

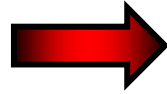
# **FCNC Processes** **waiting for** **the Next Decade**

*Andrzej J. Buras*  
*(Technical University Munich, TUM-IAS)*

**Warsaw, Nov 6th, 2009**

# Overture

**Frontiers of  
Elementary Particle  
Physics**



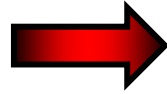
**Search for Physics Laws  
at very short distance scales**

**Heisenberg  
Principle**

•

**To test  $10^{-18}$  m  
we need  $E \cong 200$  GeV**

**Frontiers of  
Elementary Particle  
Physics**



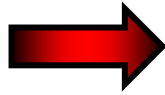
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•

**To test  $10^{-18}$  m  
we need  $E \cong 200$  GeV**

**LHC  
 $E \approx 4$  TeV**



**Tests at  
 $5 \cdot 10^{-20}$  m  
possible**

**Frontiers of  
Elementary Particle  
Physics**



**Search for Physics Laws  
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**Unlikely that we can do better  
before 2046 through high  
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Physics**

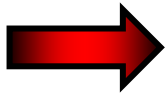


**Search for Physics Laws  
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**LHC  
 $E \approx 4$  TeV**



**Tests at  
 $5 \cdot 10^{-20}$  m  
possible**

**Unlikely that we can do better  
before 2046 through high  
energy collider experiments.**

**Flavour Physics  
governed by  
Quantum Fluctuations  
is sensitive to  
 $E \approx 200$  TeV  
and even higher  
energy scales**



**Tests at  
 $10^{-21}$  m  
and shorter  
scales  
possible**



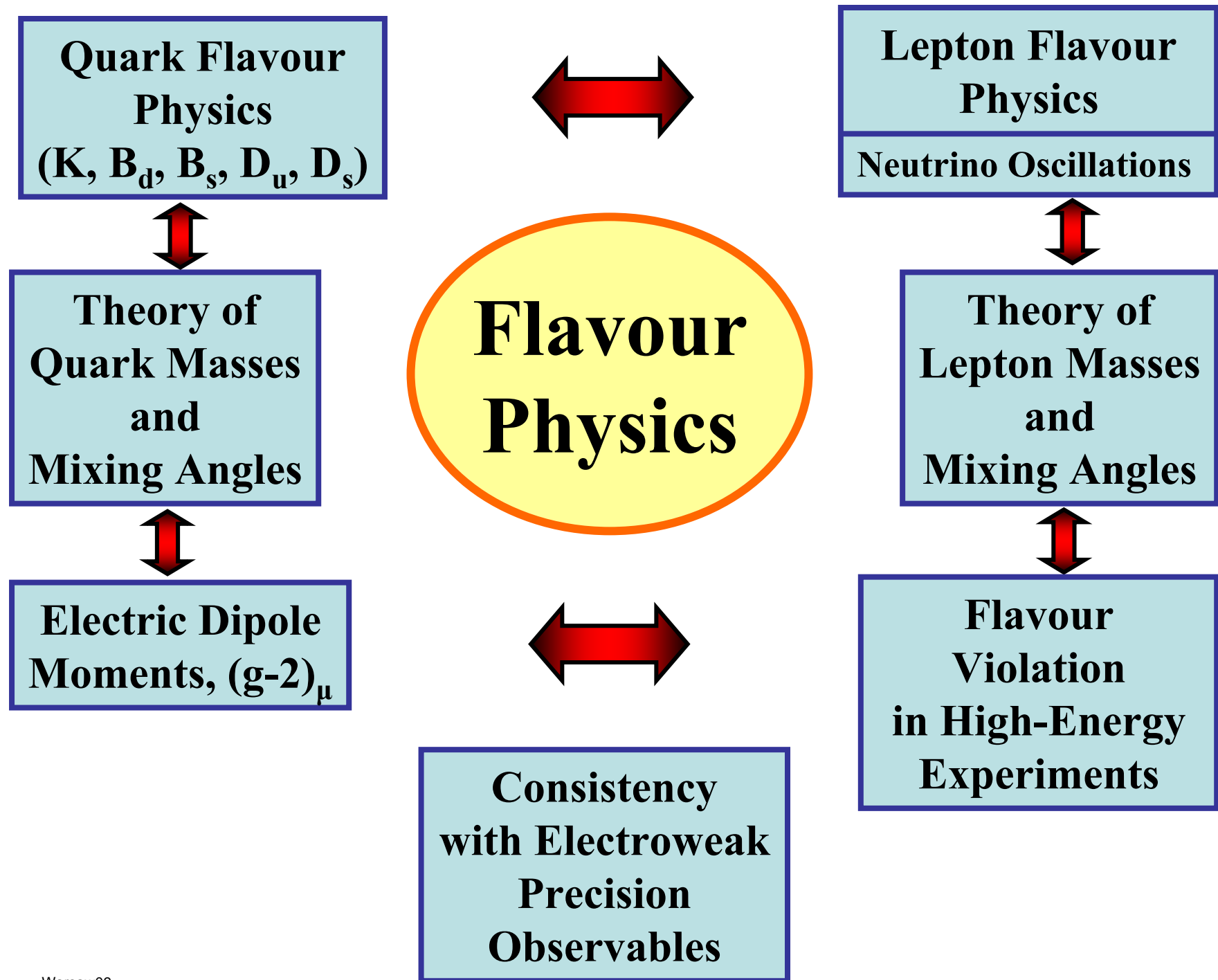
**Frontiers in testing  
very very short  
distance scales  
belong to  
Flavour Physics**

**but**

**Very high precision  
required !!**

## **Main Message of this Talk**

**In our search for a more  
fundamental theory we need  
to improve our understanding  
of **Flavour Physics****





(GIM)

## Impressive Success of the CKM Picture of Flavour Changing Interactions

Yet

- 1.** Several tensions between the flavour data and the SM exist.
- 2.** Hierarchies in Fermion Masses and Mixing Angles have to be understood with the help of some New Physics (NP).
- 3.** There is still a lot of room for NP contributions, in particular in rare decays of mesons and leptons, in  $\mathcal{CP}$  flavour violating transitions and EDM's.

Are **1.** - **3.** somehow related ?

Will we see any footprints of this NP in the 2010's ?

# Strategy for the Next 50 Min

- 1. Theoretical Framework (~ 15 min)**
- 2. 20 Goals in Flavour Physics for the Next Decade (~ 8 min)**
- 3. Waiting for Signals of New Physics in FCNC Processes (~ 25 min)**
- 4. Final Messages (~ 2 min)**

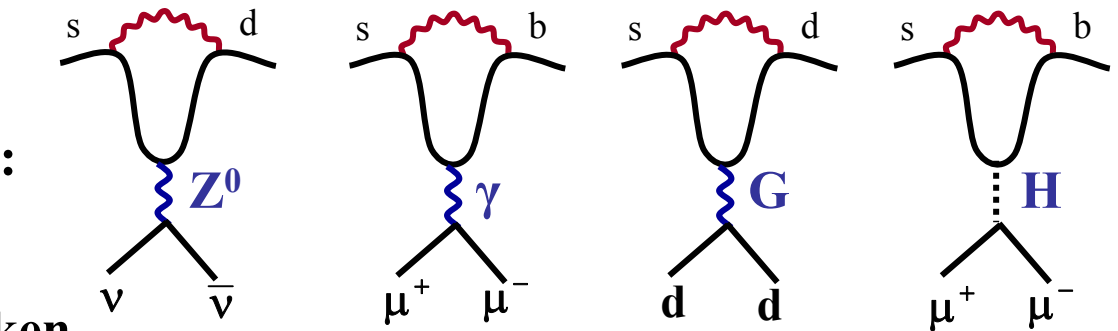
(hep-ph/0910.1032): "Flavour Theory : 2009"

**1.**

# **Theoretical Framework**

# Basic Diagrams in FCNC Processes

**Penguin Family**

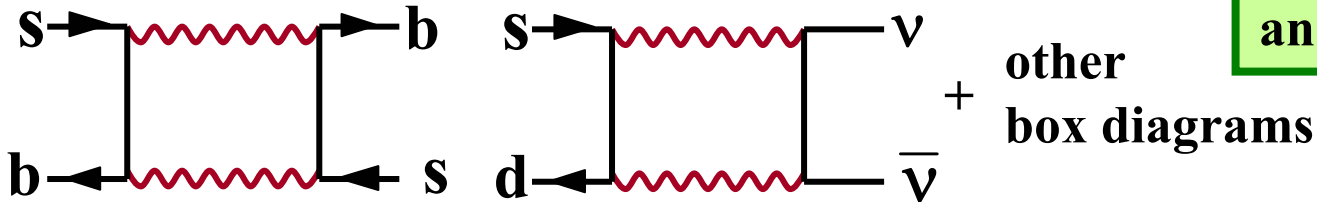


**New Physics enters here**

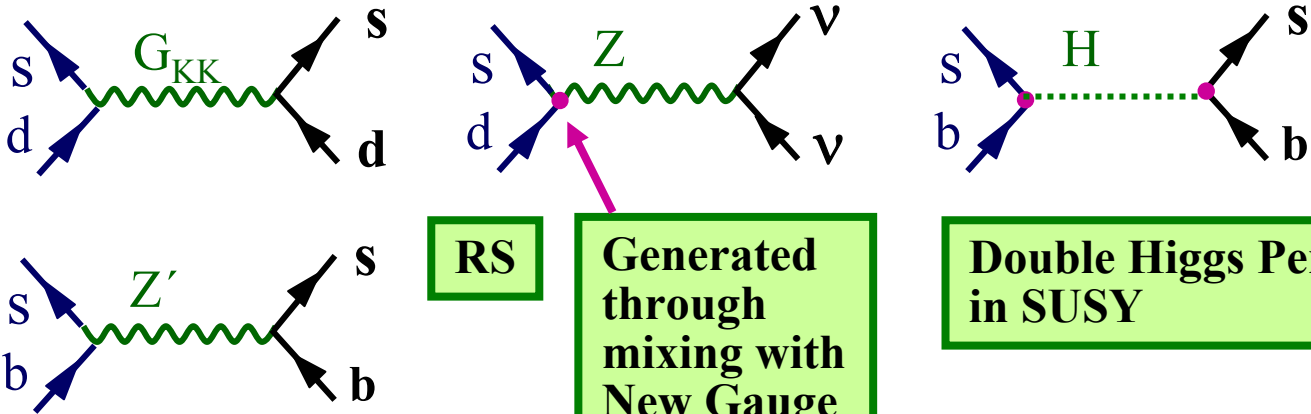
**Similar diagrams in LFV and EDM's**

**(GIM broken at one loop)**

**Box Diagrams**



**Tree Diagrams**

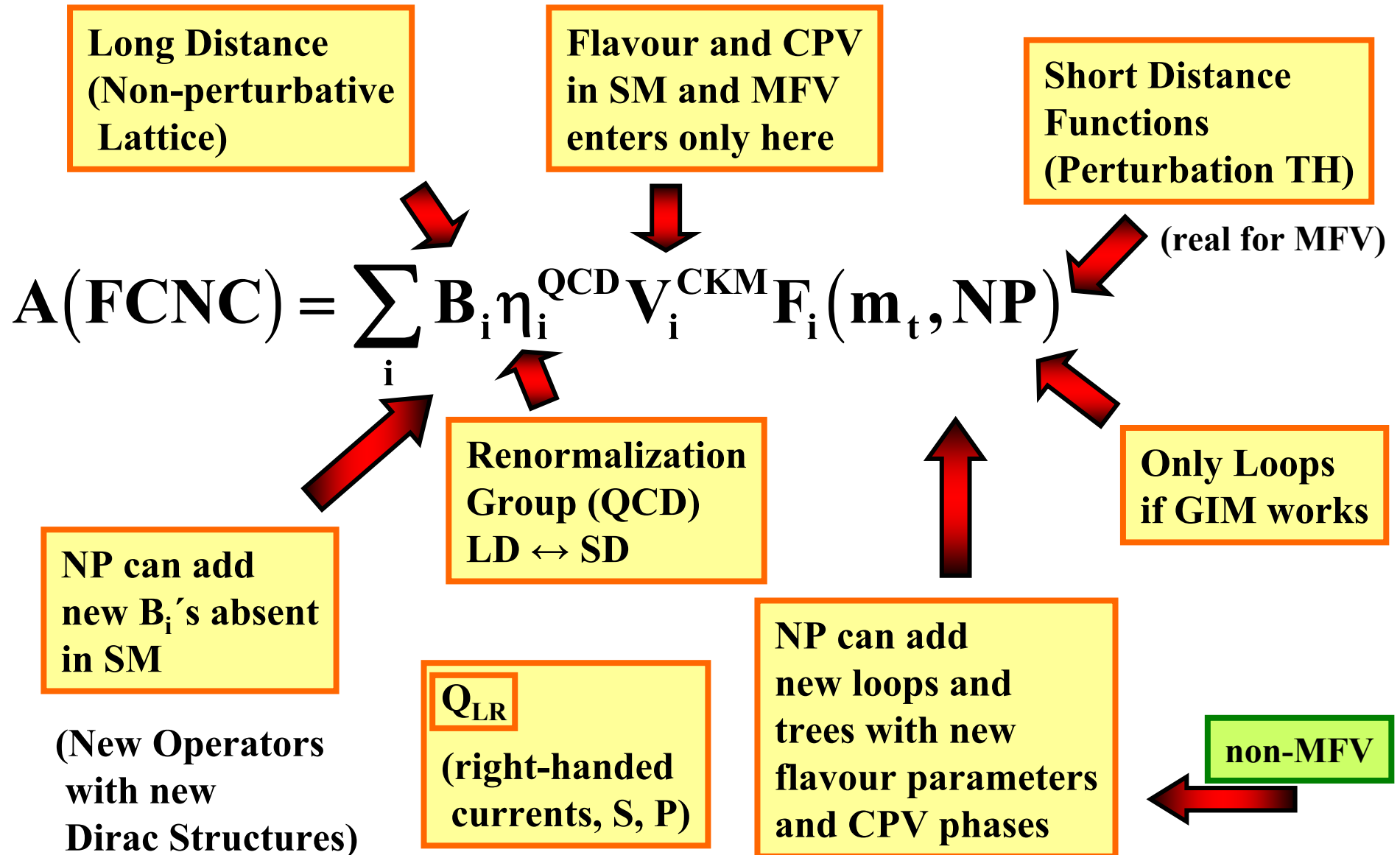


**(GIM broken at tree level)**

**RS**  
**Generated through mixing with New Gauge Bosons**

**Double Higgs Penguin in SUSY**

# Master Formula for FCNC Amplitudes



# Most popular BSM Directions

**CMFV**

(constrained MFV)

**MFV**

(NMFV)  
(GMFV)

**LHT**

(Littlest Higgs  
with T-parity)

**SUSY**

(flavour models)

**Z'**

(Langacker...)

**RS**

(Randall-Sundrum)  
(Warped Extra Dimensions)

**4th G**

(Hou..., Soni..., Lenz..., Melic)

**Vector-Like  
Quarks**

(Branco...,  
del Aguila)

**Non-Decoupling**

**New gauge bosons, fermions, scalars in loops  
and even trees with often non-CKM interactions.**

**Little Hierarchy Problem**

**Electroweak Precision Tests**

+

**Agreement of the CKM Picture of Flavour and CP Violation with existing Data (FCNC)**

**$\Lambda_{\text{NP}} \approx 1000 \text{ TeV}$**

(generic)

(generic)

**$\Lambda_{\text{NP}} \approx 5 \text{ TeV}$**

**Very strong Constraints on Physics beyond SM with scales  $O(1 \text{ TeV})$**

**Necessary to solve the hierarchy problem**

**$(M_{\text{PLANCK}} \gg \Lambda_{\text{EW}})$**

**Message 1** : **New Physics at TeV-Scale must have a non-Generic Flavour Structure**

**Message 2** : **Protection Mechanisms to suppress FCNCs generated by TeV-Scale New Physics required**

Ciuchini et al  
Isidori et al  
Agashe et al  
+50



**MFV**

**GIM**

**RS-GIM**

**T-Parity**

**R-Parity**

**Alignment**

**Degeneracy**

**Flavour Symmetries**

(abelian, non-abelian)

**Custodial Symmetries**

(continuous, discrete)



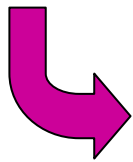
# Minimal Flavour Violation (MFV)

**MFV**

SM Yukawa Couplings are the only breaking sources of the  $SU(3)^5$  flavour symmetry of the low-energy effective theory

$(Y_t, Y_b)$

D'Ambrosio, Giudice, Isidori, Strumia (02) Chivukula, Georgi (87)



CKM the only source of Flavour Violation but for  $Y_t \approx Y_b$  new operators could enter

$\mathcal{CP}$   
SM-like

**CMFV**

Operator structure of SM remains



**VERY STRONG RELATIONS BETWEEN K and B Physics and generally  $\Delta F=2$  and  $\Delta F=1$  FCNC Processes**

AJB, Gambino, Gorbahn, Jäger, Silvestrini (00)  
Ali, London

**Related Studies** : Ratz et al (08)  
Smith et al (08)  
Zupan et al (09)

Spurion Technology

Nir et al.  
AGIS  
Feldmann, Mannel

also beyond  
MFV



# Dominant New Flavour and CP Violating Interactions at $0(\mu_{NP})$

**SUSY:**

**GIM**

- a) Misalignment of quark- and squark mass matrices, similarly for lepton sector
- b) Effects enhanced at large  $\tan\beta$  :  $\delta_{ij}^{AB}$

Typical scales(200-1000 GeV)

**LHT:**

New flavour and CP violating mixing matrices in the interactions of SM fermions with mirror fermions mediated by  $W_H, Z_H, A_H$

Typical scales (500-1000 GeV)

**RS:**

New Heavy Gauge Bosons (KK)  
New Heavy Vector-like Fermions (KK)

Tree Level FCNC's mediated by  
KK Gluon ( $\Delta F=2$ ) and Z( $\Delta F=1$ )  
(Typical scales  $M_{KK} \approx 2-3$  TeV)

Related to the explanation of hierarchies in masses and mixings

**RS-GIM**

# Battle in the Bulk to save RS with $M_{KK} \sim 2-3 \text{ TeV}$

## “Warped Flavour”

Some  
fine tuning  
required

### Custodial Symmetries, Flavour Symmetries, etc.

Blanke et al

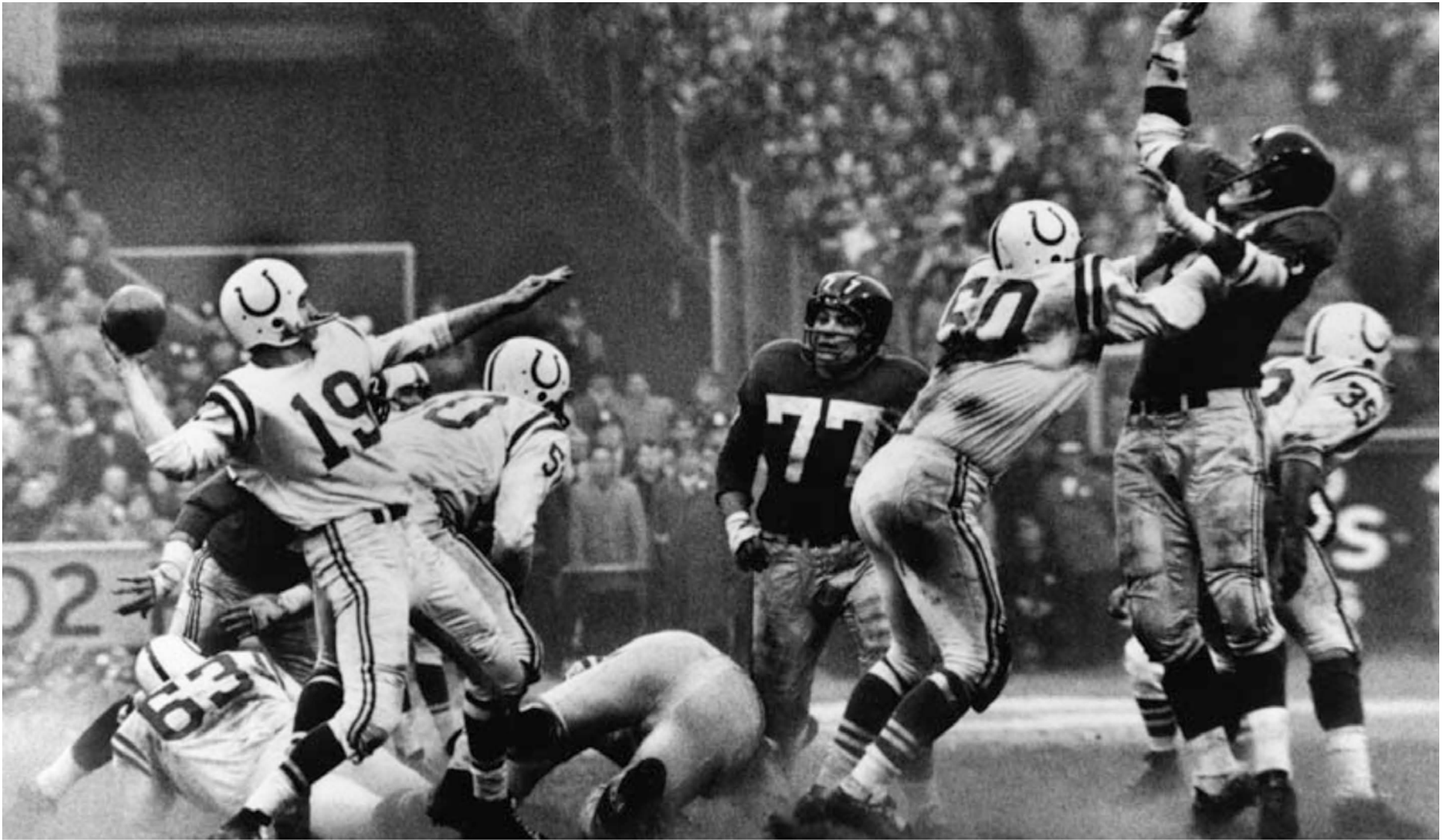
(some related to EWPT, some related to FCNC's)

Ghergetta, Pomarol; Huber, Shafi (03)  
Agashe, Delgado, May, Sundrum (03)  
Csaki, Grojean, Pilo, Terning (03)  
Agashe, Contino, Da Rold, Pomarol (06)  
Agashe, Perez, Soni (06)  
Cacciapaglia, Csaki, Weiler et al. (07)  
Csaki, Falkowski, Weiler (08) ←  
Fitzpatrick, Perez, Randall (07)  
Santiago (08)  
Casagrande, Goertz, Haisch, Neubert (08)  
Blanke, AJB, Duling, Gori, Weiler (08) ←  
Albrecht, Blanke, AJB, Duling, Gemmler (09)  
AJB, Duling, Gori (09)  
Csaki, Grossman, Perez, Surujon, Weiler (09)

Agashe, Azatov, Zhu (08)  
Azatov, Toharia, Zhu (09)  
Agashe, Contino (09)  
Gedalia, Isidori, Perez (09)  
Csaki, Curtin (09)

$Q_{LR}$  and dipole operators  
most problematic

$\epsilon_K, B \rightarrow X_s \gamma, \mu \rightarrow e \gamma, d_n$   
 $\epsilon'/\epsilon$



Quark flavor in RS:  
Overtime

**Ulrich Haisch**

# 2 x 2 Flavour Matrix of Basic NP Scenarios

(AJB, hep-ph/0101336, Erice)

	SM Operators	+ Additional Operators
CKM	<p><b>A</b></p> <p><b>CMFV</b> (<math>Y_t</math>)</p> <p>SM, 2 HDM at low <math>\tan\beta</math> LH without T-parity Universal flat ED</p>	<p><b>B</b></p> <p><b>MFV</b> (<math>Y_t, Y_b</math>)</p> <p>MSSM with MFV 2 HDM at large <math>\tan\beta</math></p>
New Flavour (CP) Violating Interactions	<p><b>C</b></p> <p><b>beyond CMFV</b></p> <p>LH with T-parity Some <math>Z'</math>-models 4<sup>th</sup> generation</p>	<p><b>D</b></p> <p><b>beyond MFV</b></p> <p>MSSM with <math>(\delta_{ij})_{AB} \neq 0</math> RS, Other <math>Z'</math> models, LR Models, NMFV</p>

# 2.

## **20 Goals in Flavour Physics for the Next Decade**

**1.**

Determination  
of  $|V_{us}|$ ,  $|V_{cb}|$ ,  
 $|V_{ub}|$  and  $\gamma$   
from  
Tree Level Decays

**2.**

Improved Lattice  
Calculations  
of  
 $F_{B_{s,d}}$ ,  $B_i$  -parameters

**3.**

Is  $\varepsilon_K$  (1964)  
consistent with  
 $S_{\psi K_S} = \sin 2\beta$   
(2001)  
within the SM?

**4.**

Is  $S_{\psi\phi}$   
much larger  
than  
 $(S_{\psi\phi})_{SM} \approx 0.035$  ?

( $\mathcal{CP}$  in  $B_s \rightarrow \psi\phi$ ) ( $A_{SL}^s$ )

**5.**

Clarification of  
few puzzles in  
Non-Leptonic  
Decays  
( $S_{\phi K_S}$ ,  $S_{\pi^0 K_S}$ ,  $\pi K$ , ...)

(Fleischer,..Buchalla,  
Gronau, London, ...)

**6.**

Discovery of  
 $B_s \rightarrow \mu^+ \mu^-$   
and  
 $B_d \rightarrow \mu^+ \mu^-$

**7.**

**Improved TH+EXP**

$$\begin{aligned}
\mathbf{B} &\rightarrow \mathbf{X}_{s,d} \gamma \\
\mathbf{B} &\rightarrow \mathbf{K}^* (\rho) \gamma \\
\mathbf{A}_{\text{CP}}^{\text{dir}} (\mathbf{B} &\rightarrow \mathbf{X}_s \gamma)
\end{aligned}$$

(Misiak,...)

**8.**

$$\begin{aligned}
\mathbf{B} &\rightarrow \mathbf{X}_s \mathbf{l}^+ \mathbf{l}^- \\
\mathbf{B} &\rightarrow \mathbf{K}^* \mathbf{l}^+ \mathbf{l}^-
\end{aligned}$$

in particular  
various angular  
observables  
(sensitive to NP)

(Hurth; Straub)

**9.**

$$\begin{aligned}
\mathbf{B}^+ &\rightarrow \tau^+ \nu \\
\mathbf{B}^+ &\rightarrow \mathbf{D}^0 \tau^+ \nu \\
\mathbf{H}^\pm &\text{ effects in} \\
\mathbf{Tree Level Decays}
\end{aligned}$$

(Hou..., Recksiegel,..  
Isidori, ... Westhoff,...)

**10.**

**Rare K Decays**

$$\begin{aligned}
\mathbf{K}^+ &\rightarrow \pi^+ \nu \bar{\nu} \\
\mathbf{K}_L &\rightarrow \pi^0 \nu \bar{\nu} \\
\mathbf{K}_L &\rightarrow \pi^0 \mu^+ \mu^- \\
\mathbf{K}_L &\rightarrow \pi^0 e^+ e^-
\end{aligned}$$

(TH very clean,  
sensitive to NP)

**11.**

**Rare B Decays**

$$\begin{aligned}
\mathbf{B} &\rightarrow \mathbf{X}_s \nu \bar{\nu} \\
\mathbf{B} &\rightarrow \mathbf{K}^* \nu \bar{\nu} \\
\mathbf{B} &\rightarrow \mathbf{K} \nu \bar{\nu}
\end{aligned}$$

(Straub) (sensitive to  
right-handed currents)

**12.**

**Lattice  
Calculations of  
Penguin hadronic  
matrix elements  
for  $\varepsilon'/\varepsilon$**   
(NA31, NA48, KTeV)

(Very sensitive to  
NP in the EW-Penguins)



**13.**

**$\mathcal{CP}$  in Charm  
Decays and  
 $D^+ \rightarrow l^+ \nu$ ,  $D_s^+ \rightarrow l^+ \nu$   
 $D^0 \rightarrow \mu^+ \mu^-$**

(Bigi; Grossman,..Golowich..  
Kronfeld)

**14.**

**Search for  $\mathcal{CP}$   
in the Lepton  
Sector and  
 $\theta_{13}$**

(Feruglio,..Antusch,..  
Branco,..Hagedorn)

**15.**

**Tests of  
 $\mu$ -e,  $\mu$ - $\tau$   
universalities  
in  
 $K^+ \rightarrow l^+ \nu$ ,  $B^+ \rightarrow l^+ \nu$**

(Isidori,..Paradisi, ...)

**16.**

**Lepton Flavour  
Violation  
 $\mu \rightarrow e \gamma$ ,  $\tau \rightarrow \mu \gamma$ ,  
 $\tau \rightarrow e \gamma$   
 $\mu \rightarrow 3e$ ,  $\tau \rightarrow 3e$   
 $\tau \rightarrow 3\mu$**

(Hisano,..Raidal,..)

**17.**

**Electric Dipole  
Moments  
of  
neutron, leptons  
( $d_n$ ,  $d_e$ )**

(Nagai, ...Paradisi,..)

**18.**

**Clarification  
of  
( $g-2$ ) $_{\mu}$   
Anomaly**

(Passera,..Jegerlehner,  
Czarnecki,..de Rafael)

**19.**

**Tests of Flavour  
Violation in  
High Energy  
Processes**

**(Hiller, Nir, Melic,  
Trampetic,...)**

**19.**

**Tests of Flavour  
Violation in  
High Energy  
Processes**

**(Hiller, Nir, Melic,  
Trampetic,...)**

**20.**

**Construction  
of  
a New SM**

**19.**

**Tests of Flavour  
Violation in  
High Energy  
Processes**

**(Hiller, Nir, Melic,  
Trampetic,...)**

**20.**

**Construction  
of  
a New SM**

**21.**

**22.**

**23.**

**24.**

# Searching for the Higgs



Robert Buras

**Near the Czarny Staw Gasiennicowy ( 10. September 2009)**

**3.**

**Waiting for Signals of  
New Physics in FCNC Processes**

# Models investigated by TUM-Teams

(This decade)

**SM**

**MFV**

**MSSM+MFV**

**Z'-Models**

**General  
MSSM**

**Universal  
Extra  
Dimensions**

**RS with  
custodial  
protection**

**Littlest  
Higgs**

**Littlest  
Higgs with  
T-Parity**

**SUSY+Flavour  
Abelian  
Symmetry  
(Agashe+Carone)**

**SUSY with  
SU(3) Flavour  
(Ross et al)  
(RVV2)**

**SUSY with  
SU(2) Flavour  
(LH-currents)**

**Flavour Blind  
MSSM**

# My Collaborators

**SUSY**



**W. Altmannshofer**

**S. Gori**

**P. Paradisi**

**D. Straub**

**LHT**



**M. Blanke**

**B. Duling**

**S. Recksiegel**

**C. Tarantino**

**RS**



**M. Albrecht**

**M. Blanke**

**B. Duling**

**K. Gemmler**

**S. Gori**

**A. Weiler**



## The ABBBSW Collaboration



**W. Altmannshofer**



**P. Ball**



**A. Bharucha**



**AJB**



**D. Straub**



**M. Wick**

## The BBBR Collaboration



**I. Bigi**



**M. Blanke**



**AJB**

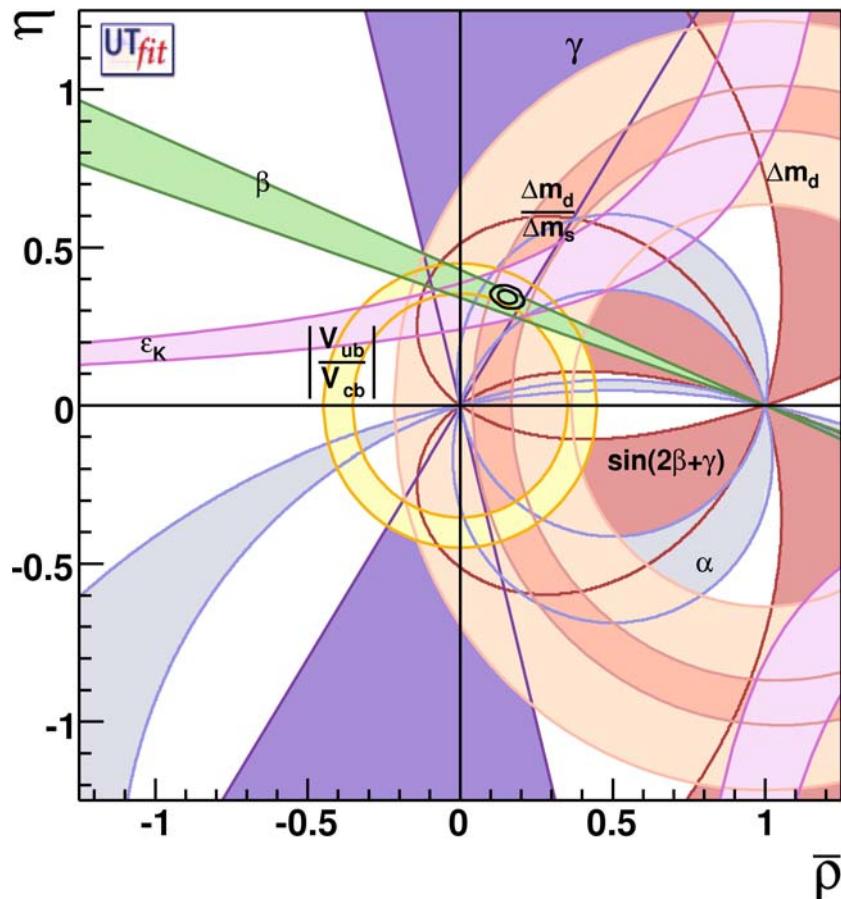


**S. Recksiegel**

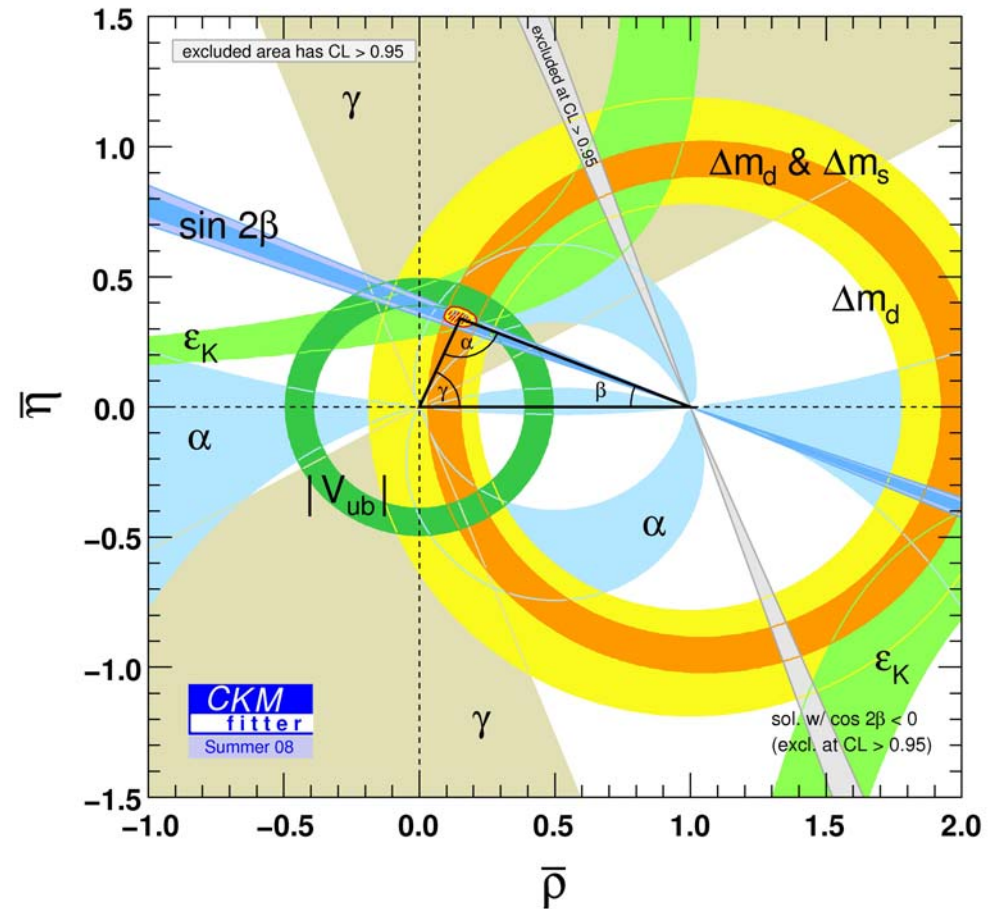
# Unitarity Triangle Fits

(Icons of Flavour Physics)

UT fit



CKM fitter



# Unitarity Triangle

$(R_b, \gamma)$   
Reference UT  
(Goto et al)

(coming  
decade)

$$\alpha \stackrel{?}{=} 90^\circ$$

(this  
decade)

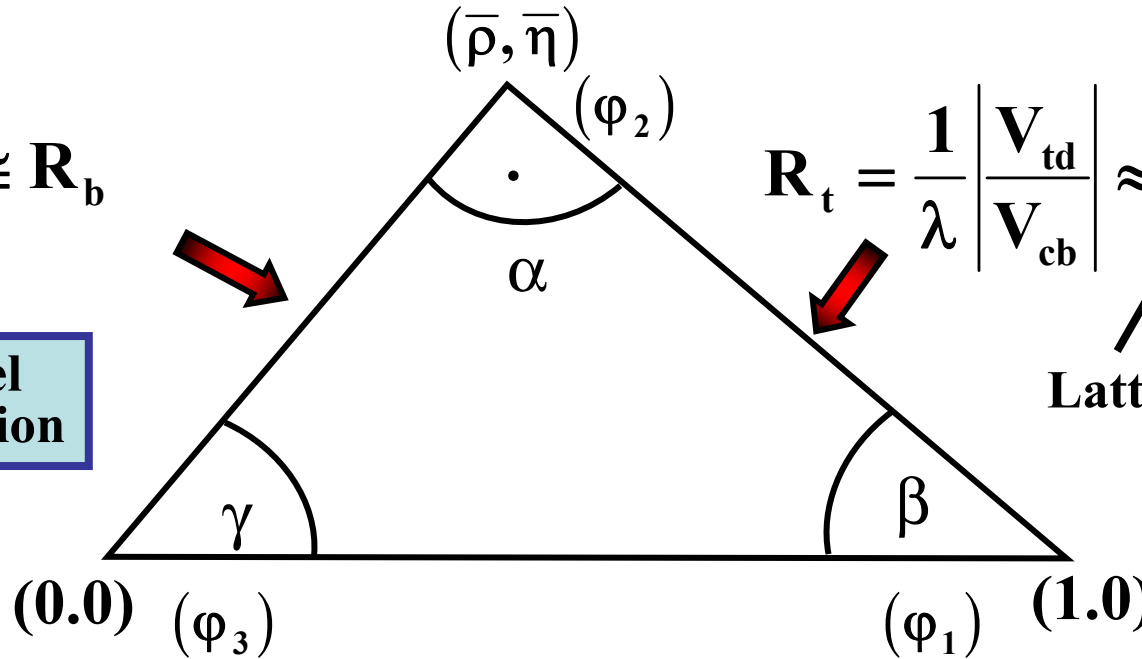
$R_t, \beta$   
Universal UT  
of CMFV  
(BGGJS, BBGT)

$(\varphi_{NP}=0, r_{NP}=1)$

$$\frac{1}{\lambda} \left| \frac{V_{ub}}{V_{cb}} \right| \cong R_b$$

Tree Level  
Determination

(NP free)



$$R_t = \frac{1}{\lambda} \left| \frac{V_{td}}{V_{cb}} \right| \approx \xi \sqrt{\frac{\Delta M_d}{\Delta M_s}} r_{NP}$$

Lattice

$$\xi = 1.21 \pm 0.04$$

Loop  
Determination

(Not NP free)

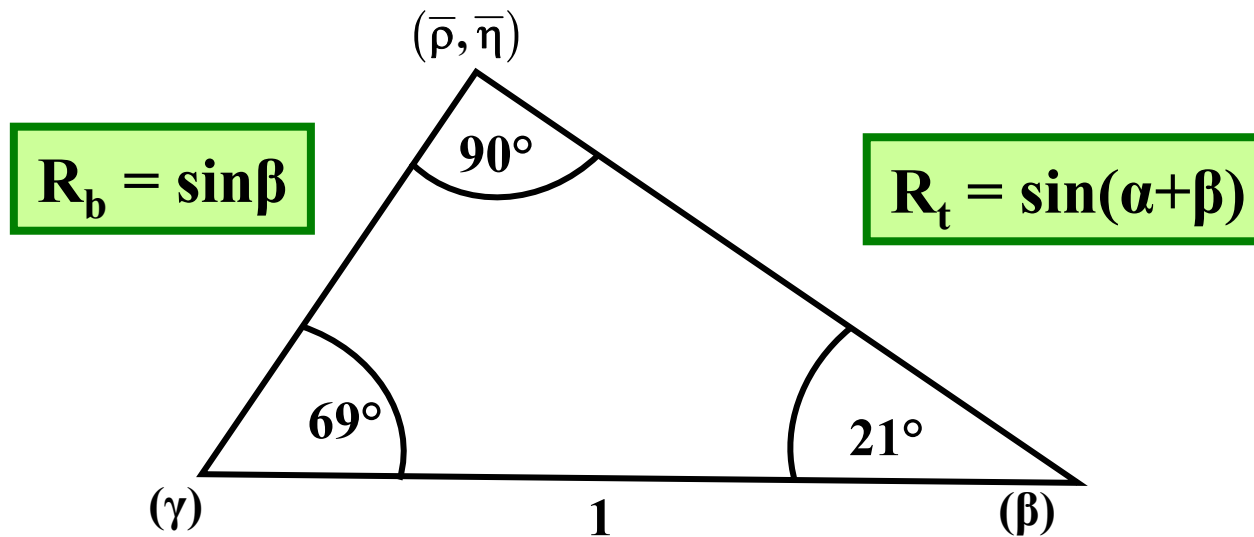
Flavour  
Matrix

$\varphi_{NP} = 0$	$\varphi_{NP} = 0$
$r_{NP} = 1$	$r_{NP} \neq 1$
$\varphi_{NP} \neq 0$	$\varphi_{NP} \neq 0$
$r_{NP} \neq 1$	$r_{NP} \neq 1$

$$S_{\psi K_s} = \sin(2\beta + 2\varphi_{NP})$$

# Unitarity Triangle in LO Approximation

$$\alpha = 90^\circ \quad \sin 2\beta = 2/3$$



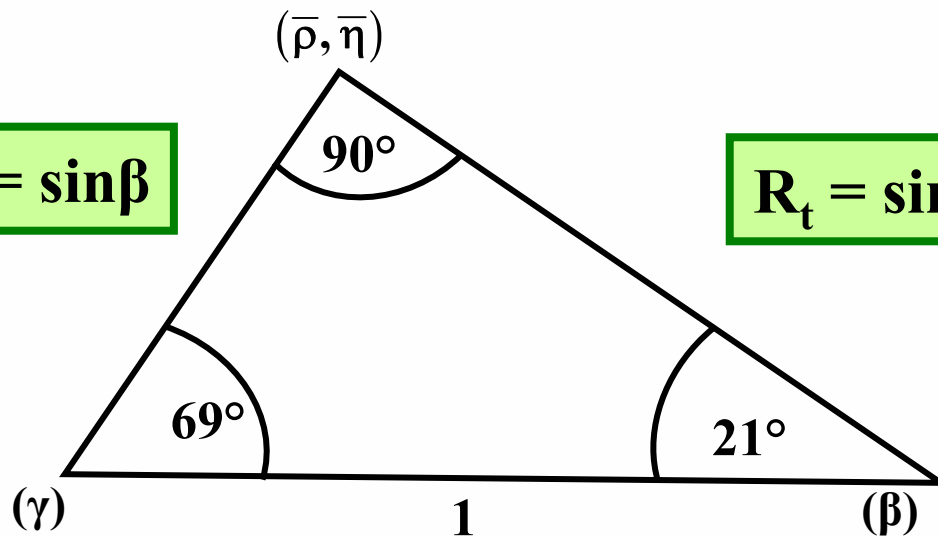
$$\bar{\rho} = \sin \beta \cos \gamma \quad \bar{\eta} = \sin \beta \sin \gamma$$

# Unitarity Triangle in LO Approximation

$$\alpha = 90^\circ \quad \sin 2\beta = 2/3$$

$$R_b = \sin \beta$$

$$R_t = \sin(\alpha + \beta)$$

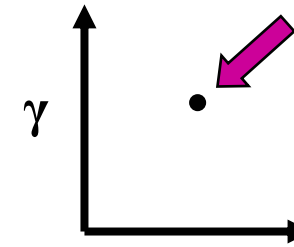


$$\bar{\rho} = \sin \beta \cos \gamma \quad \bar{\eta} = \sin \beta \sin \gamma$$

# Search for New Physics in 2010's

★ To study transparently possible tensions between  $\varepsilon_K$ ,  $\sin 2\beta$ ,  $V_{ub}$ ,  $\gamma$ ,  $\Delta M_d / \Delta M_s$

Leave  $(\bar{\rho}, \bar{\eta})$  plane  
Go to



Tree level (NP free) Determination possible

$$R_b \sim \left| \frac{V_{ub}}{V_{cb}} \right|$$

★ To search for NP in rare K, B<sub>d</sub>, B<sub>s</sub>, D decays, CP in B<sub>s</sub>, D decays, Lepton Flavour Violations

Go to

Specific Plots (Correlations)

$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu})$  vs  $\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$   
 $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$  vs  $S_{\psi\phi}$   
 $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$  vs  $\text{Br}(B_d \rightarrow \mu^+ \mu^-)$   
 $\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$  vs  $S_{\psi\phi}$   
 $d_n$  vs  $S_{\phi K_s}$   
 $A_{CP}(B \rightarrow X_S \gamma)$  vs  $S_{\phi K_s}$   
 $\text{Br}(\tau \rightarrow \mu \gamma)$  vs  $\Delta(g-2)_\mu$   
 $\text{Br}(\tau \rightarrow \mu \mu \mu)$  vs  $\text{Br}(\tau \rightarrow \mu \gamma)$   
 $\text{Br}(\mu \rightarrow 3e)$  vs  $\text{Br}(\mu \rightarrow e \gamma)$

★ Correlations will be crucial to distinguish various NP scenarios

# Can SM describe simultaneously CP in K and B<sub>d</sub> Systems?

$$|\epsilon_K|^{SM} \sim \kappa_\epsilon \hat{B}_K |V_{cb}|^2 \left( \underbrace{\frac{1}{2} |V_{cb}|^2 R_t^2 \sin 2\beta \eta_{tt}^{QCD}}_{\text{BJW (90)}} S_0(x_t) + \underbrace{F(\eta_{ct}^{QCD}, \eta_{cc}^{QCD}, m_c, \dots)}_{\text{HN (94)}} \right)$$

2009  
News



$$\hat{B}_K \cong 0.72 \pm 0.03$$

(precise and lower by  
~ 10% vs 2007)

RBC-UKQCD  
Aubin et al.  
ETMC

Large N  
 $\hat{B}_K = 0.75$



$$\kappa_\epsilon \cong 0.92 \pm 0.02$$

(correction neglected  
in the past)

AJB + Guadagnoli (08)  
(Nierste; Vysotsky)

BBG (87)



NNLO QCD  
calculation

of  $\eta_{cc}, \eta_{ct}$

Brod + Gorbahn (09)

(BG)

$$|\epsilon_K^{SM}| = (1.80 \pm 0.22) \cdot 10^{-3}$$

$$|\epsilon_{exp}| = (2.223 \pm 0.012) \cdot 10^{-3}$$

(BaBar  
Belle)

using  $(\sin 2\beta)_{\psi K_s} = 0.672 \pm 0.023$

(NA48, KLOE, KTeV)





**Diego Guadagnoli**



# Possible Solutions to $\varepsilon_K$ - Anomaly

$$|\varepsilon_K|^{\text{SM}} \sim \kappa_\varepsilon \hat{\mathbf{B}}_K |\mathbf{V}_{cb}|^2 \left( \frac{1}{2} |\mathbf{V}_{cb}|^2 \mathbf{R}_t^2 \sin 2\beta \eta_{tt}^{\text{QCD}} S_0(\mathbf{x}_t) + \mathbf{F}(\eta_{ct}^{\text{QCD}}, \eta_{cc}^{\text{QCD}}, \mathbf{m}_c, \dots) \right)$$

**1.**

Add New Physics to  $\varepsilon_K$

CMFV  $S_0(\mathbf{x}_t) \rightarrow S_0(\mathbf{x}_t) + \Delta S_0^{\text{NP}}$  or simply  $\Delta\varepsilon_k$  (Non-MFV)

AJB  
Guadagnoli

**2.**

Increase  $\sin 2\beta \cong 0.67 \Rightarrow 0.85$

$\varphi_{\text{NP}} \cong -8.1^\circ$

$$S_{\psi K_s} = \sin(2\beta + 2\varphi_{\text{NP}})$$

(Ufit; BBGT; Ball, Fleischer;  
Branco et al)

Large  $|\mathbf{V}_{ub}|$

Lunghi  
Soni

Super-B

**3.**

Increase  $R_t \rightarrow \gamma = \delta_{\text{CKM}} \approx 67^\circ \Rightarrow 82^\circ$

LHC

**4.**

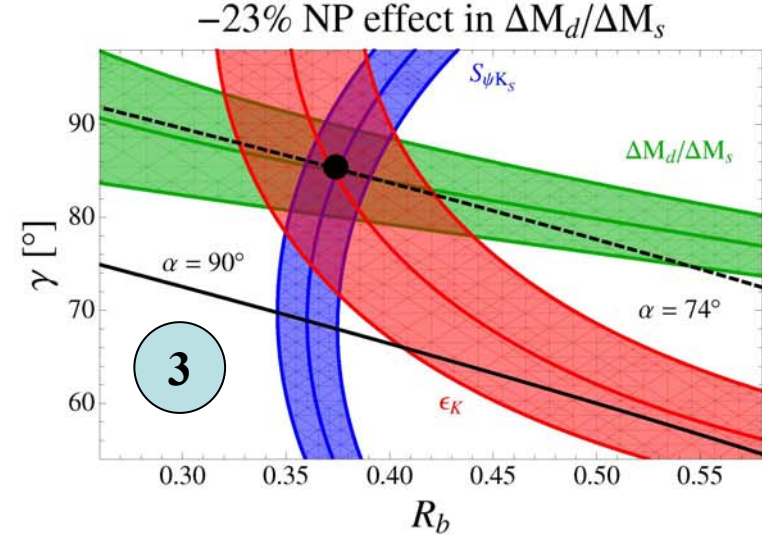
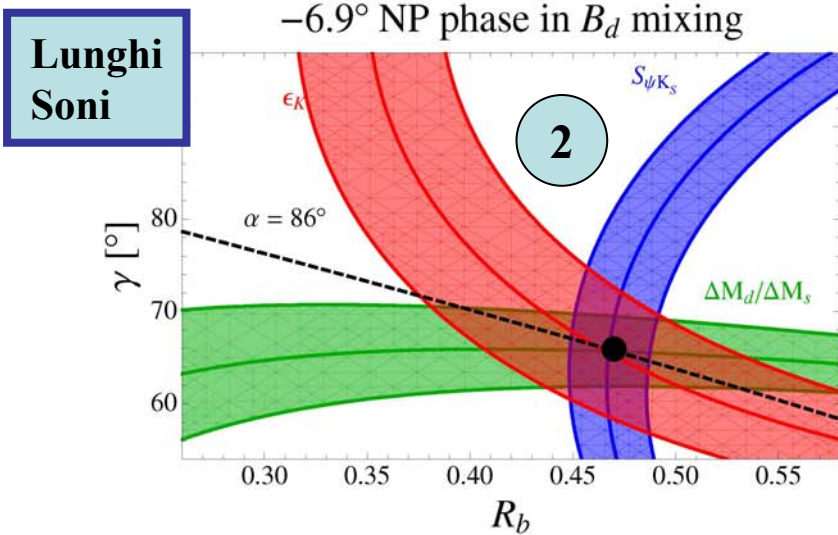
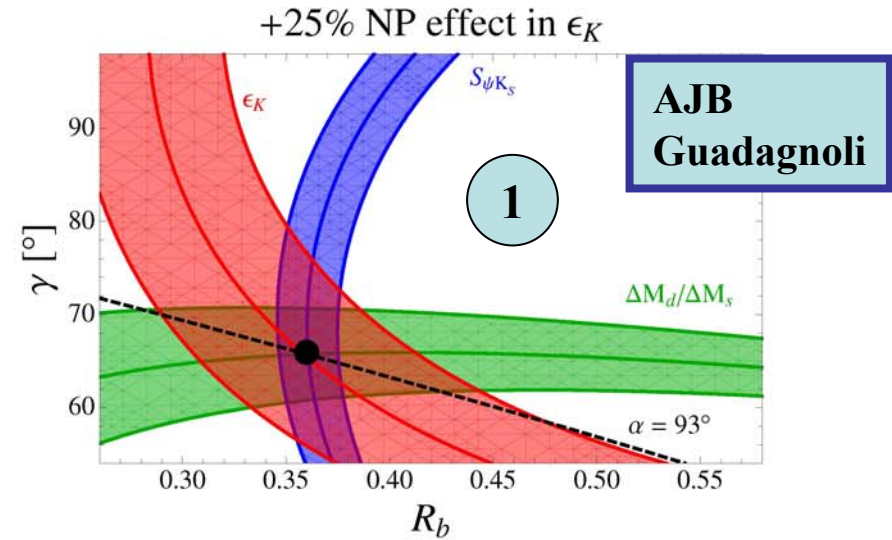
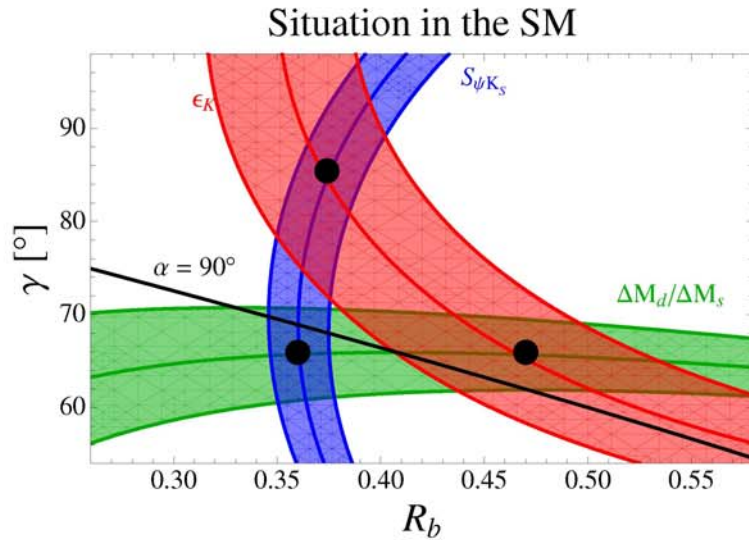
Increase  $|\mathbf{V}_{cb}| \approx (41.2 \cdot 10^{-3}) \Rightarrow (43.5 \cdot 10^{-3})$

Super-B

AJB, Parodi, Stocchi (2002)  
 Altmannshofer, AJB,  
 Guadagnoli (2007)

# The $R_b$ - $\gamma$ Plane

Altmannshofer, AJB, Gori,  
 Paradisi, Straub (2009)



# $K^+ \rightarrow \pi^+ \nu\bar{\nu}$ and $K_L \rightarrow \pi^0 \nu\bar{\nu}$ (Z<sup>0</sup>-penguins)

(TH cleanest FCNC decays in Quark Sector)

Extensive  
TH efforts  
over  
20 years

- Buchalla, AJB; Misiak, Urban (NLO QCD)
- AJB, Gorbahn, Haisch, Nierste (NNLO QCD)
- Brod, Gorbahn (QED, EW two loop)
- Isidori, Mescia, Smith (several LD analyses)
- Buchalla, Isidori (LD in  $K_L \rightarrow \pi^0 \nu\bar{\nu}$ )

$$\frac{\text{Br}(K^+ \rightarrow \pi^+ \nu\bar{\nu})}{\text{Br}(K_L \rightarrow \pi^0 \nu\bar{\nu})} = 3.2 \pm 0.2$$

SM

$$\text{Br}(K^+ \rightarrow \pi^+ \nu\bar{\nu}) = (8.4 \pm 0.7) \cdot 10^{-11} \quad \text{Br}(K_L \rightarrow \pi^0 \nu\bar{\nu}) = (2.6 \pm 0.4) \cdot 10^{-11}$$

Exp

$$\text{Br}(K^+ \rightarrow \pi^+ \nu\bar{\nu}) = \left( 17^{+11}_{-10} \right) \cdot 10^{-11} \quad \text{Br}(K_L \rightarrow \pi^0 \nu\bar{\nu}) \leq 6.8 \cdot 10^{-8}$$

(E787, E949 Brookhaven)

(E391a, KEK)

Future :

NA62  
Project X (FNAL) ↑

Both very  
sensitive to  
New Physics

J-PARC KOTO ↑

CP-conserving  
TH uncertainty 2-3%

CP-Violation in Decay  
TH uncertainty 1-2%

# Maximal Enhancements of $K_L \rightarrow \pi^0 \nu\bar{\nu}$ and $K^+ \rightarrow \pi^+ \nu\bar{\nu}$

Model independent bound

$$\text{Br}(K_L \rightarrow \pi^0 \nu\bar{\nu}) \leq 4.4 \text{ Br}(K^+ \rightarrow \pi^+ \nu\bar{\nu})$$

Grossman Nir

Model	$\text{Br}(K^+ \rightarrow \pi^+ \nu\bar{\nu})$	$\text{Br}(K_L \rightarrow \pi^0 \nu\bar{\nu})$
CMFV	20%	20%
MFV	30%	30%
LHT	150%	200%
RS	60%	150%
GMSSM	300%	500%
AC	2%	2%
RVV	10%	10%

(Bobeth et al  
Haisch, Weiler  
Isidori et al)

(Blanke et al)

(Duling et al)

(ABGPS)

SUSY with flavour symmetries



(abelian)

(non-abelian)

Large RH Currents

RS = RS with custodial protections

AC = Agashe, Carone

RVV = Ross, Velasco-Sevilla, Vives (04)

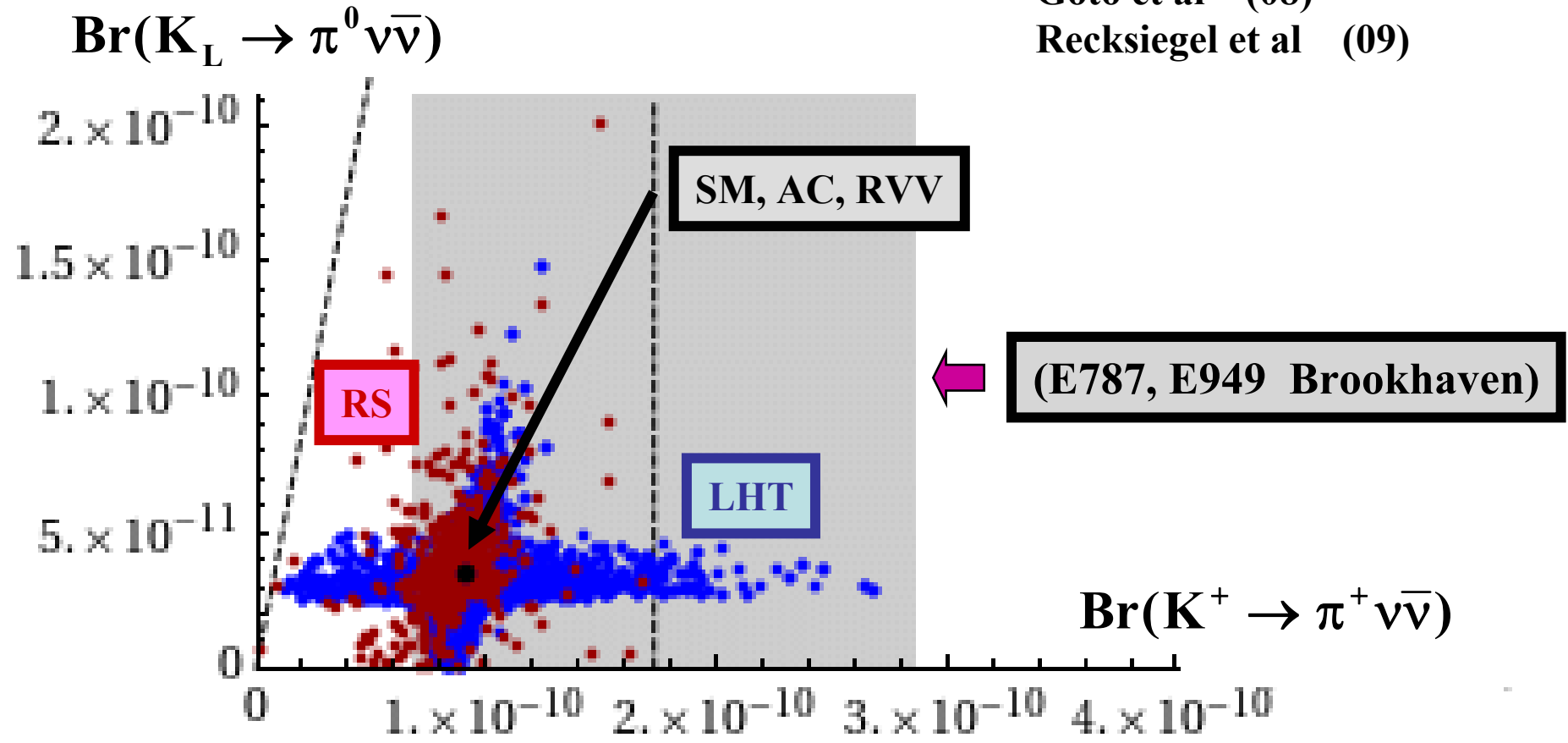
$U(1)_F$

$SU(3)_F$



$K_L \rightarrow \pi^0 \nu \bar{\nu}$  vs.  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

Blanke et al (08)  
Goto et al (08)  
Recksiegel et al (09)





$$\mathbf{B}_s \rightarrow \mu^+ \mu^- \text{ and } \mathbf{B}_d \rightarrow \mu^+ \mu^-$$

Z-Penguin (SM + Boxes CMV)

SM

$$\text{Br}(\mathbf{B}_s \rightarrow \mu^+ \mu^-) = (3.6 \pm 0.4) \cdot 10^{-9}$$

$$\text{Br}(\mathbf{B}_d \rightarrow \mu^+ \mu^-) = (1.1 \pm 0.1) \cdot 10^{-10}$$

Error dominated by  $\hat{\mathbf{B}}_{d,s}$

AJB (03)

CMFV  
“Golden Relation”

$$\frac{\text{Br}(\mathbf{B}_s \rightarrow \mu^+ \mu^-)}{\text{Br}(\mathbf{B}_d \rightarrow \mu^+ \mu^-)} = \frac{\hat{\mathbf{B}}_d}{\hat{\mathbf{B}}_s} \frac{\tau(\mathbf{B}_s)}{\tau(\mathbf{B}_d)} \frac{\Delta M_s}{\Delta M_d}$$

( $\Delta B = 1$ )

( $1.00 \pm 0.03$ )  
Lattice

( $\Delta B = 2$ )

Valid in all CMFV models

Can be strongly violated in SUSY, LHT, RS

95% CL

$$\text{Br}(\mathbf{B}_s \rightarrow \mu^+ \mu^-) \leq \begin{cases} 3.3 \cdot 10^{-8} \text{ (CDF)} \\ 5.3 \cdot 10^{-8} \text{ (D0)} \end{cases}$$

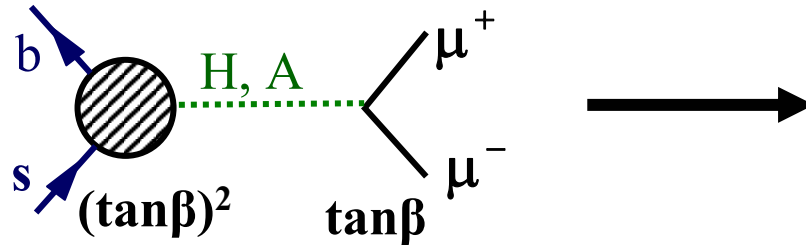
$$\text{Br}(\mathbf{B}_d \rightarrow \mu^+ \mu^-) \leq 1 \cdot 10^{-8} \text{ (CDF)}$$

LHC should be able to discover  $\mathbf{B}_s \rightarrow \mu^+ \mu^-$  even at the SM level

# $B_{s,d} \rightarrow \mu^+ \mu^-$ in SUSY and Higgs Penguins

(Helicity suppression lifted)

Babu, Kolda (99),...+100



$$\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-) \sim \frac{(\tan \beta)^6}{M_A^4}$$

Can reach CDF and DØ bounds

Very important for the distinction of SUSY from LHT and RS !!!



$$\frac{\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)_{\text{LHT}}}{\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)_{\text{SM}}} \leq 1.3$$

(Z-penguin)  
(Blanke et al) (09)

$$\frac{\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)_{\text{RS}}}{\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)_{\text{SM}}} \leq 1.1$$

(Z-penguin + Z-tree with  
r.h. couplings)  
(Custodial protection at work)  
(Gori et al) (08)

# Mixing Induced CP Asymmetry in $B_s \rightarrow \psi\phi$ ( $S_{\psi\phi}$ )

(TH very clean; <sup>\*</sup>Analog of  $S_{\psi K_s}$ )

$$S_{\psi\phi} = \sin(2|\beta_s| - 2\phi_s^{\text{new}}) \stackrel{\text{SM}}{\cong} 0.035$$

$$V_{ts} = -|V_{ts}|e^{-\beta_s}$$

$$(\beta_s = -1^\circ)$$

New Phase in  $B_s^0 - \bar{B}_s^0$  mixing

$$0.81^{+0.12}_{-0.32}$$



CDF  
D0

$$0.20 \leq (S_{\psi\phi})_{\text{exp}} \leq 0.98$$

90% C.L. (HFAG)

If confirmed, clear signal of NP with non-MFV interactions and new sources of CP

## Model Expectations

$$S_{\psi\phi} \leq \begin{cases} 0.75 \text{ (AC) (abelian flavour, SUSY) (Higgs penguin) } & \text{ABGPS} \\ 0.50 \text{ (RVV) (non-abelian flavour, SUSY) (Higgs penguin)} \\ 0.75 \text{ (RS) (Heavy KK Gauge Bosons) (Duling et al (08))} \\ 0.30 \text{ (LHT) (Mirror Fermions at work) (Tarantino et al (09))} \end{cases}$$

<sup>\*</sup>) See however Faller, Fleischer, Mannel (08)



# Maximal Enhancements of $S_{\psi\phi}$ , $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ and $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

(without taking correlation between them)

Model	Upper Bound on ( $S_{\psi\phi}$ )	Enhancement of $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$	Enhancement of $\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$
CMFV	0.04	20%	20%
MFV	0.04	1000%	30%
LHT	0.30	30%	150%
RS	0.75	10%	60%
GMSSM	0.75	1000%	300%
AC	0.75	1000%	2%
RVV	0.50	1000%	10%

**Correlations between  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ ,  $K_L \rightarrow \pi^0 \nu \bar{\nu}$ ,  $S_{\psi\phi}$ ,  $B_s \rightarrow \mu^+ \mu^-$**



**Impact of a future  $S_{\psi\phi} \approx 0.3$**

LHT  
RS

**Sizable Enhancements in  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$   
and  $K_L \rightarrow \pi^0 \nu \bar{\nu}$  excluded in RS and  
unlikely in LHT**

(Blanke et al)

**$B_{s,d} \rightarrow \mu^+ \mu^-$  SM-like**

(abelian)  
AC  
RVV  
(non-abelian)

**$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$  forced to be  
 $3 \cdot \text{Br}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} \sim 10^{-8}$**

**SUSY  
Flavour  
Models**

**Altmannshofer, AJB, Gori, Paradisi, Straub (09)**

**ABGPS**

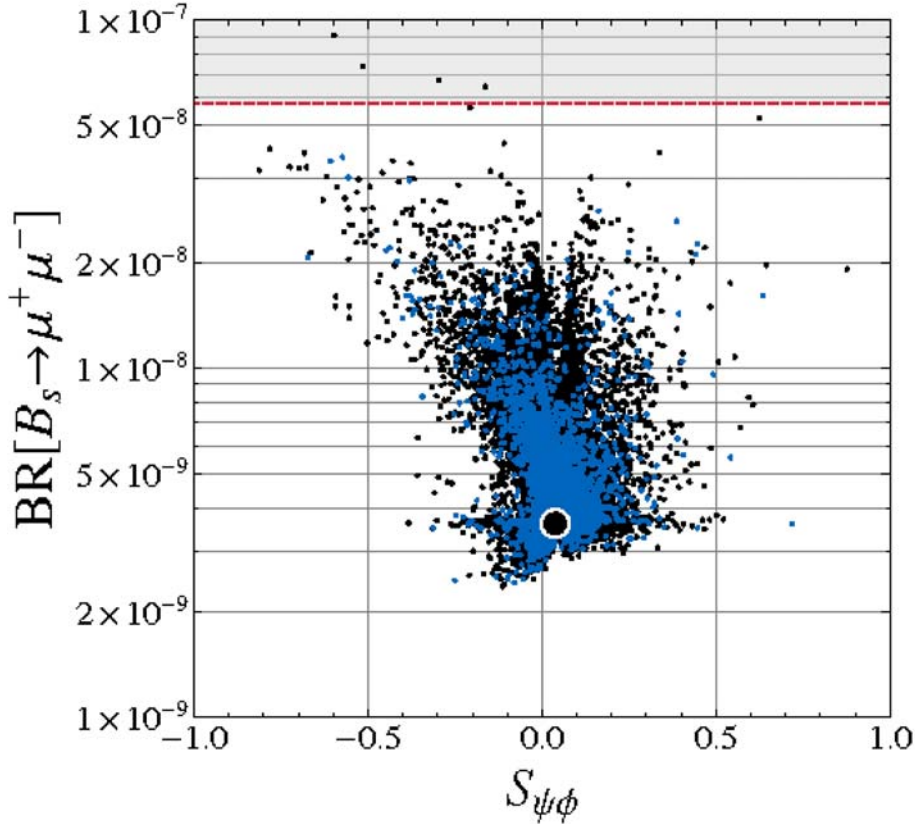
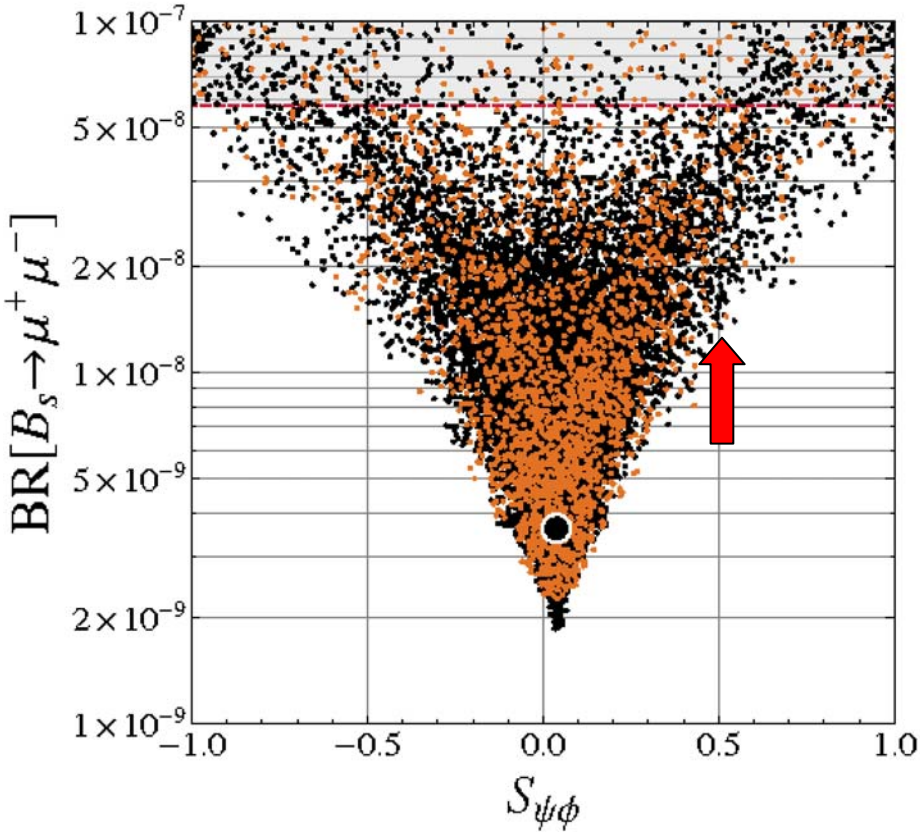
CDF, D0  
LHCb

# $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ vs $S_{\psi\phi}$

ABGPS

**Solution 3 to  $\epsilon_K$ -Anomaly**  
**Abelian (AC)**

**Solution 1 to  $\epsilon_K$ -Anomaly**  
**Non-Abelian (RVV)**



**(Large Effects in  $D^0-\bar{D}^0$ )**

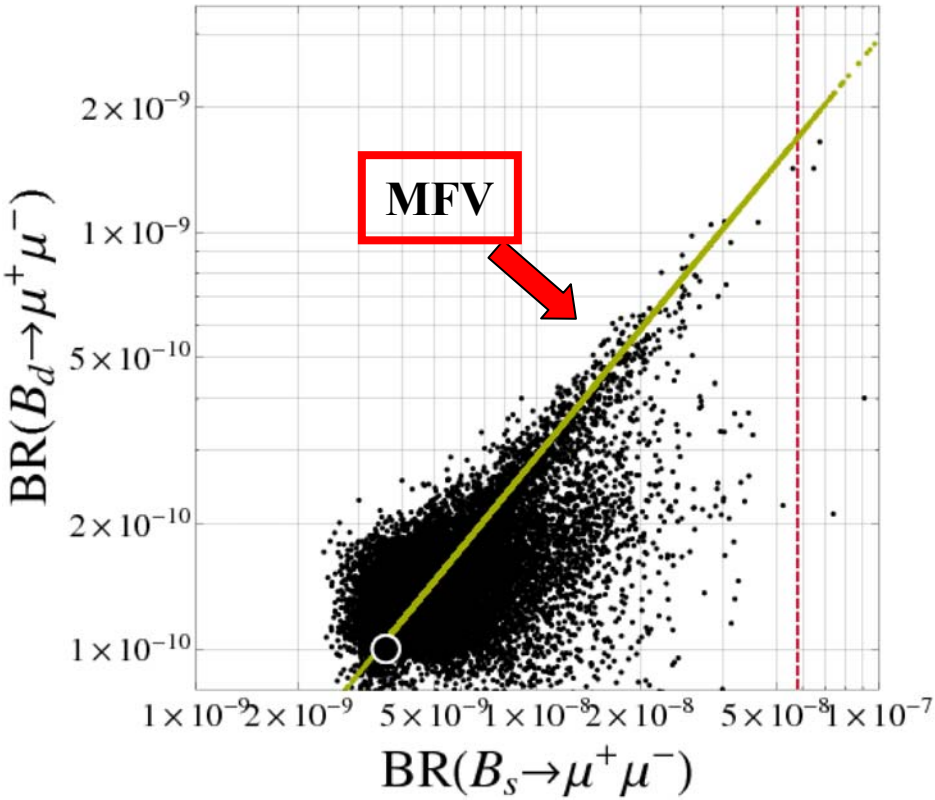
**(Small Effects in  $D^0-\bar{D}^0$ )**

ABGPS

# $\text{Br}(B_d \rightarrow \mu^+ \mu^-)$ vs $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$

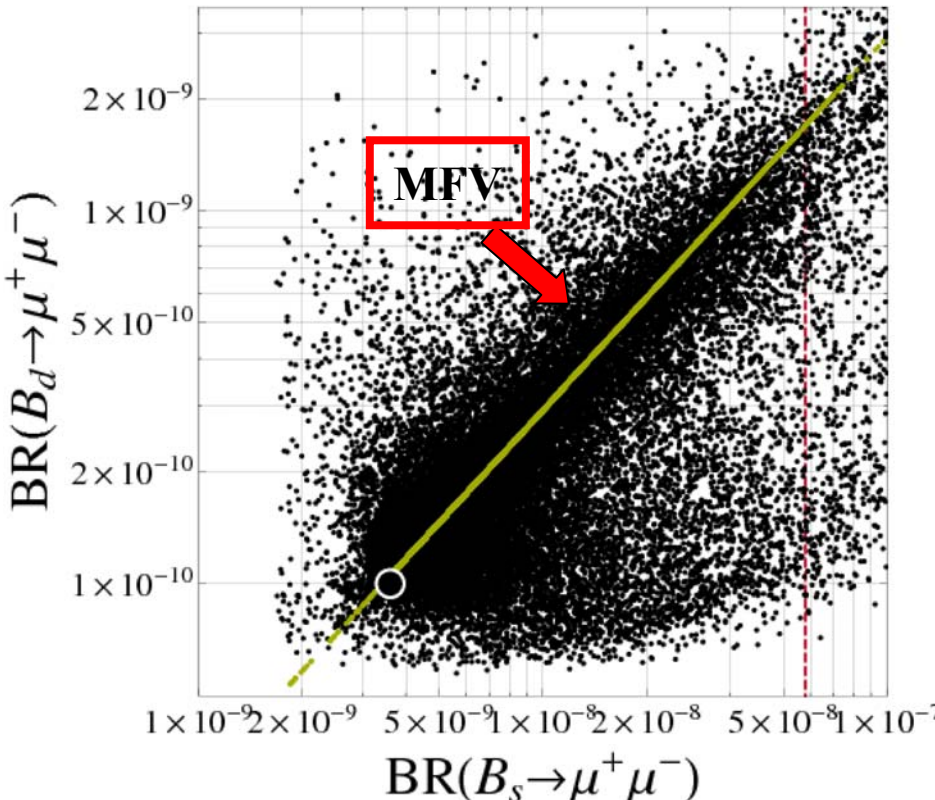
MFV

AJB; Hurth, Isidori, Kamenik Mescia



RVV2

(RH currents)



LH currents

# Lepton Flavour Violation, $\Delta(g-2)_\mu$ and EDM's

$$S_{\phi K_s} = 0.44 \pm 0.17 \quad (S_{\phi K_s})_{SM} \approx (S_{\psi K_s})_{SM} + 0.02 \approx 0.70$$

**(Beneke)**

**(MEGA)**  $\text{Br}(\mu \rightarrow e\gamma) < 1.2 \cdot 10^{-11} \rightarrow 10^{-13}$  **(MEG)** **SM:  $10^{-54}$**

$$(a_\mu)_{SM} < (a_\mu)_{\text{exp}} \quad (3.1\sigma)$$

$$a_\mu = \frac{1}{2}(g-2)_\mu$$

**(Regan et al)**  $d_e < 1.6 \cdot 10^{-27} \rightarrow 10^{-31}$   $(d_e)_{SM} \approx 10^{-38}$

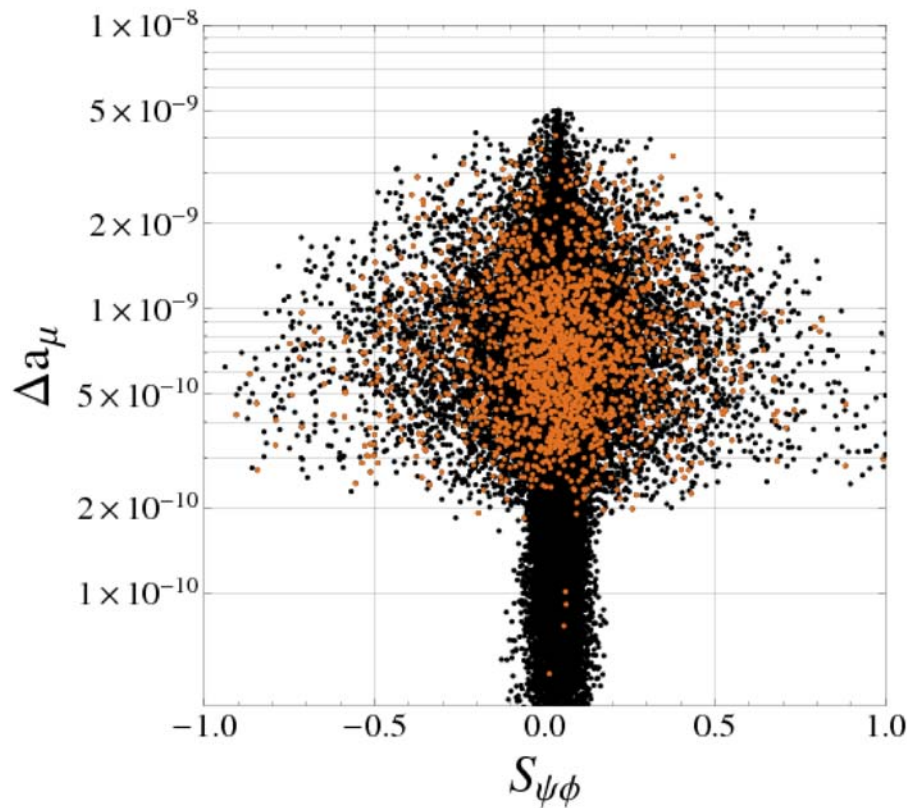
**(Baker et al)**  $d_n < 2.9 \cdot 10^{-26} \rightarrow 10^{-28}$   $(d_n)_{SM} \approx 10^{-32}$

[e cm]

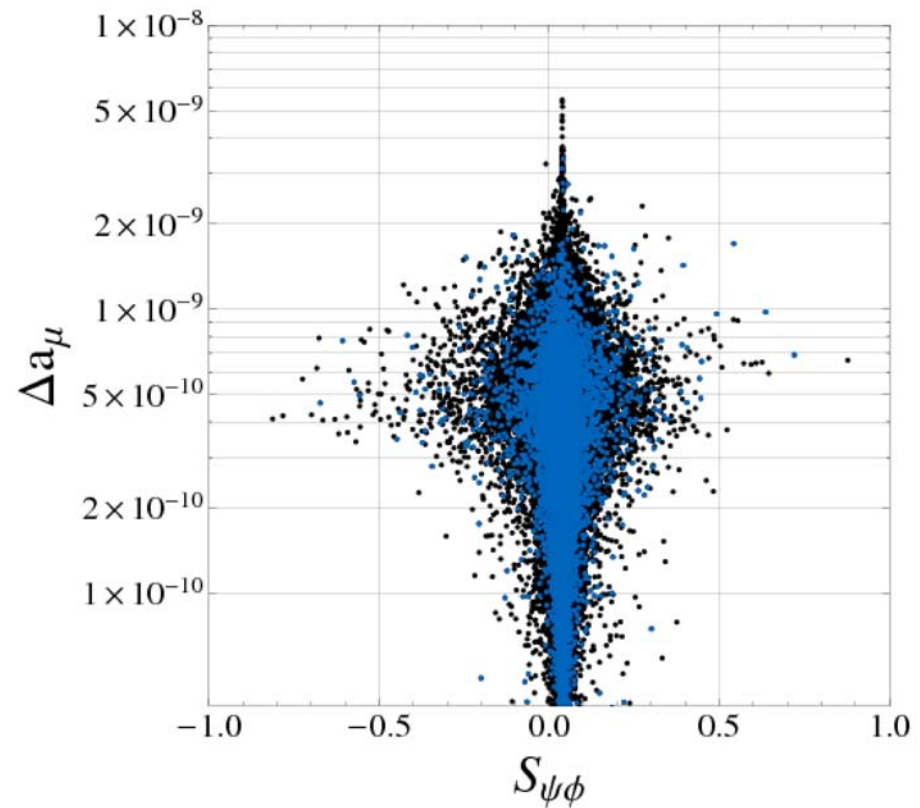
# Simultaneous Solution to $\Delta a_\mu$ and $S_{\psi\phi}$ Anomalies

■ Solution 3 to  $\epsilon_K$ -Anomaly  
Abelian (AC)

■ Solution 1 to  $\epsilon_K$ -Anomaly  
Non-Abelian (RVV)



(Large Effects in  $D^0-\bar{D}^0$ )

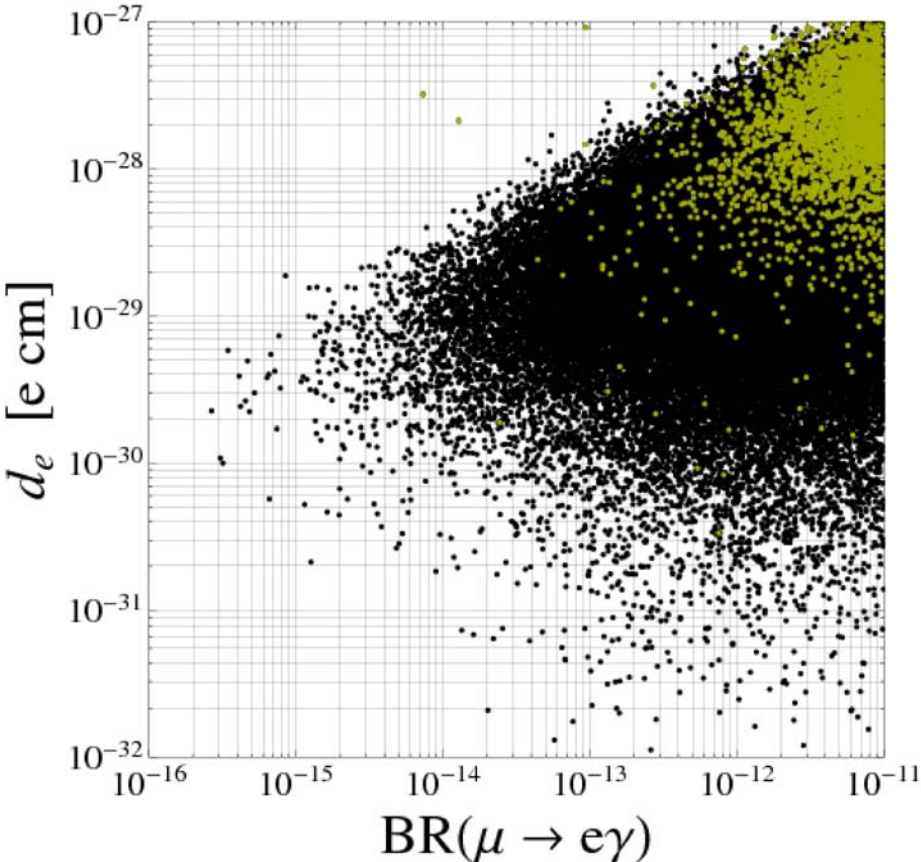
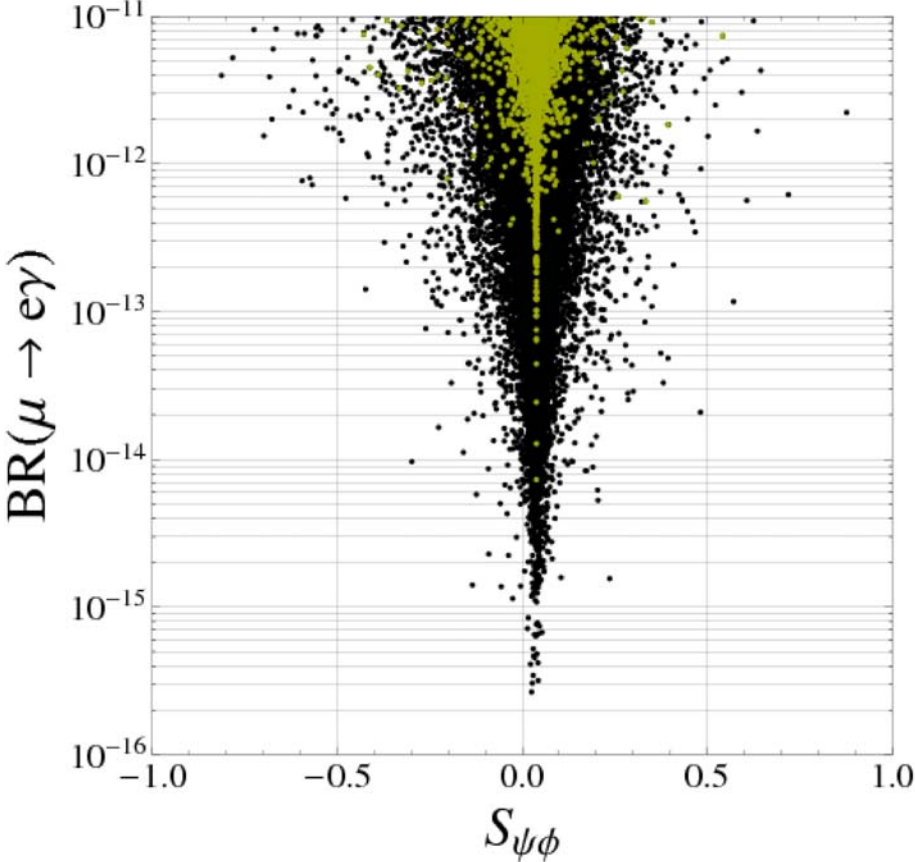


(Small Effects in  $D^0-\bar{D}^0$ )



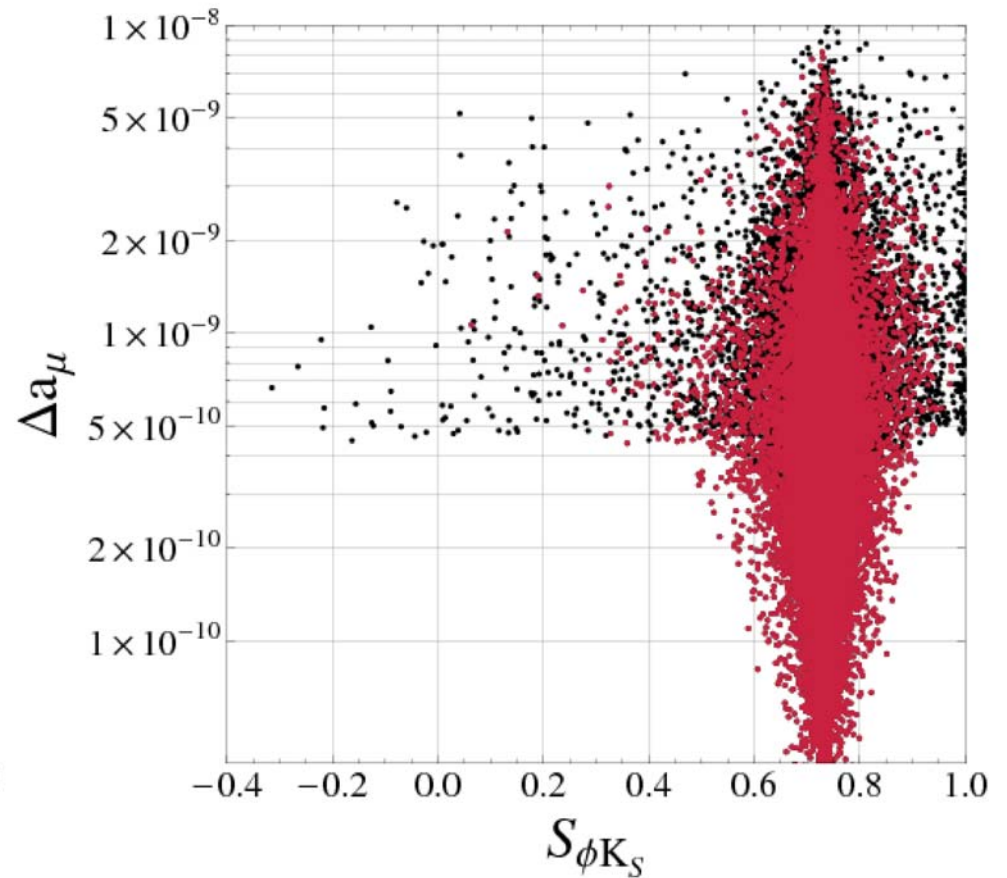
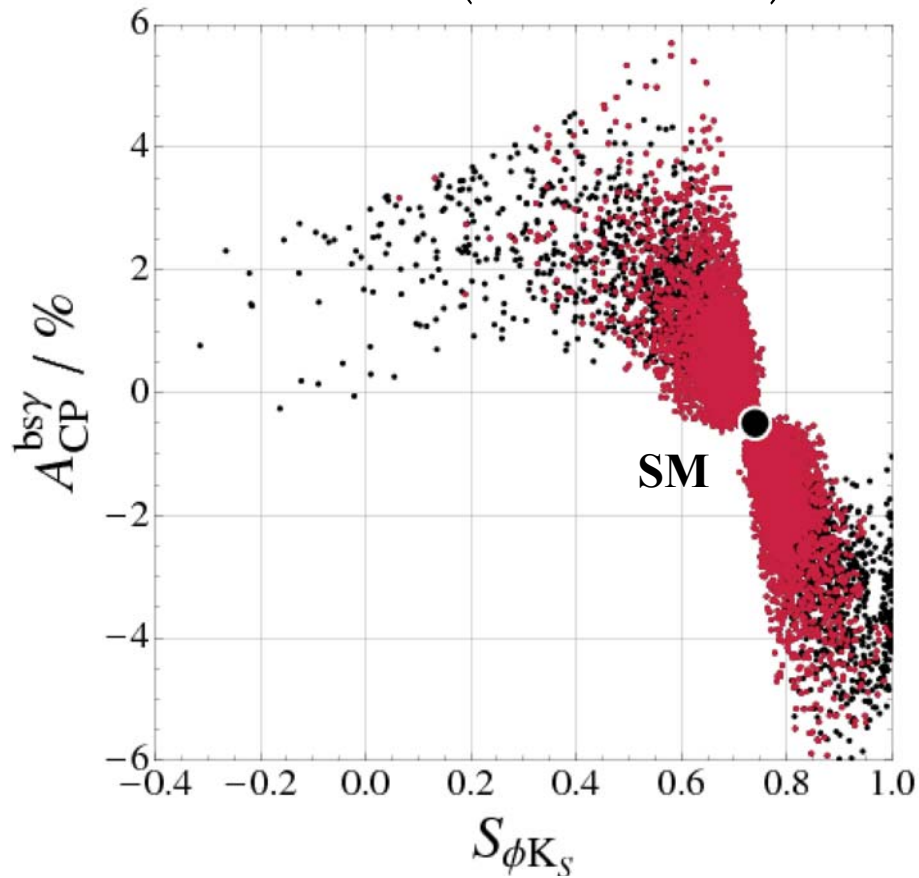
# Correlations in the SU(3) Flavour Model (RVV2)

■ Solution to  $(g-2)_\mu$  anomaly



# Correlations in a Flavour Model with LH Currents

■  $\text{Br}(\text{B}_s \rightarrow \mu^+ \mu^-) < 6 \cdot 10^{-9}$





# Clear Distinction between MSSM and LHT

**MSSM**

$$\frac{\text{Br}(\mu^- \rightarrow e^- e^+ e^-)}{\text{Br}(\mu^- \rightarrow e^- \gamma)} \approx \frac{1}{161}$$

$$\frac{\text{Br}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)}{\text{Br}(\tau^- \rightarrow \mu^- \gamma)} \approx \frac{1}{435}$$

**LHT**

**0.02 – 1**

**0.04 – 0.4**

**Both  
can  
reach  
MEGA's  
 $\mu \rightarrow e \gamma$   
bound**

**MSSM**

: (Ellis, Hisano, Raidal, Shimizu; Arganda, Herrero; Paradisi)  
(Brignole, Rossi)

**LHT**

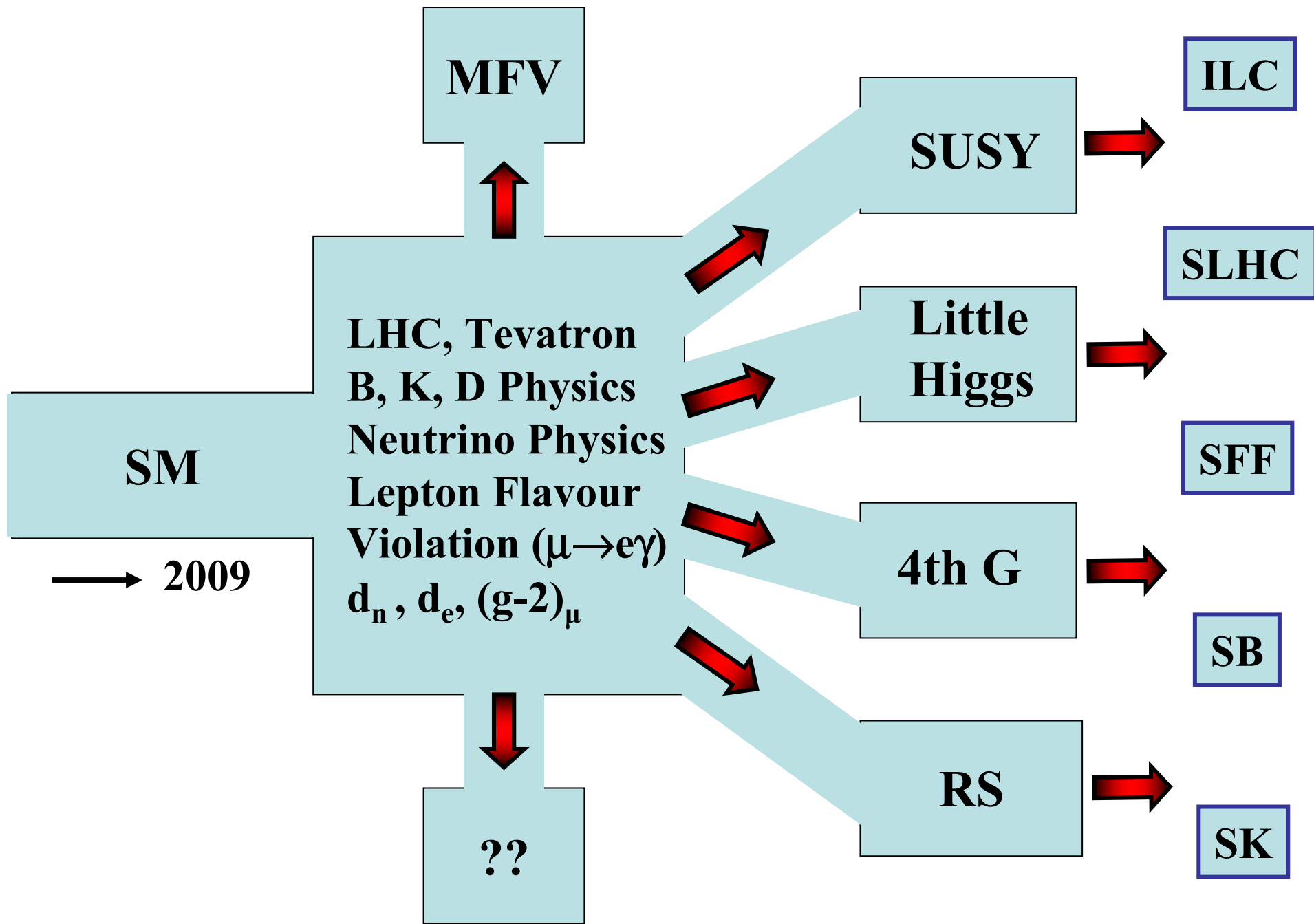
: (Blanke, Ajb, Duling, Poschenrieder, Tarantino) (2007)  
del Aguila, Illana, Jenkins (2008), Goto, Okada, Yamamoto (2009)

# DNA Tests of Flavour Models

	AC	RVV2	AKM	$\delta$ LL	FBMSSM	LHT	RS
$D^0 - \bar{D}^0$	★★★★	★	★	★	★	★★★★	?
$\epsilon_K$	★	★★★★	★★★★	★	★	★★	★★★★
$S_{\psi\phi}$	★★★★	★★★★	★★★★	★	★	★★★★	★★★★
$S_{\phi K_S}$	★★★★	★★	★	★★★★	★★★★	★	?
$A_{CP}(B \rightarrow X_s \gamma)$	★	★	★	★★★★	★★★★	★	?
$A_{7,8}(B \rightarrow K^* \mu^+ \mu^-)$	★	★	★	★★★★	★★★★	★★	?
$A_9(B \rightarrow K^* \mu^+ \mu^-)$	★	★	★	★	★	★	?
$B \rightarrow K^{(*)} \nu \bar{\nu}$	★	★	★	★	★	★	★
$B_s \rightarrow \mu^+ \mu^-$	★★★★	★★★★	★★★★	★★★★	★★★★	★	★
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	★	★	★	★	★	★★★★	★★★★
$\mu \rightarrow e \gamma$	★★★★	★★★★	★★★★	★★★★	★★★★	★★★★	★★★★
$d_n$	★★★★	★★★★	★★★★	★★	★★★★	★	★★★★
$d_e$	★★★★	★★★★	★★	★	★★★★	★	★★★★
$(g - 2)_\mu$	★★★★	★★★★	★★	★★★★	★★★★	★	★★

**4.**

# **Final Messages**



## Final Messages of this Talk

**Flavour  
Physics  
(Quarks  
and  
Leptons)**

:

**Many observables (decays) not measured yet or measured poorly. Flavour Physics only now enters the precision era.**



**Spectacular  
deviations from SM  
still possible**



**Interplay**

**Direct searches  
at Tevatron, LHC,  
ILC**

## Final Messages of this Talk

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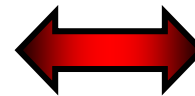
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Flavour  
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**Correlations between various  
observables can distinguish NP  
scenarios easier than LHC !**



**Great discoveries are just ahead of us !**

## Final Messages of this Talk

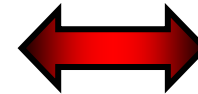
**Flavour  
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NP models**

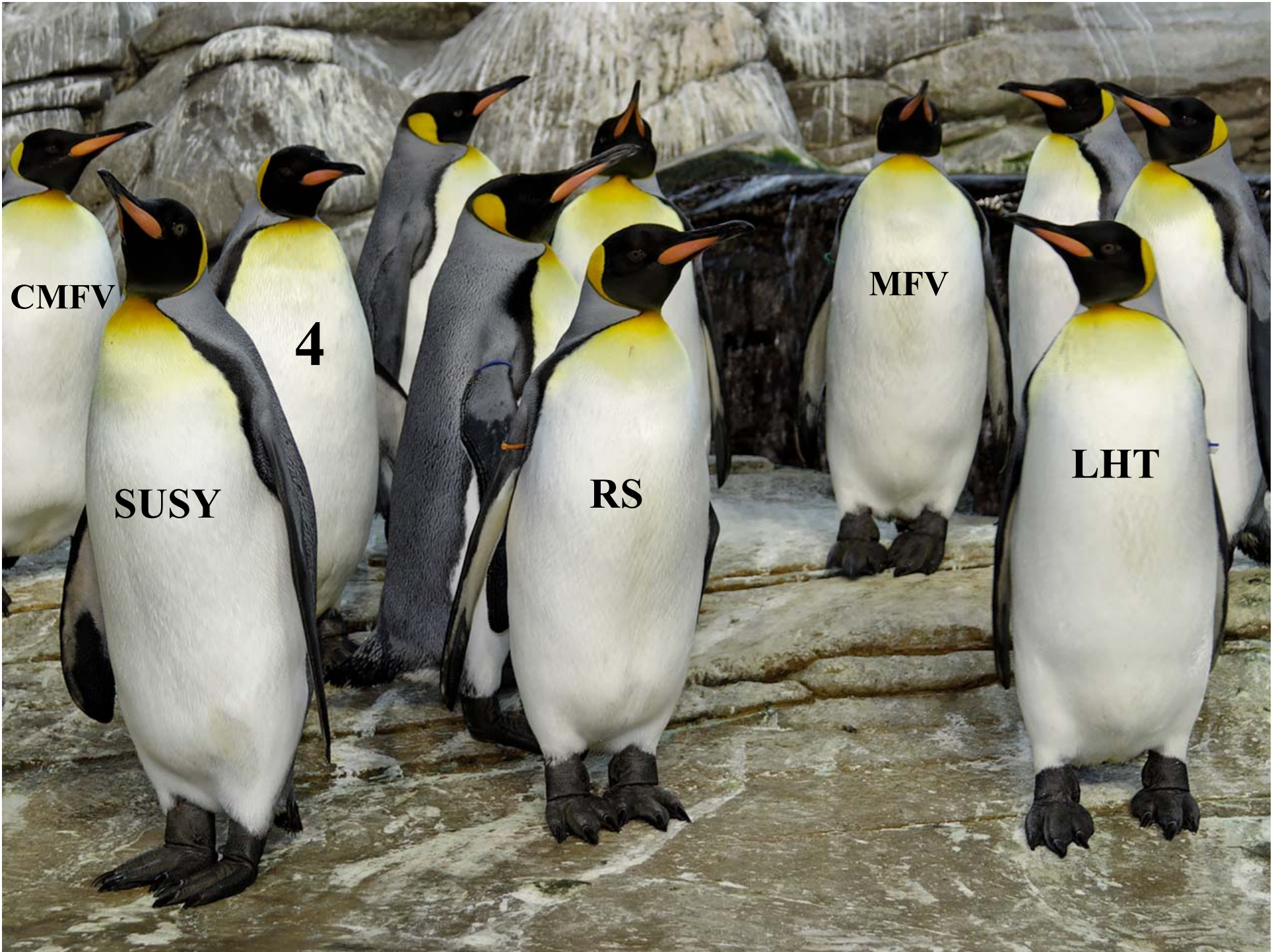
**Correlations between various  
observables can distinguish NP  
scenarios easier than LHC !**



**Thank  
You !**

**Great discoveries are just ahead of us !**





CMFV

SUSY

4

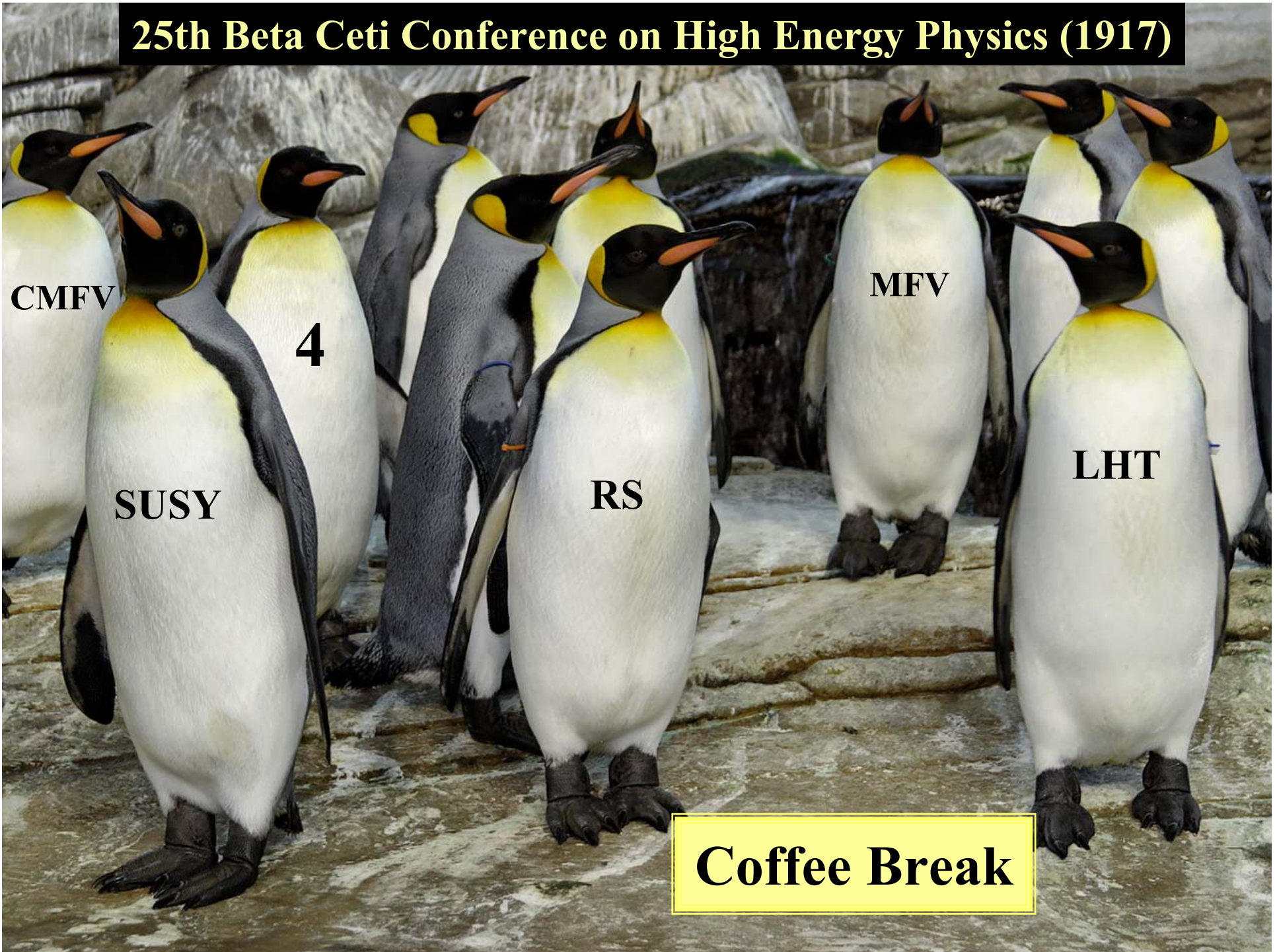
RS

MFV

LHT



# 25th Beta Ceti Conference on High Energy Physics (1917)



CMFV

4

SUSY

RS

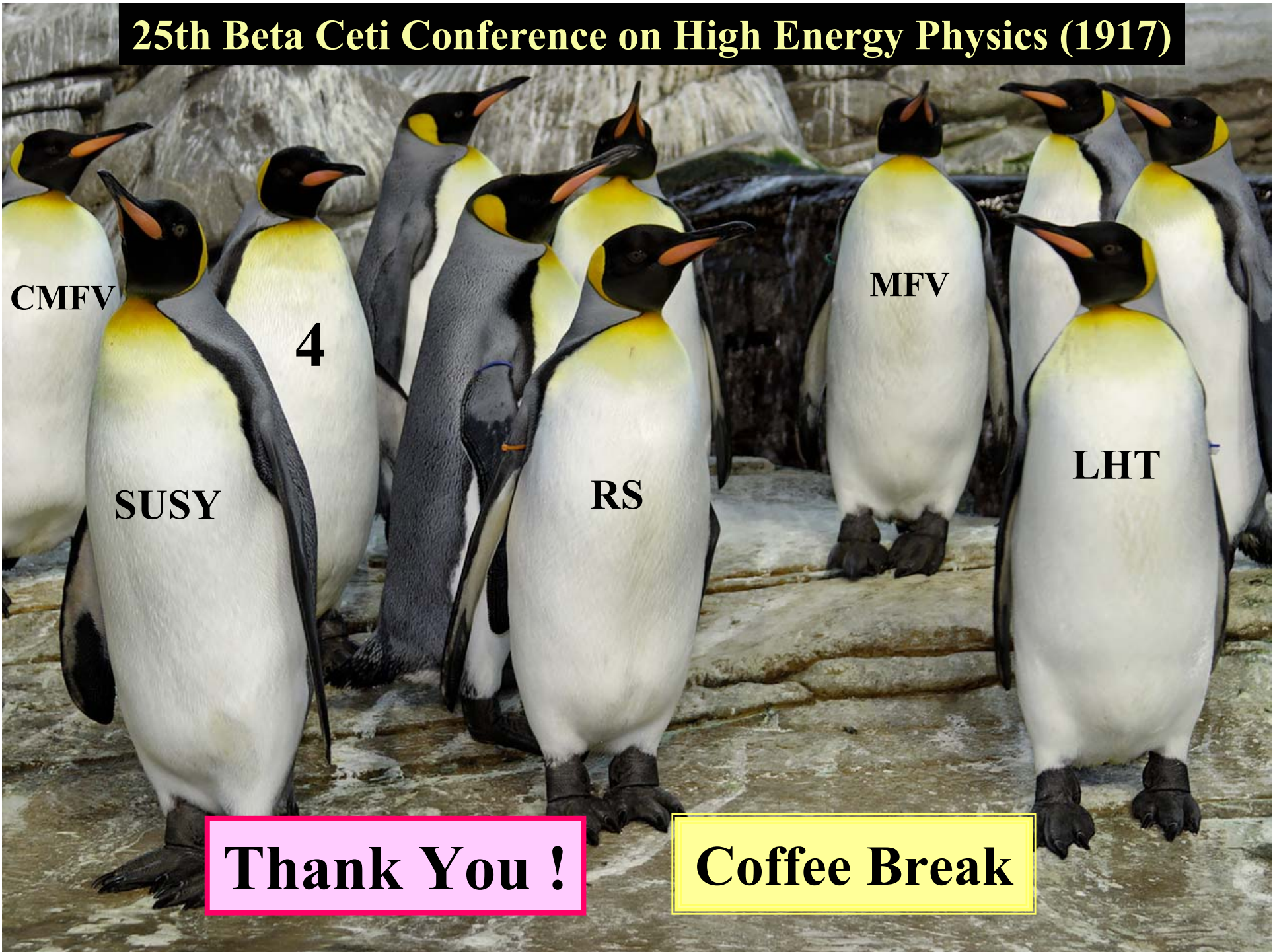
MFV

LHT

Coffee Break



**25th Beta Ceti Conference on High Energy Physics (1917)**



CMFV

4

SUSY

RS

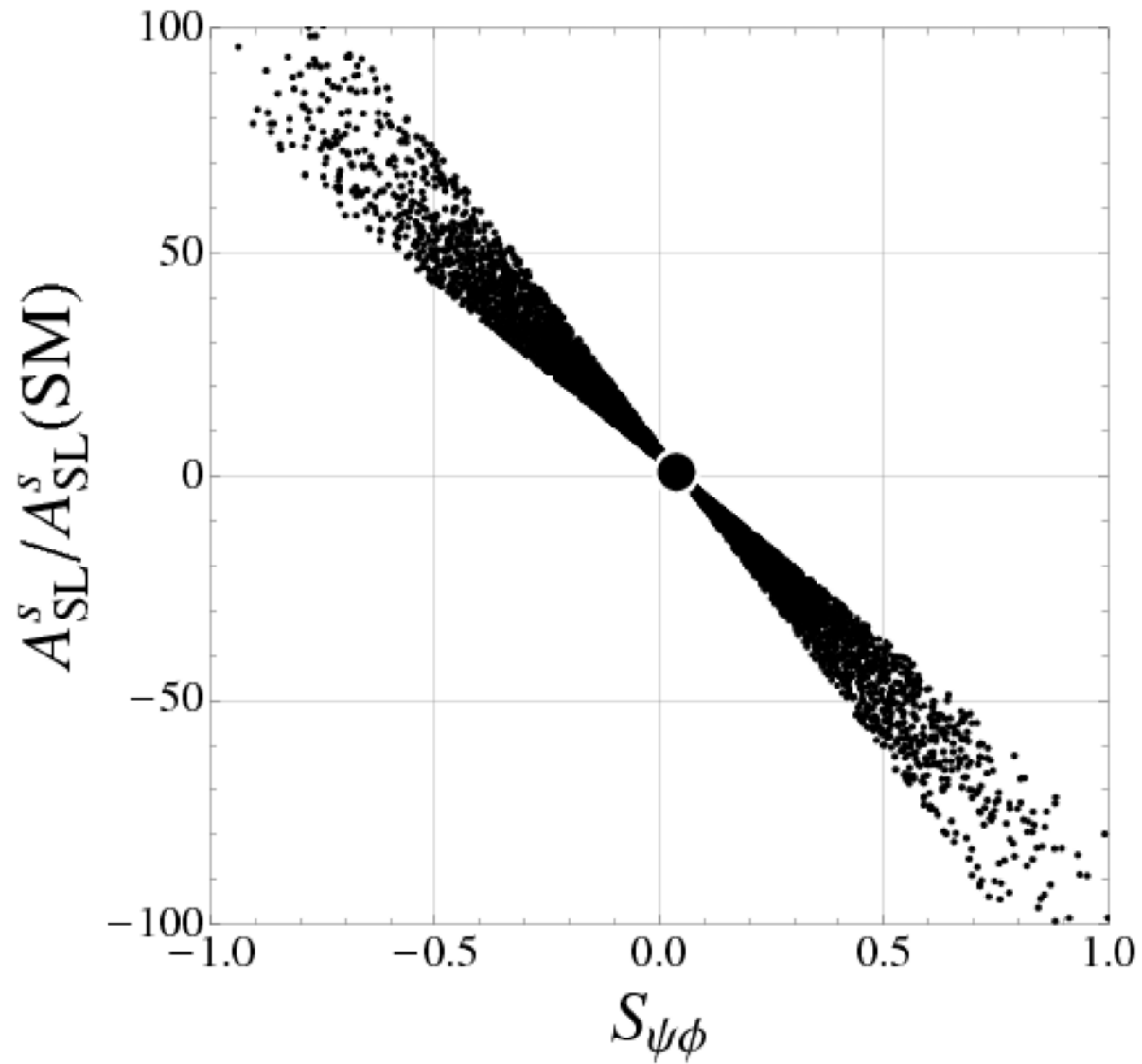
MFV

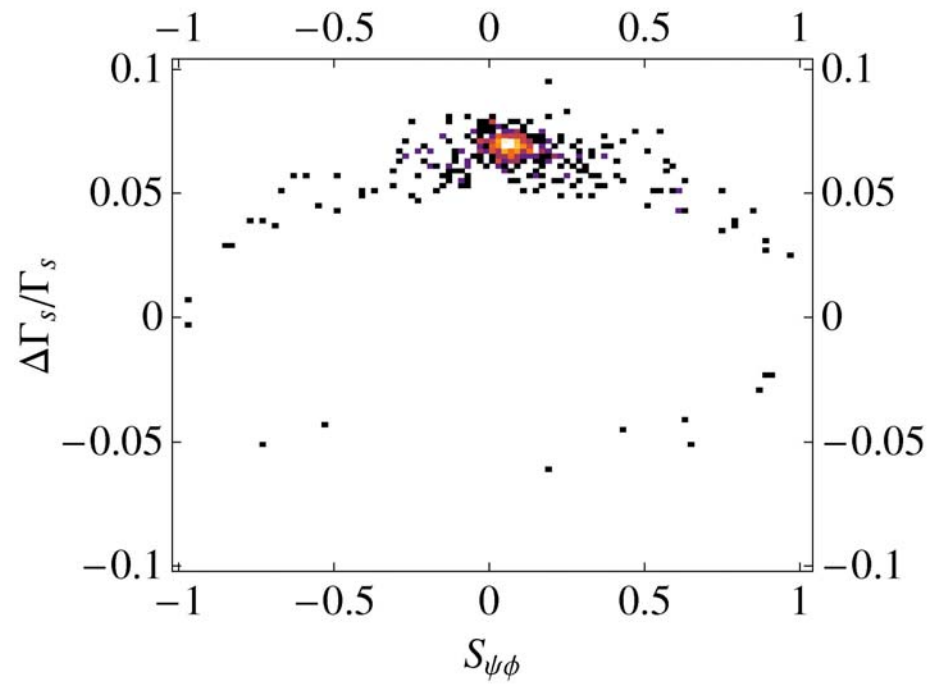
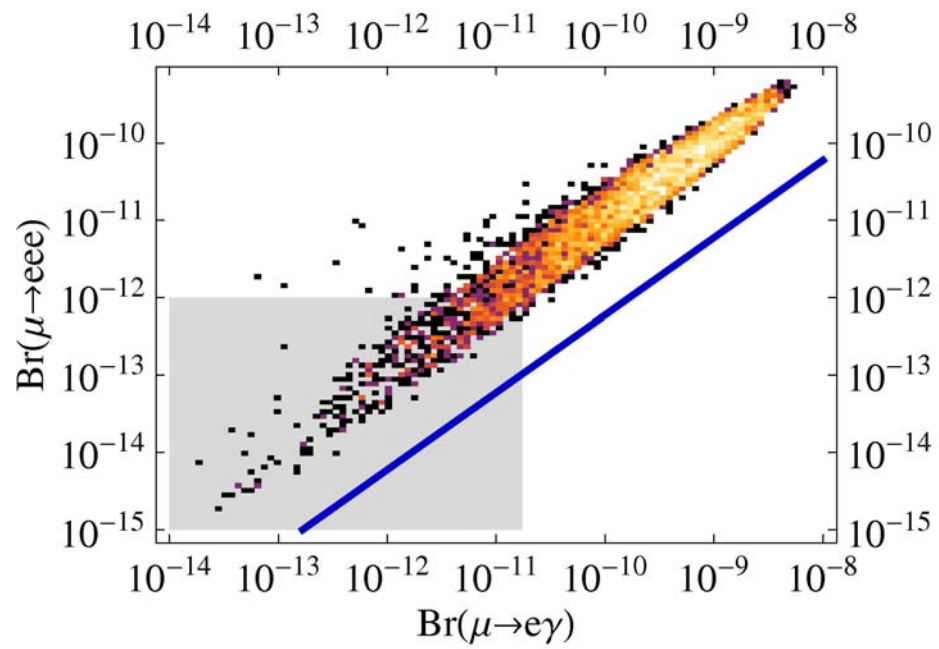
LHT

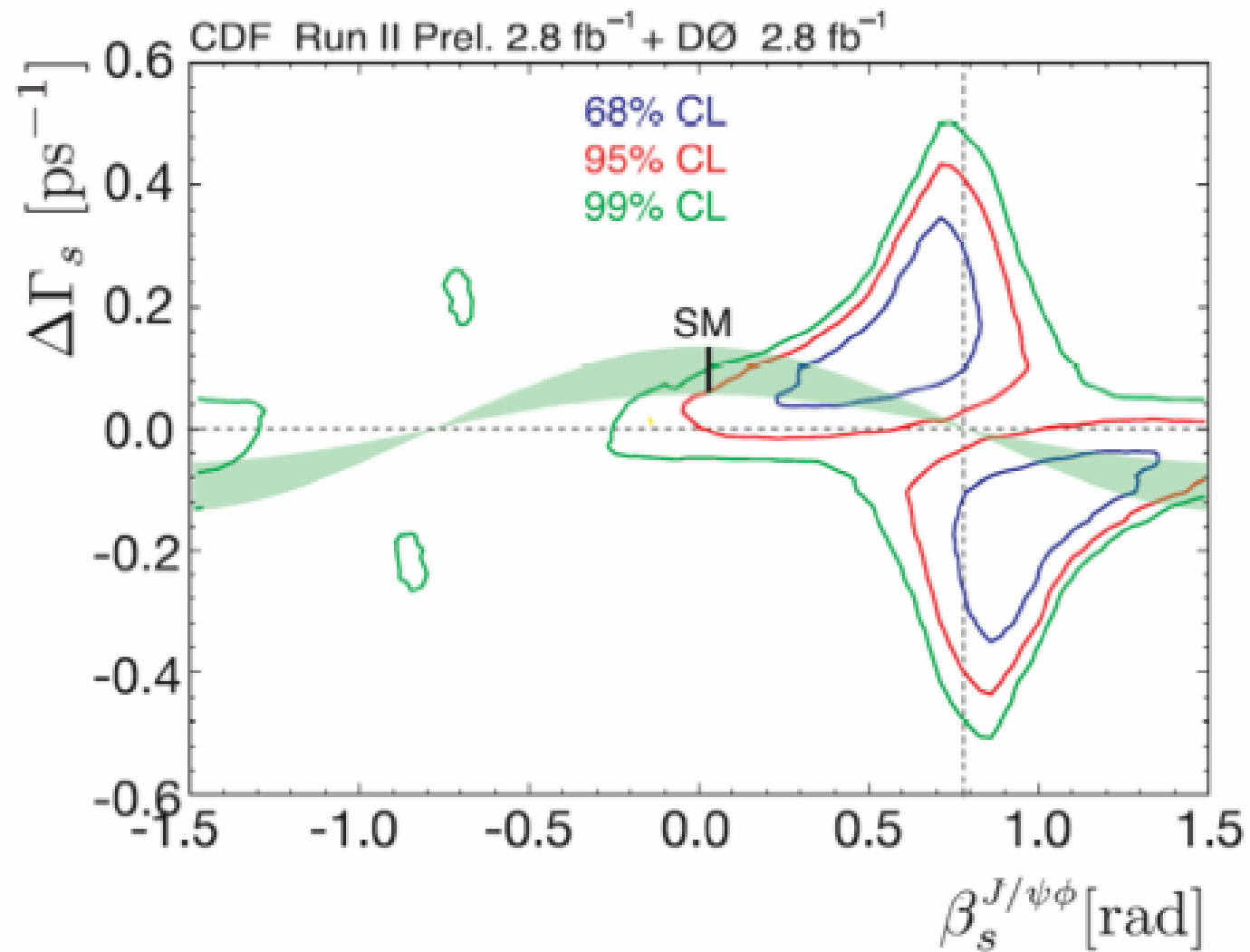
**Thank You !**

**Coffee Break**

# Backup









# DNA Flavour Test of New Physics Models

	GMSSM	AC	RVV	$\delta_{LL}$ only	FBMSSM
$D^0 - \bar{D}^0$ mixing	★★★★	★★★★	★	★	★
$\epsilon_K$	★★★★	★	★★★★	★	★
$S_{\psi\phi}$	★★★★	★★★★	★★★★	★	★
$S_{\phi K_S}, S_{\eta' K_S}$	★★★★	★★★★	★★	★★★★	★★★★
$A_{CP}^{bs\gamma}$	★★★★	★	★	★★★★	★★★★
$\langle A_{7,8} \rangle (B \rightarrow K^* \mu^+ \mu^-)$	★★★★	★	★★	★★★★	★★★★
$\langle A_9 \rangle (B \rightarrow K^* \mu^+ \mu^-)$	★★★★	★	★★	★	★
$B_s \rightarrow \mu^+ \mu^-$	★★★★	★★★★	★★★★	★★★★	★★★★
$B \rightarrow K^{(*)} \nu \bar{\nu}$	★★	★	★	★	★
$K \rightarrow \pi \nu \bar{\nu}$	★★★★	★	★★	★	★
$d_e, d_n$	★★★★	★★★★	★★	★★	★★★★

★★★★: large effects, ★★: medium effects, ★: small effects

# Return of $\varepsilon'/\varepsilon$ ?

**Final  
Result  
(NA48, KTeV)**

$$\text{Re}(\varepsilon'/\varepsilon) = (16.8 \pm 1.4) \cdot 10^{-4}$$

**(2009)**

$$\text{Re}(\varepsilon'/\varepsilon)_{\text{SM}} \approx \left\{ \begin{array}{l} \text{QCD} \\ \text{Penguins} \end{array} \right\}_{(B_6)} - \left\{ \begin{array}{l} \text{Electroweak} \\ \text{Penguins} \end{array} \right\}_{(B_8)}$$

**Very sensitive  
to New Physics**

**Wilson  
Coefficients  
of Penguins  
known at  
NLO (1990's)  
Munich (92,93)  
Rome (93)**

**Large N calculations of  
hadronic Matrix Elements**

**Bardeen, AJB, Gerard (85)  
Pich et al  
De Rafael et al.  
Bijnens + Prades } (1990's)**

**New Efforts  
on the Lattice**

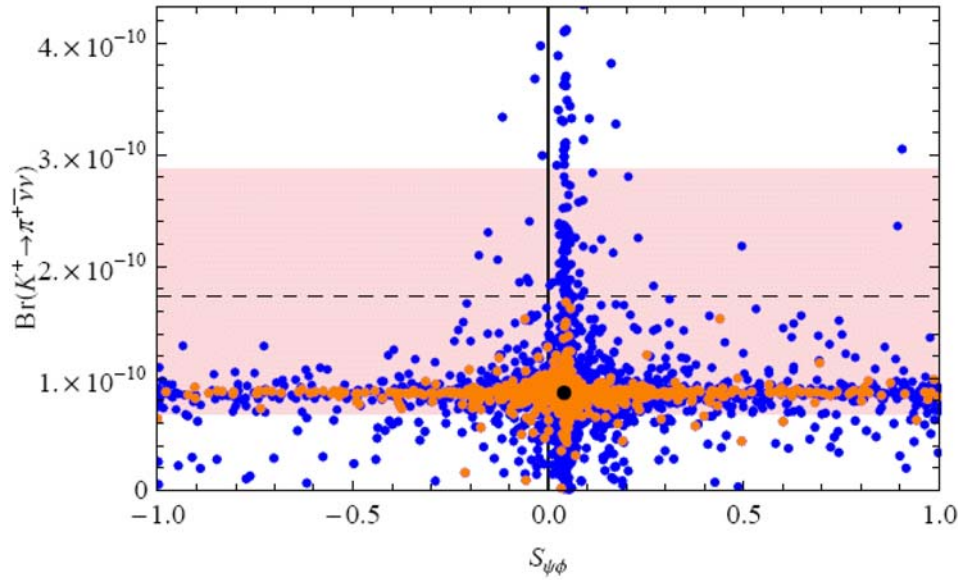
**(Norman Christ  
et al.)**

**20015 ?**



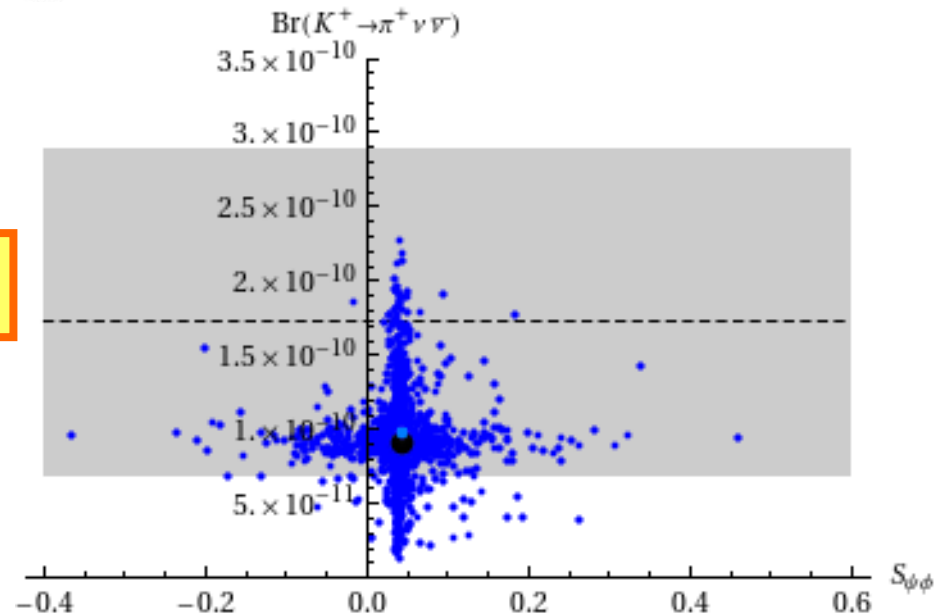
$$\mathbf{K^+ \rightarrow \pi^+ \nu \bar{\nu} \text{ vs. } S_{\psi\phi}}$$

**(Simultaneous Large Enhancements unlikely)**



**RS**

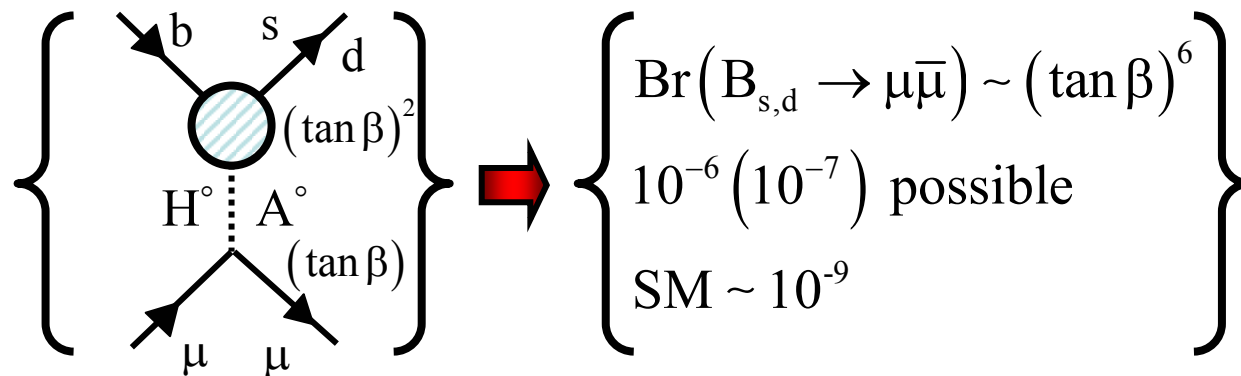
**LHT**



# $B_{s,d} \rightarrow \mu^+ \mu^-$ and MSSM with MFV at large $\tan\beta$

In MSSM at large  $\tan\beta$   
 (CKM still the only source of Flavour and CP Violation)

Strong Enhancement



Babu, Kolda  
 Chankowski, Slawianowska  
 Bobeth, Ewerth, Krüger, Urban  
 Huang, Liao, Yan, Zhu  
 Isidori, Retico  
 Dedes, Dreiner, Nierste  
 Dedes, Pilaftis  
 Chankowski, Rosiek  
 Foster, Okumura, Roszkowski  
 Carena et al.  
 Isidori, Paradisi

$\text{Br}(B_s \rightarrow \mu\bar{\mu}) < 6 \cdot 10^{-8}$

95% C.L.  
 (CDF, DØ)

$\text{Br}(B_d \rightarrow \mu\bar{\mu}) < 2 \cdot 10^{-8}$

95% C.L.

# $\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)$ vs $(\Delta M_s)^{\text{exp}} / (\Delta M_s)^{\text{SM}}$ in SUSY at Large $\tan \beta$

**AJB, Chankowski, Rosiek, Slawianowska (2002)**

**Gorbahn, Jäger, Nierste, Trine (2008)**

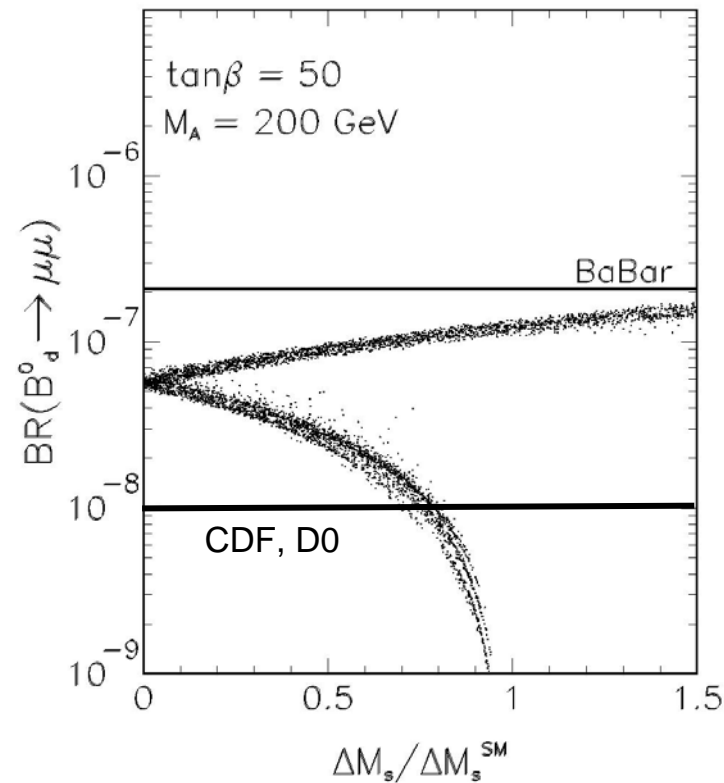
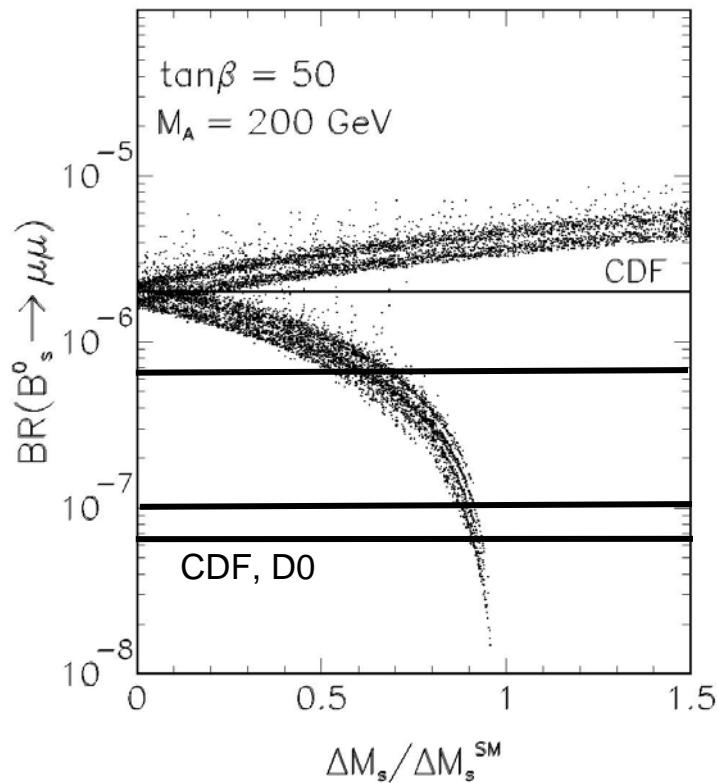
**Could be modified by Non-MFV (Chankowski; Dedes, Pilafitsis)**

**2002**

**2004**

**2007**

**2008**



**2002**

**2008**

$$\boxed{\mathbf{B}^+ \rightarrow \tau^+ \nu} \quad (\mu^+ \nu)$$

$$\mathbf{Br}(\mathbf{B}^+ \rightarrow \tau^+ \nu)_{\text{exp}} = (1.73 \pm 0.35) \cdot 10^{-4} \quad (\text{Belle, BaBar})$$

$$\mathbf{Br}(\mathbf{B}^+ \rightarrow \tau \nu)_{\text{SM}} \approx G_F^2 F_B^2 |V_{ub}|^2 = (1.1 \pm 0.5) \cdot 10^{-4}$$

$$\frac{\mathbf{Br}(\mathbf{B}^+ \rightarrow \tau \nu)_{\text{MSSM}}}{\mathbf{Br}(\mathbf{B}^+ \rightarrow \tau \nu)_{\text{SM}}} = \left[ 1 - \left( \frac{m_B}{m_{H^\pm}} \right)^2 \frac{\tan^2 \beta}{1 + \varepsilon_0 \tan \beta} \right]^2 \quad \begin{array}{l} (\text{Hou}) \\ (\text{Akeroyd, Recksiegel}) \\ (\text{Isidori, Paradisi}) \end{array}$$

This decay could be problematic for MSSM-MFV with large  $\tan\beta$

Tree-Level  
 $H^+$  exchange

Altmannshofer, AJB, Guadagnoli, Wick (07)

$$\mathbf{B^+ \rightarrow \tau^+ \nu, K^+ \rightarrow l^+ \nu}$$

(LFV effects in  
B and K Physics)

Sensitivity  
to NP

**A.**

$$\frac{\text{Br}(B^+ \rightarrow \mu^+ \nu)}{\text{Br}(B^+ \rightarrow \tau^+ \nu)}$$

(test of  $\mu \leftrightarrow \tau$  universality)

Isidori - Paradisi (2006)

**B.**

$$\frac{\Gamma(K^+ \rightarrow \mu^+ \nu)}{\Gamma(K^+ \rightarrow e^+ \nu)}$$

(test of  $\mu \leftrightarrow e$  universality)

Masiero, Paradisi, Petronzio (2005)

Very accurate  
precision test

Tested soon at CERN  
to 0.5%

TH:  
 $\pm 0.1\%$

$(g-2)_\mu$  and EDM's

Flavour  
Conserving



$(g-2)_\mu$  : Flavour and CP conserving

Resolution of the  
 $(g-2)_\mu$  problem

$$\left[ (g-2)_\mu \right]_{\text{SM}} \neq \left[ (g-2)_\mu \right]_{\text{exp}}$$

$$a_\mu^{\text{exp}} = 11659\ 2080\ (63)\ 10^{-11}$$

$$a_\mu^{\text{SM}} = 11659\ 1785\ (51)\ 10^{-11}$$

3.6  $\sigma$   
discrepancy

MSSM  
~~LHT~~



EDM's Flavour conserving but ~~CP~~

MSSM, ~~LHT~~, WED

But  $e^+e^-$  from  
BaBar  $\rightarrow$  0.9  $\sigma$

(?)

# Putting $S_0(10)$ -SUSY-GUT of Dermisek-Raby into difficulties

M. Albrecht, W. Altmannshofer, AJB, D. Guadagnoli, D. Straub

**1.** The Model gives a nice description of quark and lepton masses, PMNS and most of CKM elements.

Also  
SUSY  
Spectrum

**2.** But fails to describe simultaneously the data on

$$B_{s,d} \rightarrow \mu^+ \mu^-, B \rightarrow X_s \gamma, B \rightarrow X_s l^+ l^-, B_u \rightarrow \tau \nu$$

**3.** Gives  $|V_{ub}| \approx 3.2 \cdot 10^{-3}$

$$< \underbrace{(4.2 \pm 0.3) \cdot 10^{-3}}_{\text{Exp.}}$$

↑ Generally too low

Some recent solutions:  
Altmannshofer et al.

$$\mathbf{K^+ \rightarrow \pi^+ \nu\bar{\nu}, K_L \rightarrow \pi^0 \nu\bar{\nu}, K_L \rightarrow \pi^0 l^+ l^-, B \rightarrow K(K^*)}$$



### $Z^0$ - Penguin dominated Decays

Decay	SM	Exp	TH
$\mathbf{K^+ \rightarrow \pi^+ \nu\bar{\nu}}$	$(8.5 \pm 0.7) \cdot 10^{-11}$	$(17.3^{+11.5}_{-10.5}) \cdot 10^{-11}$ (BNL)	$\pm 2-3\%$
$\mathbf{K_L \rightarrow \pi^0 \nu\bar{\nu}}$	$(2.6 \pm 0.3) \cdot 10^{-11}$	$< 6.7 \cdot 10^{-8}$ (KEK)	$\pm 1-2\%$
$\mathbf{K_L \rightarrow \pi^0 e^+ e^-}$	$(3.5 \pm 1.0) \cdot 10^{-11}$	$< 28 \cdot 10^{-11}$ (KTeV)	$\pm 15\%$
$\mathbf{K_L \rightarrow \pi^0 \mu^+ \mu^-}$	$(1.4 \pm 0.3) \cdot 10^{-11}$	$< 38 \cdot 10^{-11}$ (KTeV)	$\pm 15\%$
$\mathbf{B \rightarrow K^+ \nu\bar{\nu}}$	$(4.5 \pm 0.7) \cdot 10^{-6}$	$< 14 \cdot 10^{-6}$ (Belle)	$\pm 15\%$
$\mathbf{B \rightarrow K^* \nu\bar{\nu}}$	$(6.8 \pm 1.1) \cdot 10^{-6}$	$< 80 \cdot 10^{-6}$ (BABAR)	$\pm 15\%$
$\mathbf{B \rightarrow X_S \nu\bar{\nu}}$	$(2.7 \pm 0.2) \cdot 10^{-5}$	$< 64 \cdot 10^{-5}$ (ALEPH)	$\pm 3\%$



# Very strong Constraints on New Physics

$$\text{Br}(\mathbf{B} \rightarrow \mathbf{X}_S \gamma)_{\text{exp}} = (3.52 \pm 0.24) \cdot 10^{-4}$$

$$\text{Br}(\mathbf{B} \rightarrow \mathbf{X}_S \gamma)_{\text{SM}} = \begin{cases} (3.15 \pm 0.23) \cdot 10^{-4} & \text{(Misiak et al)} \\ (2.98 \pm 0.26) \cdot 10^{-4} & \text{(Becher, Neubert)} \end{cases}$$

$$\text{Br}(\mathbf{B} \rightarrow \mathbf{X}_S \mathbf{l}^+ \mathbf{l}^-)_{\text{exp}} = \begin{cases} (1.6 \pm 0.5) \cdot 10^{-6} & \text{(low } q^2) \\ (4.4 \pm 1.3) \cdot 10^{-7} & \text{(high } q^2) \end{cases}$$

$$\text{Br}(\mathbf{B} \rightarrow \mathbf{X}_S \mathbf{l}^+ \mathbf{l}^-)_{\text{SM}} = \begin{cases} (1.6 \pm 0.1) \cdot 10^{-6} & \text{(low } q^2) \\ (2.3 \pm 0.8) \cdot 10^{-6} & \text{(high } q^2) \end{cases}$$

Isidori et al. (incl.)  
Gorbahn et al. (incl.)  
Feldmann et al. (excl.)

Zero in  $A_{\text{FB}}$

$$\hat{s}_0 = (3.50 \pm 0.12) \text{GeV}^2$$



TH  
very clean

$$A_{\text{CP}}(\mathbf{B} \rightarrow \mathbf{X}_S \gamma)_{\text{exp}} = 0.004 \pm 0.036$$

$$A_{\text{CP}}(\mathbf{B} \rightarrow \mathbf{X}_S \gamma)_{\text{SM}} = 0.004 \pm 0.002$$

All this can be improved  
at Super-B  
Super-Belle

(Still factor 10 enhancement possible !)

# FCNCs at Tree Level and $\Delta M_K$

$$\Delta M_K \cong 2 \cdot 10^{-7} \text{ GeV}$$

( $\epsilon_K$  even worse)

Disaster !!!  
Missed by  
8 orders of  
magnitude !!!

$= 0$

GIM Mechanism

(1971)

Gaillard + Lee (1974)

$$\Delta M_K \cong 2 \cdot 10^{-7} \left[ \frac{M_Z^2}{M_X^2} \right] \text{ GeV} = 3.5 \cdot 10^{-15} \text{ GeV}$$

New very heavy neutral boson !

$$\{ M_X \cong 10^6 \text{ GeV} \} \rightarrow$$

Testing  
 $10^{-22} \text{ m} !$

**Tree Level FCNC mediated by KK gauge bosons and Z (breakdown of standard GIM mechanism)**

**RS**

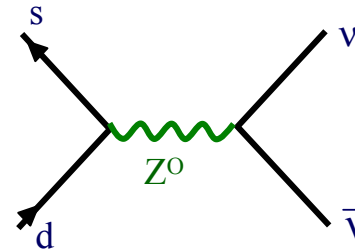
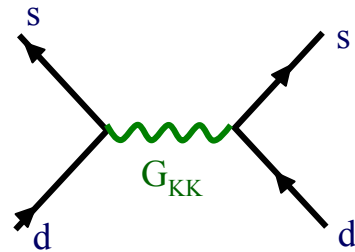
$$\mathbf{d} \equiv \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$\bar{\mathbf{d}} \mathbf{D}_L^+ \begin{pmatrix} \mathbf{a} \\ \mathbf{b} \\ \mathbf{c} \end{pmatrix} \mathbf{D}_L \gamma_\mu \mathbf{Z}^\mu \mathbf{d} \neq \bar{\mathbf{d}} \gamma_\mu \mathbf{Z}^\mu \mathbf{d}$$

**Related to the explanation of hierarchies in masses and mixings**

**(non-universality in gauge interactions)**

$$\mathbf{0} \left( \frac{v^2}{M_{KK}^2} \right)$$



$$\mathbf{0} \left( \frac{v^2}{M_{KK}^2} \right)$$

**But RS-GIM helps in avoiding disaster.**

**Gherghetta, Pomarol  
Huber, Shafi  
Agashe, Soni, Perez**

# Essential Ingredients in the Master Formula

**1.**

**Hadronic Matrix Elements ( $\hat{B}_i$ )**

(Progress still has to be made) Recent progress:  $\hat{B}_K$

**2.**

**QCD and QED RG-Effects for  $\mu < m_t$  ( $\eta_i^{\text{QCD}}$ )**

1990's - era of NLO calculations

2000's - era of NNLO calculations

★  $B \rightarrow X_s l^+ l^-$  (Greub et al; Isidori et al, Beneke et al)

★  $B \rightarrow X_s \gamma$  (Misiak et al) Bobeth et al)

★  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  (AJB, Gorbahn, Haisch, Nierste)

★ Non - Leptonic (Buchalla; Beneke, Jäger,...)

+ Semi - Leptonic (Gorbahn, Haisch)

3 Loop  $\hat{\gamma}_{\text{anom}}$

# Selected Actors for the next 15 Minutes

$|V_{ub}|, |V_{cb}|, \gamma$  from tree decays

$\epsilon_K$

$$K^+ \rightarrow \pi^+ \nu \bar{\nu}$$

$$K_L \rightarrow \pi^0 \nu \bar{\nu}$$

$$B_{s,d} \rightarrow \mu^+ \mu^-$$

$$S_{\psi\phi}, A_{SL}^s$$

$$\mu \rightarrow e\gamma, \tau \rightarrow \mu\gamma$$

$$d_n, d_e \text{ (EDM's)}$$



$$S_{\phi K_s}, (S_{\phi\phi})$$

$$\Delta(g-2)_\mu$$

$$A_{CP} (b \rightarrow s\gamma)$$

$$B \rightarrow K^* l^+ l^-$$



# 4th Generation

GIM at tree level  
but strongly broken  
at one loop  
 $m_t, m_b, >m_t \gg m_c$

Still a possibility !!

New activities:

George Hou at al.

Soni, Alok, Giri, Mohanda, Nandi (08)  
Bobrowski, Lenz, Riedl, Rohrwild (09)

This NP Scenario  
is very different  
from  
SUSY, LHT, RS

:

Non-Decoupling Effects  
of the 4th Generation  
Fermions in Low Energy  
Processes

However

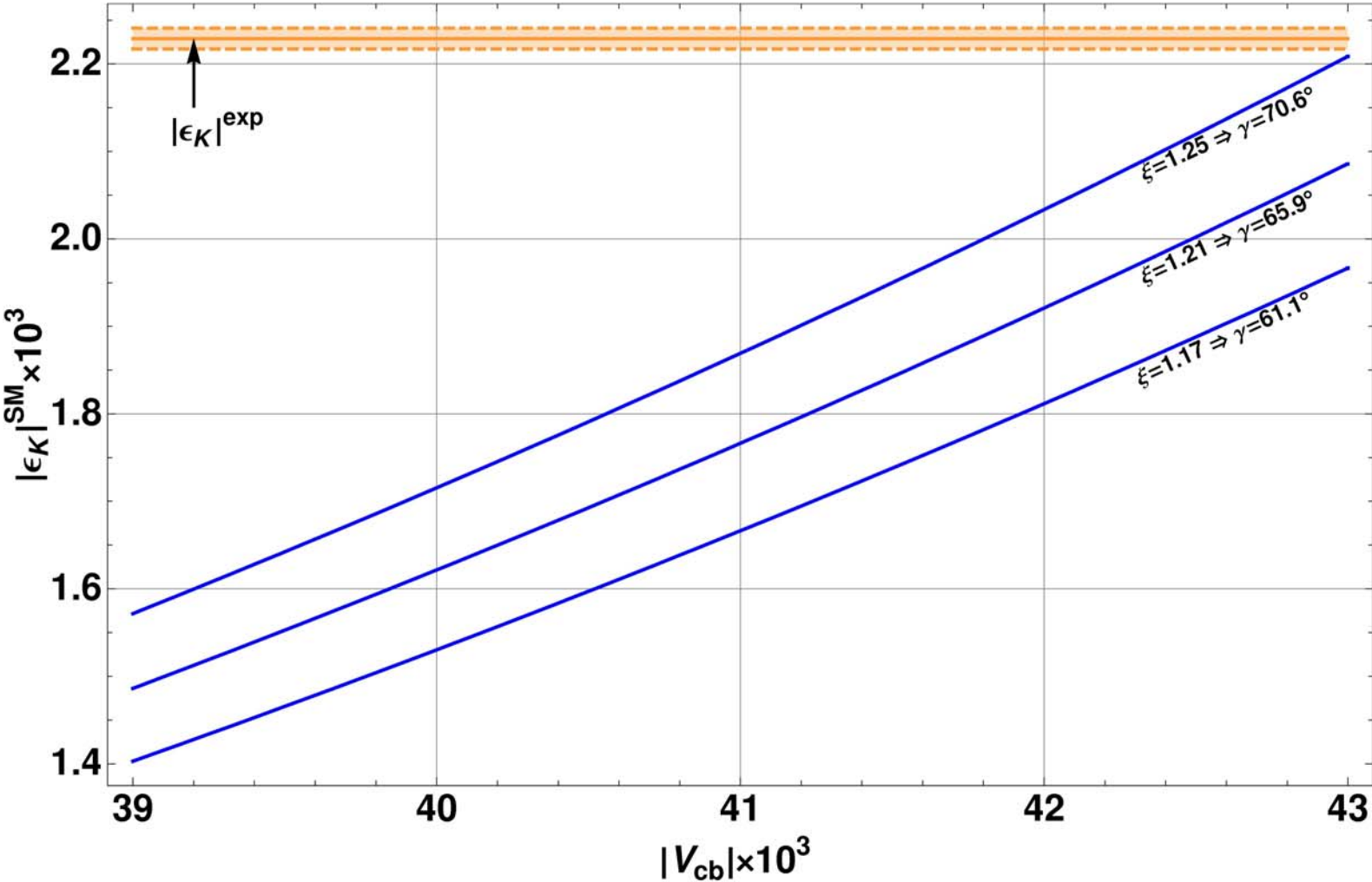
:

It does not address  
the hierarchy problems

$\epsilon_K$  needs precise value of  $|V_{cb}|$

AJB  
Guadagnoli  
(2009)

$\epsilon_K \sim |V_{cb}|^4$



# Number of new Flavour Parameters

(Quark Sector)

(physical)

**Real**

**$\mathcal{CP}$  Phases**

**SUSY**

**36**

**27**

**(R-parity)**

**FBMSSM**

**6**

**1**

**LHT**

**7**

**3**

**some  
sensitivity  
to UV**

**RS**

**18**

**9**

**SM**

**9**

**1**



## Where to Expect Large NP Effects

- 1.** LFV ( $\mu \rightarrow e\gamma$ ,  $\mu \rightarrow 3e$ ,  $\tau \rightarrow 3e$ ) ; EDM's
- 2.**  $K_L \rightarrow \pi^0 \nu \bar{\nu}$ ,  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ ,  $K_L \rightarrow \pi^0 I^+ I^-$ ,  $(\epsilon_K)$ ,  $\epsilon'/\epsilon$
- 3.** CP-Violation in  $B_s$ -Decays, in  $B \rightarrow X_d \gamma$
- 4.**  $B_{s,d} \rightarrow \mu^+ \mu^-$ , ( $B_{s,d} \rightarrow \tau^+ \nu$ )
- 5.** CP-Violation in D-Decays
- 6.**  $B \rightarrow X_s \nu \bar{\nu}$ ,  $B_{s,d} \rightarrow K^* I^+ I^-$
- 7.** CP-Violation in  $B_d$ ,  $B^\pm$  Decays  $(S_{\phi K_s}, S_{\pi^0 K_s}, \dots)$

# Other interesting Processes

- ◆  $\mu^- \rightarrow e^- e^+ e^-$ : even more constrained than  $\mu \rightarrow e \gamma$

$$Br(\mu^- \rightarrow e^- e^+ e^-)_{\text{exp}} < 1.0 \cdot 10^{-12}$$

[SINDRUM Collaboration]

- ◆  $\tau \rightarrow \mu \gamma$  and  $\tau \rightarrow e \gamma$ : similar to  $\mu \rightarrow e \gamma$

$$Br(\tau \rightarrow \mu \gamma)_{\text{exp}} < 1.6 \cdot 10^{-8}$$

[Belle, BaBar]

$$Br(\tau \rightarrow e \gamma)_{\text{exp}} < 9.4 \cdot 10^{-8}$$

[BaBar, Belle]

- ◆  $\tau \rightarrow \mu \pi$ : semileptonic decay

$$Br(\tau \rightarrow \mu \pi)_{\text{exp}} < 5.8 \cdot 10^{-8}$$

[Belle, BaBar]

(Future:  
Super B)

- ◆  $\mu \rightarrow e$  conversion

$$R(\mu T_i \rightarrow e T_i) < 4.3 \cdot 10^{-12}$$

$$10^{-18} \text{ (J-Parc)}$$

- ◆  $K_L \rightarrow \mu e$ : flavour violating in both quark and lepton sectors

$$Br(K_L \rightarrow \mu e)_{\text{exp}} < 4.7 \cdot 10^{-12}$$

[BNL E871 Collaboration]

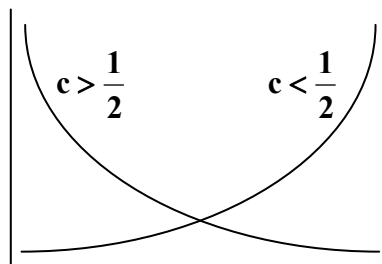
# Fermion Localisation and Yukawa Couplings

SM fermion (zero mode) shape function depends strongly on bulk mass parameter characteristic for a given fermion:

$$f^{(0)}(y, c) \propto e^{\left(\frac{1-c}{2}\right)y}$$

UV brane

IR brane



Higgs

$c > \frac{1}{2}$  : localisation near UV brane

$c < \frac{1}{2}$  : localisation near IR brane

effective 4D Yukawa couplings:

$$(Y_{u,d})_{ij} = (\lambda_{u,d})_{ij} f_i^Q f_j^{u,d}$$

- $\lambda_{u,d} \sim 0(1)$  anarchic complex 3 x 3 matrices  $\equiv Y_{5D}$
- hierachical structure of quark masses and CKM parameters can be naturally generated by exponential suppression of  $f^{Q,u,d}$  at IR brane.

**First look at  $\Delta F = 2$**

**: Burdman; Agashe, Perez, Soni**

**First more sophisticated analysis**

**: Csaki, Falkowski, Weiler (0804.1954)**

**Application of model-independent results of Ufit group to RS-type models.**

**Hierarchy of fermion masses and weak mixings solely due to geometry  
 $Y_{5D}$  anarchic and  $0(1)$**

**KK-Gluon  
→  
Contribution to  $\varepsilon_k$**

$$\mathbf{M_{KK} \gtrsim 21 \text{ TeV}}$$