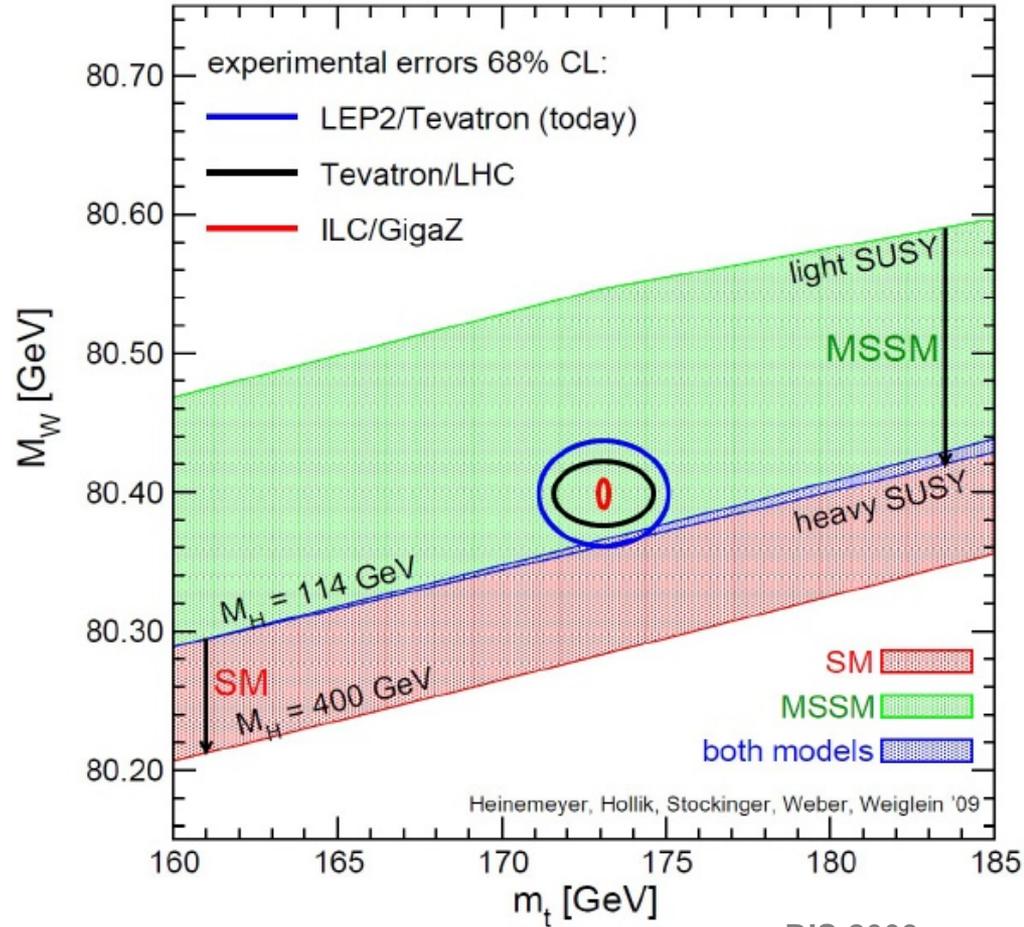
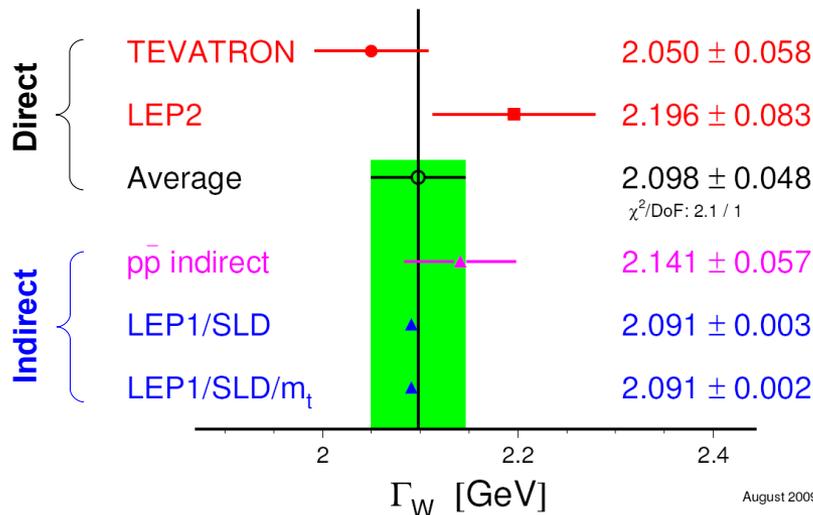
M_W & Γ_W – today and future

W-Boson Mass [GeV]



LEP EW WG
Aug 2009

W-Boson Width [GeV]



DIS 2009
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