

The Higgs boson



as a window to Beyond the Standard Model Physics

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I. what have we discovered so far ...

... and why we need an EWSB sector

The physics discovered so far can be powerfully classified according to a **gauge principle**, except for the terms responsible for the particles' masses

$$\mathcal{L}_{SM} = \mathcal{L}_0 + \mathcal{L}_{mass}$$

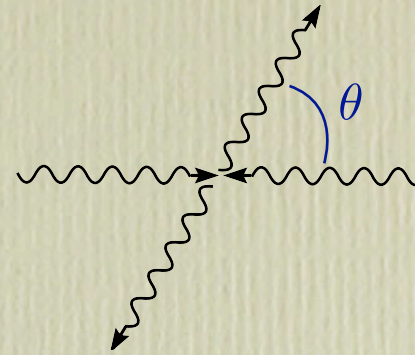
$$\mathcal{L}_0 = -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}W_{\mu\nu}^a W^{a\mu\nu} - \frac{1}{4}G_{\mu\nu}G^{\mu\nu} + \sum_{j=1}^3 \left(\bar{\Psi}_L^{(j)} i \not{D} \Psi_L^{(j)} + \bar{\Psi}_R^{(j)} i \not{D} \Psi_R^{(j)} \right)$$

$$\mathcal{L}_{mass} = M_W^2 W_\mu^+ W^{-\mu} + \frac{1}{2} M_Z^2 Z^\mu Z_\mu - \sum_{i,j} \left\{ \bar{u}_L^{(i)} M_{ij}^u u_R^{(j)} + \bar{d}_L^{(i)} M_{ij}^d d_R^{(j)} + \bar{e}_L^{(i)} M_{ij}^e e_R^{(j)} + \bar{\nu}_L^{(i)} M_{ij}^\nu \nu_R^{(j)} + h.c. \right\}$$

Mass terms are not invariant under the local $SU(2)_L \times U(1)_Y$ symmetry

Mass terms are responsible for the inconsistency of the theory at high energies:

The scattering of **longitudinal** W's and Z's violates unitarity at high energy



The optical theorem

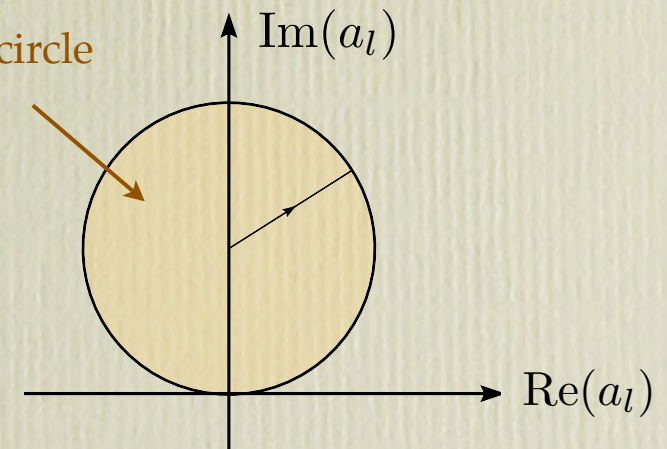
$$\frac{E}{p} \frac{1}{s} \text{Im} (A(\theta = 0)) = \sigma_{tot}(WW \rightarrow \text{anything})$$

requires for each partial wave:

$$\text{Im}(a_l(s)) = |a_l(s)|^2 + |a_l^{in}(s)|^2$$

$$\text{Re}(a_l(s)) \leq \frac{1}{2}$$

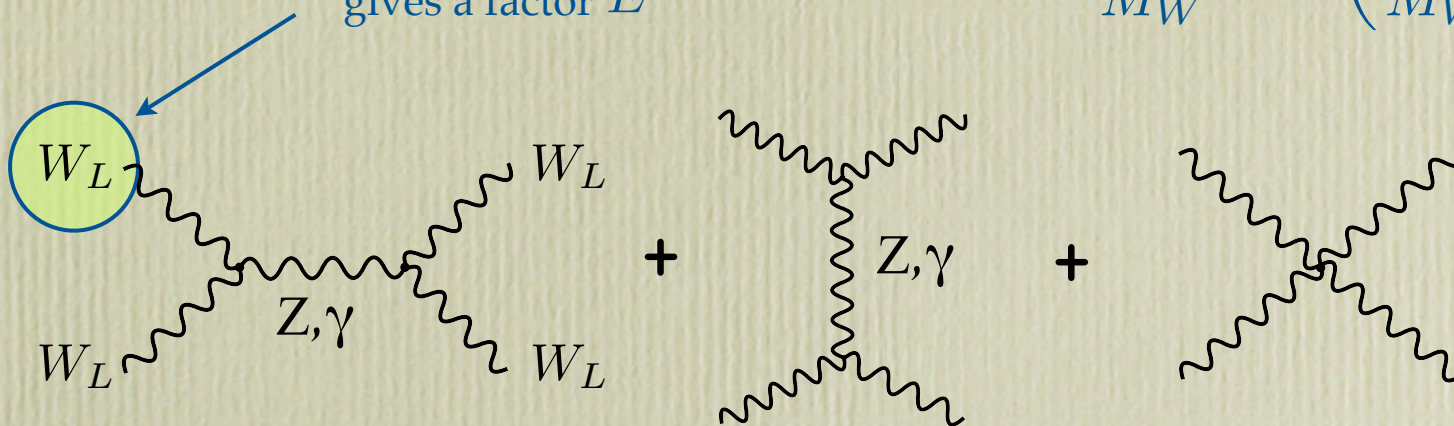
physical amplitudes bound
within the unitarity circle



The amplitude for scattering of **longitudinal** W's and Z's grows with the energy and eventually violates the unitarity bound:

Ex:
$$A(W_L^+ W_L^- \rightarrow W_L^+ W_L^-) = \frac{g_2^2}{4M_W^2} (s + t)$$

each longitudinal polarization gives a factor E
$$\epsilon_L^\mu = \frac{p^\mu}{M_W} + O\left(\frac{E}{M_W}\right)$$



Unitarity is violated at

$$\sqrt{s} \simeq \Lambda = 1.2 \text{ TeV}$$

The breaking of gauge invariance is in fact a fake: the symmetry is just **hidden**

$$\Sigma = \exp(i\sigma^a \chi^a / v)$$

$$D_\mu \Sigma = \partial_\mu \Sigma - ig_2 \frac{\sigma^a}{2} W_\mu^a \Sigma + ig_1 \Sigma \frac{\sigma_3}{2} B_\mu$$

$\rho = 1$ follows from a larger global $SU(2)_L \times SU(2)_R$ approximate invariance

$$\Sigma \rightarrow U_L \Sigma U_R^\dagger$$

broken only by g_1 and $\lambda^u \neq \lambda^d$

$$\mathcal{L}_{mass} = \frac{v^2}{4} \text{Tr} \left[(D_\mu \Sigma)^\dagger (D^\mu \Sigma) \right] - \frac{v}{\sqrt{2}} \sum_{i,j} (\bar{u}_L^{(i)} \bar{d}_L^{(i)}) \Sigma \begin{pmatrix} \lambda_{ij}^u u_R^{(j)} \\ \lambda_{ij}^d d_R^{(j)} \end{pmatrix} + h.c.$$

$$+ a v^2 \text{Tr} [\Sigma^\dagger D_\mu \Sigma T^3]^2$$

In fact, an additional term that breaks the LR symmetry has been omitted as $\rho_{exp} \simeq 1$

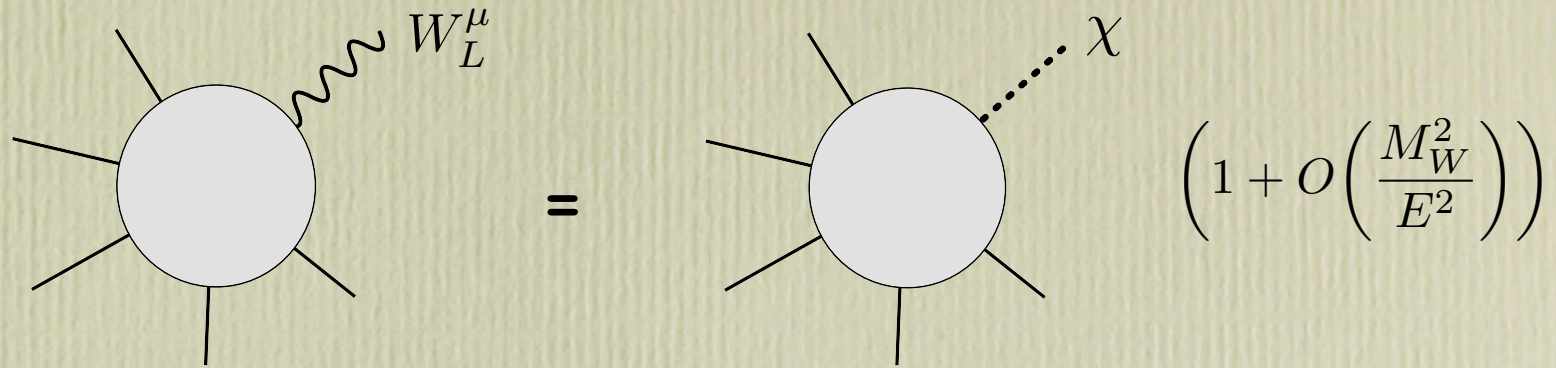
- The $SU(2)_L \times U(1)_Y$ symmetry is now manifest, although **non-linearly realized**

$$\Sigma \rightarrow U_L \Sigma U_Y^\dagger \quad U_L(x) = \exp(i\alpha_L^a(x)\sigma^a/2) \quad U_Y(x) = \exp(i\alpha_Y(x)\sigma^3/2)$$

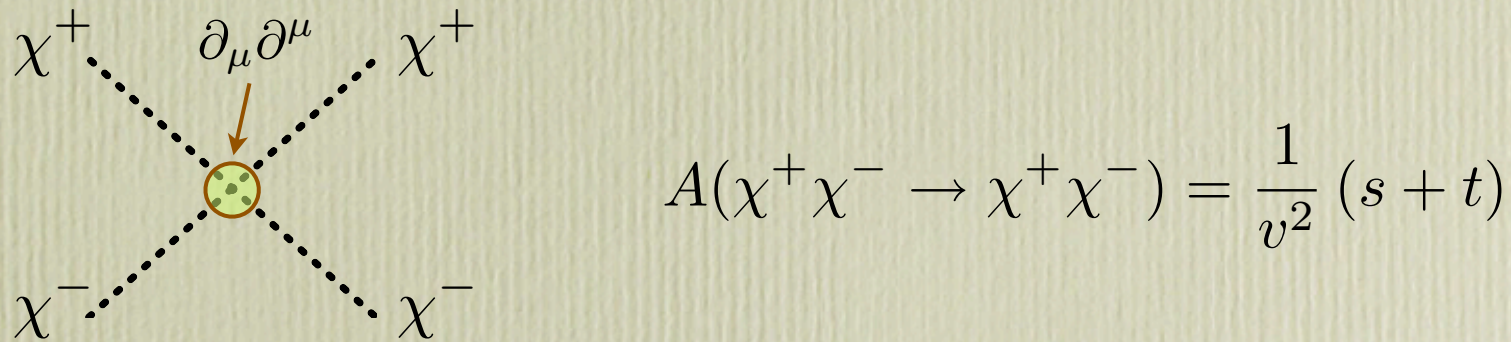
- In the unitary gauge $\langle \Sigma \rangle = 1$, \mathcal{L}_{mass} is equal to the original mass Lagrangian with

$$\rho \equiv \frac{M_W^2}{M_Z^2 \cos^2 \theta_W} = 1$$

Violation of unitarity, thanks to the **Equivalence Theorem**,



can be traced back to the scattering of the Goldstone bosons:



and it is linked to the **non-renormalizability** of the Lagrangian



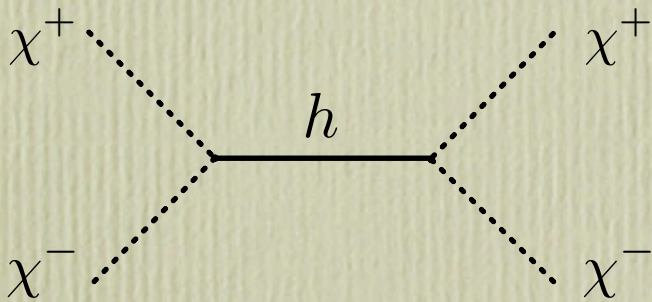
We need a new EWSB sector that acts as a UV completion of the EW chiral Lagrangian and restores unitarity

II. Restoring unitarity by adding
1 new field: the Higgs model

The most economical EWSB sector consists of 1 scalar field **singlet** under the $SU(2)_L \times SU(2)_R$ (and the local $SU(2)_L \times U(1)_Y$) symmetry :

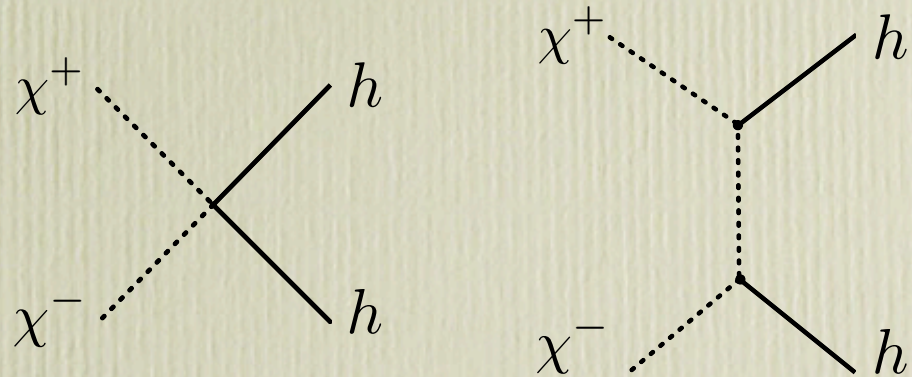
$$\mathcal{L}_{EWSB} = \frac{v^2}{4} \text{Tr} [D_\mu \Sigma^\dagger D^\mu \Sigma] + \underbrace{a}_{\substack{\text{a and b are free} \\ \text{parameters}}} \frac{v}{2} h \text{Tr} [D_\mu \Sigma^\dagger D^\mu \Sigma] + \underbrace{b}_{\substack{\text{a and b are free} \\ \text{parameters}}} \frac{1}{4} h^2 \text{Tr} [D_\mu \Sigma^\dagger D^\mu \Sigma] + V(h)$$

- For **a=1** the scalar exchange unitarizes the WW scattering



$$A(\chi^+ \chi^- \rightarrow \chi^+ \chi^-) = \frac{1}{v^2} \left[s - \frac{a s^2}{s - m_h^2} + (s \leftrightarrow t) \right]$$

- For **b=1** also the **inelastic** channels respect unitarity



$a=b=1$ defines the **Higgs Model**, whose Lagrangian can be rewritten in the standard form in terms of the $SU(2)_L$ doublet

$$H = \frac{1}{\sqrt{2}} e^{i\sigma^a \chi^a / v} \begin{pmatrix} 0 \\ v + h \end{pmatrix}$$

Unitarity of the Higgs Model can be traced back to its **renormalizability**

There is an unbroken custodial symmetry $SO(3)$ preserved by the Higgs vev that leads to $\rho = 1$

$$H = \begin{pmatrix} w_1 + i w_2 \\ w_3 + i w_4 \end{pmatrix} \quad H^\dagger H = \sum_i (w_i)^2$$

$V(H^\dagger H)$ is $SO(4) \sim SU(2)_L \times SU(2)_R$ invariant

$\langle H^\dagger H \rangle = v^2$ breaks $SO(4) \rightarrow SO(3)$

1. Unitarity bound on Higgs mass

$$A(W_L^+ W_L^- \rightarrow W_L^+ W_L^-) = -\frac{g_2^2 m_h^2}{4M_W^2} \left[\frac{s}{s - m_h^2} + \frac{t}{t - m_h^2} \right] \rightarrow -\frac{g_2^2 m_h^2}{4M_W^2}$$

Unitarity of WW scattering requires:

$$m_h \leq \sqrt{\frac{8\pi\sqrt{2}}{5G_F}} \simeq 780 \text{ GeV}$$

The heavier the Higgs is, the more strongly it couples $\lambda_4 = \frac{m_h^2}{2v^2}$

and the broader it is $\Gamma(h \rightarrow W^+ W^-) \simeq \frac{1}{16\pi} \frac{m_h^3}{v^2}$



As a general rule: the later unitarity is cured, the more strongly coupled the EWSB sector will be

2. Bounds on the Higgs mass through the quartic coupling

The physical Higgs mass is set by the quartic coupling, which is a **running** parameter

$$m_h^2 = 2\lambda_4 v^2$$

$$16\pi^2 \frac{d}{d \log Q} \lambda_4 = 24 \lambda_4^2 - (3g'^2 + 9g^2 - 12y_t^2) \lambda_4 + \frac{3}{8} g'^4 + \frac{3}{4} g'^2 g^2 + \frac{9}{8} g^4 - 6 y_t^4 + \dots$$

- For a **too heavy** Higgs, the first term dominates and drives λ_4 to a Landau pole at large energy scales

TRIVIALITY BOUND

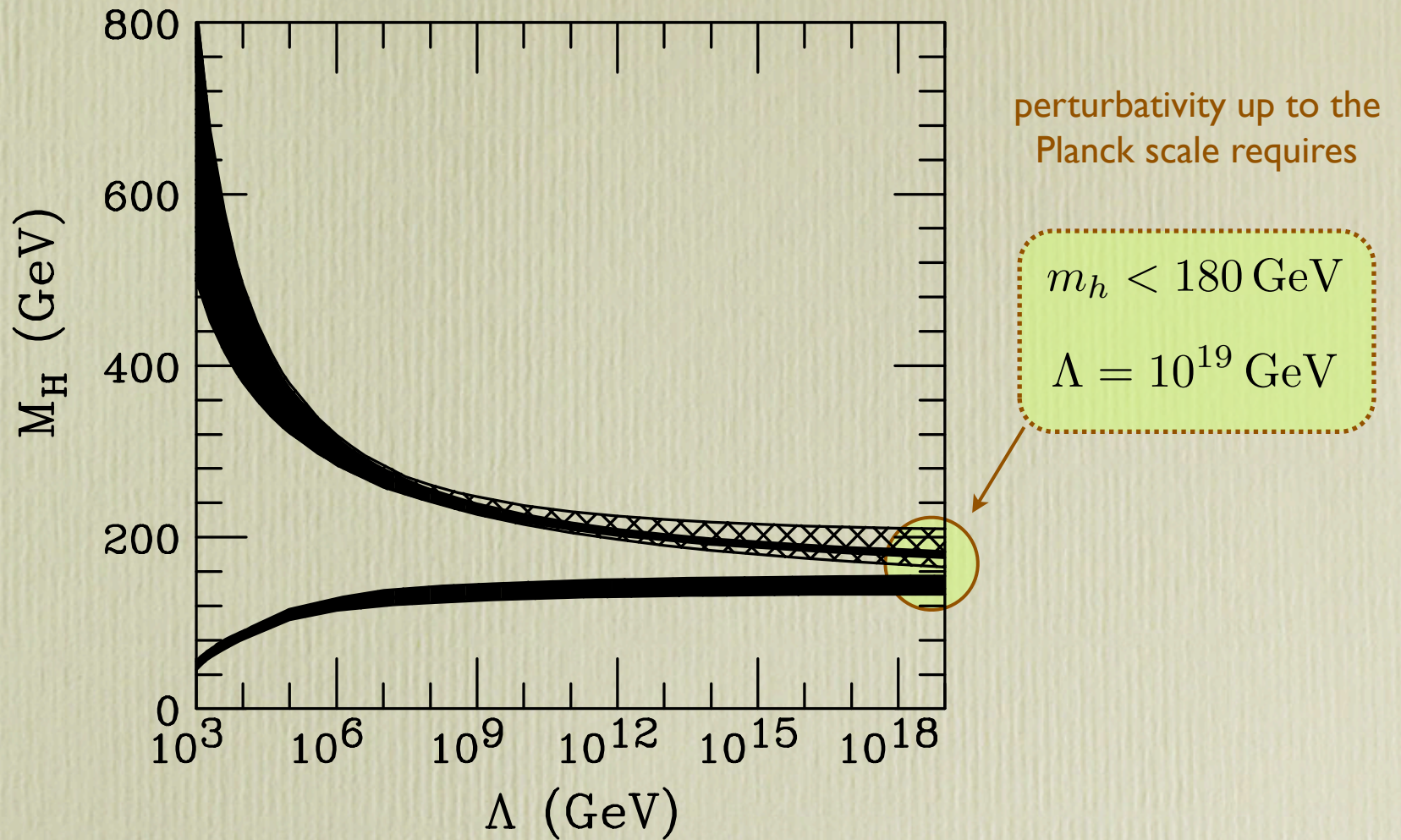
$$m_h^2 \lesssim \frac{4\pi^2 v^2}{3 \log(\Lambda/v)}$$

largest scale of validity of the theory (cutoff scale)

- For a **too small** Higgs, the last term dominates and drives λ_4 negative at large energy scales

VACUUM STABILITY BOUND

$$m_h^2 \gtrsim \frac{3y_t^4 v^2}{4\pi^2} \log(\Lambda/v)$$



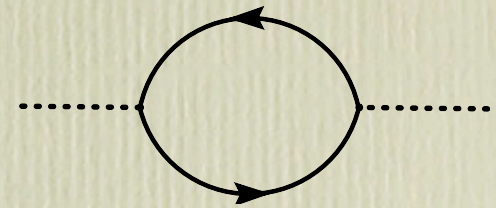
from: T. Hambye, K. Riesselmann Phys Rev, D55 (1997) 7255

3. UV instability of the Higgs mass term

[aka: the Hierarchy Problem]

The Higgs mass term receives **quadratically divergent** corrections from SM loops, making the physical mass highly sensitive to the value of the cutoff scale:

$$\delta m_h^2 = \left[6 y_t^2 - \frac{3}{4} (3 g_2^2 + g_1^2) - 6 \lambda_4 \right] \frac{\Lambda^2}{8\pi^2}$$



The larger Λ , the less natural a light Higgs is

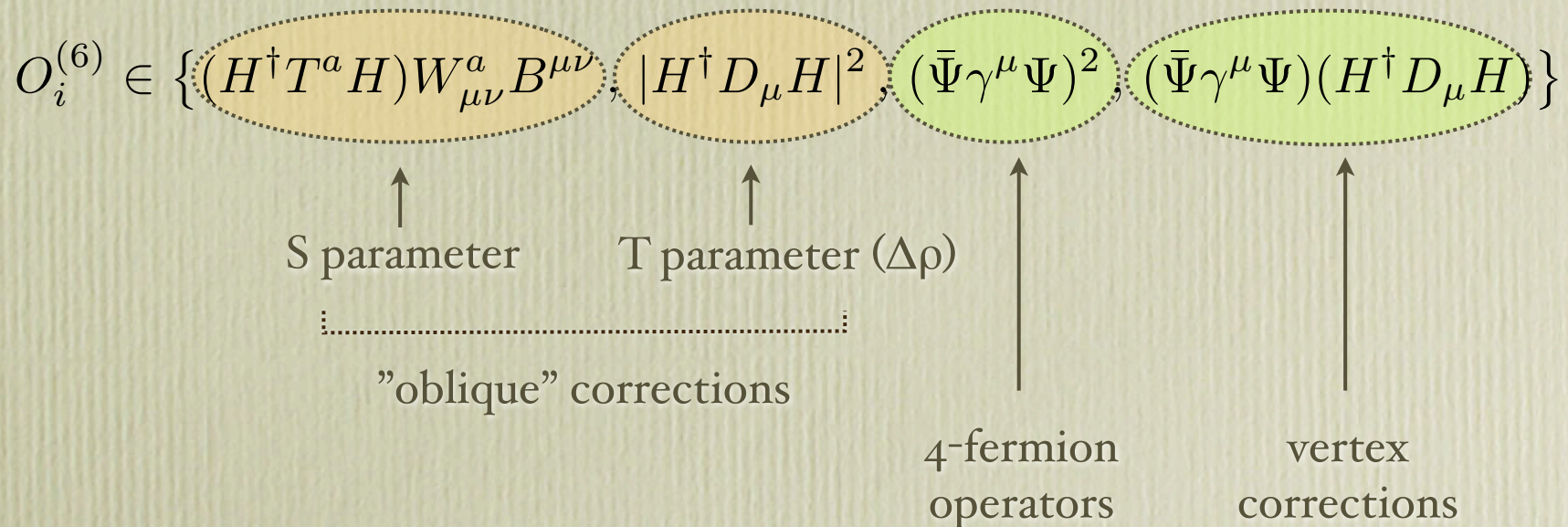


The cutoff might be low: the Higgs model should be perhaps regarded as a **parameterization** rather than a dynamical explanation of EWBSB

3. LEP constraints on m_h and Λ

If the Higgs model is considered as an effective field theory, New Physics effects are encoded in **higher order** (non-renormalizable) **operators** :

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{i,p} \frac{c_i}{\Lambda^p} O_i^{(4+p)}$$



Notice: those above are flavor and CP-conserving operators

The EW precision measurements performed at LEP, SLD and Tevatron

| | |
|--------------------------------|---|
| Γ_Z | total Z width |
| σ_h | $e\bar{e}$ hadronic cross section at Z peak |
| R_h | $\Gamma(Z \rightarrow \text{hadrons})/\Gamma(Z \rightarrow \mu^+\mu^-)$ |
| R_b | $\Gamma(Z \rightarrow b\bar{b})/\Gamma(Z \rightarrow \text{hadrons})$ |
| R_c | $\Gamma(Z \rightarrow c\bar{c})/\Gamma(Z \rightarrow \text{hadrons})$ |
| A_P^τ | τ polarization asymmetry |
| A_{LR}^e | Left/Right asymmetry in $e\bar{e}$ |
| A_{LR}^b | LR Forward/Backward asymmetry in $e\bar{e} \rightarrow b\bar{b}$ |
| A_{LR}^c | LR FB asymmetry in $e\bar{e} \rightarrow c\bar{c}$ |
| A_{FB}^ℓ | Forward/Backward asymmetry in $e\bar{e} \rightarrow \ell\bar{\ell}$ |
| A_{FB}^b | Forward/Backward asymmetry in $e\bar{e} \rightarrow b\bar{b}$ |
| A_{FB}^c | Forward/Backward asymmetry in $e\bar{e} \rightarrow c\bar{c}$ |
| M_Z | pole Z mass |
| G_F | Fermi constant for μ decay |
| m_t | pole top mass |
| M_W | pole W mass |
| $\alpha_s(M_Z)$ | strong coupling |
| $\alpha_{\text{em}}^{-1}(M_Z)$ | electromagnetic coupling |

can be used to test the Higgs Model and put constraints on m_h and Λ

Global fit to the Higgs Model

[from the LEP EWWG]

The dependence upon the Higgs mass is **logarithmic** and comes in through loop effects

On the whole the Standard Model performs rather well, with a clear indication for a **light Higgs**

$$m_h \lesssim 154 \text{ GeV} \quad @ \text{ 95\% CL}$$

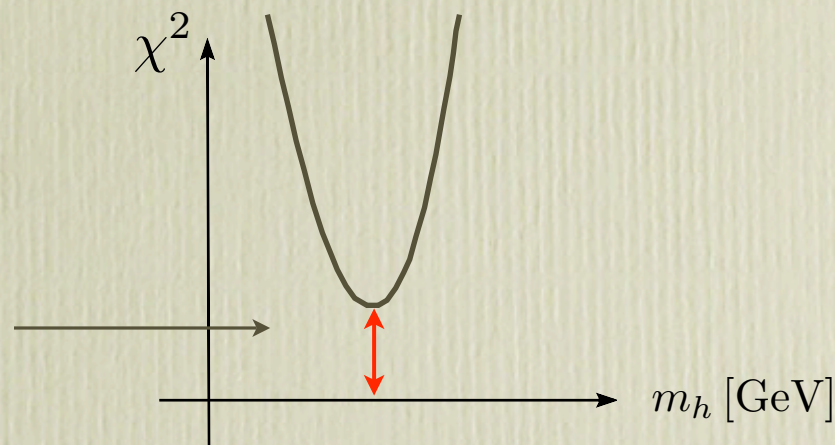
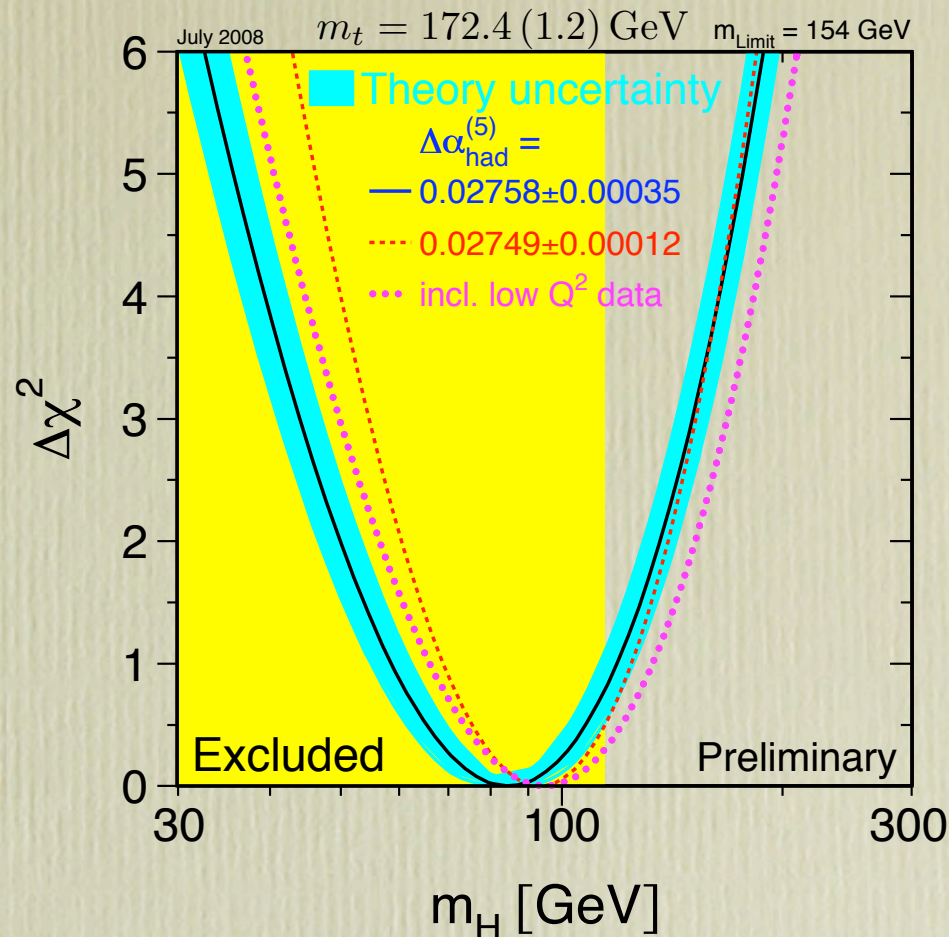
yet the fit is **not** entirely satisfactory:

P~4.5%

$$\frac{\chi_{min}^2}{ndf} (all) = \frac{28.0}{17}$$

P~15%

$$\frac{\chi_{min}^2}{ndf} (only - high) = \frac{18.2}{13}$$

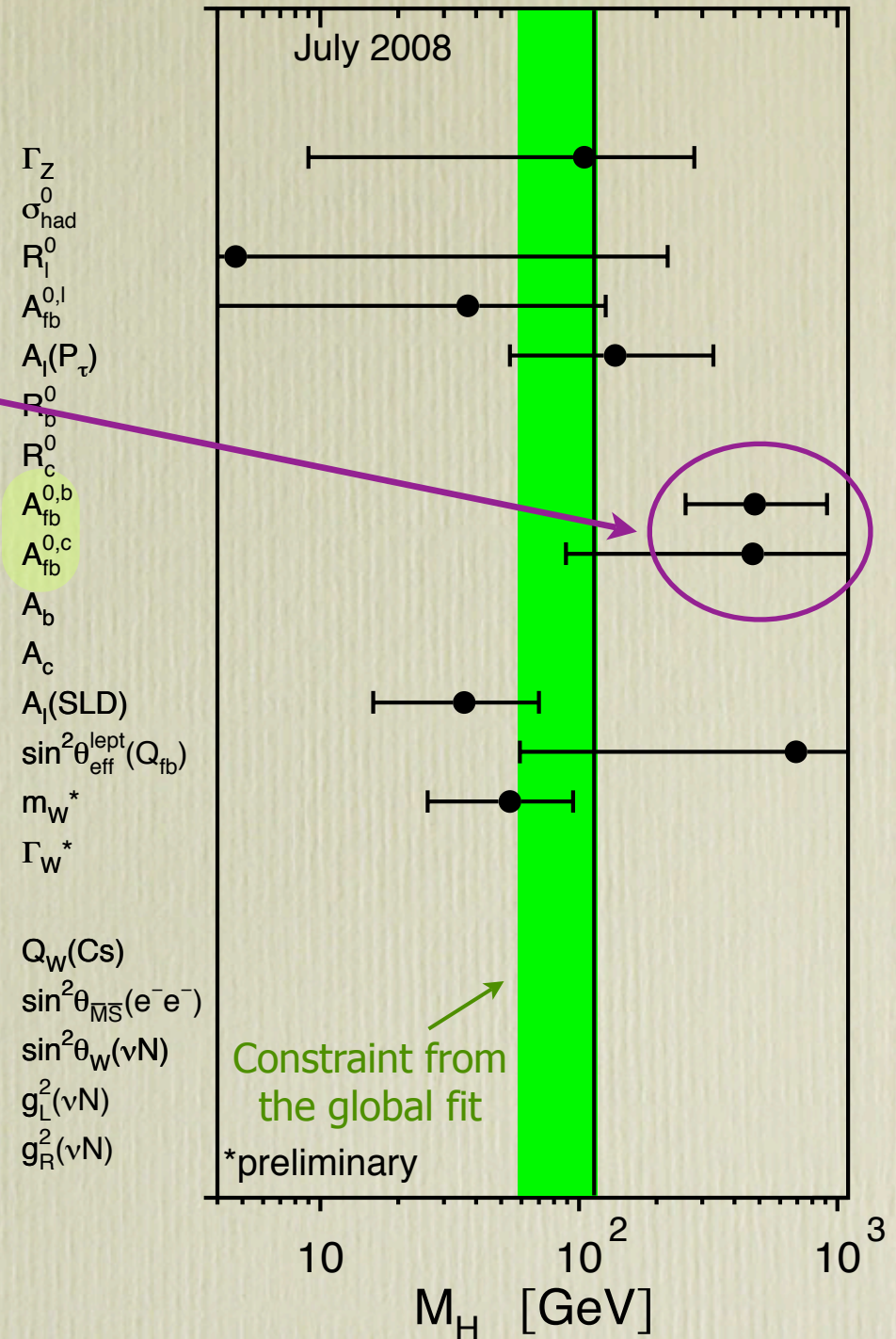


Best fit $m_h = 87_{-27}^{+36}$ GeV is the result of a **tension**
between leptonic and hadronic asymmetries

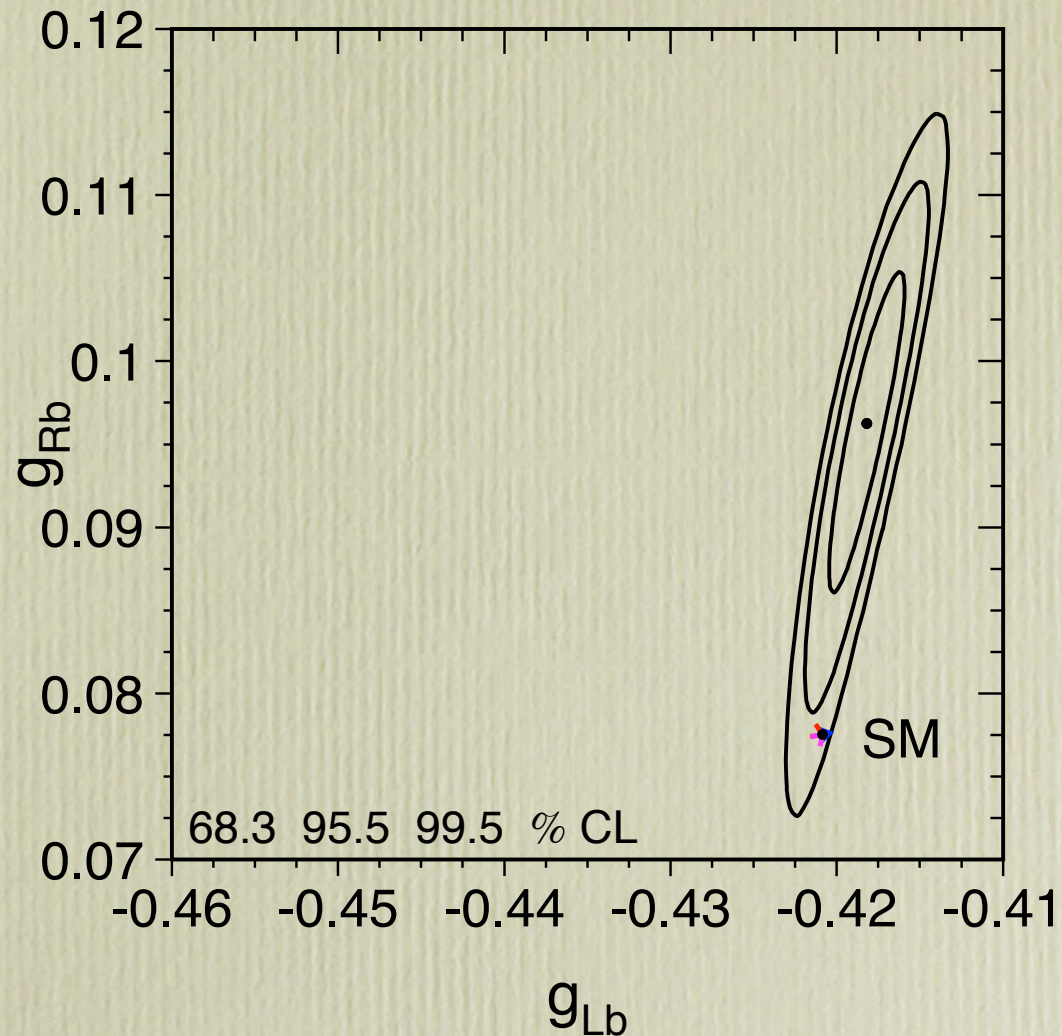
Only the hadronic asymmetries
(and the NuTeV result) push
for a high Higgs mass

removing $A_{fb}^{0,b}$ from the fit
gives a better χ^2 but also :

$$m_h = 55_{-20}^{+30} \text{ GeV}$$



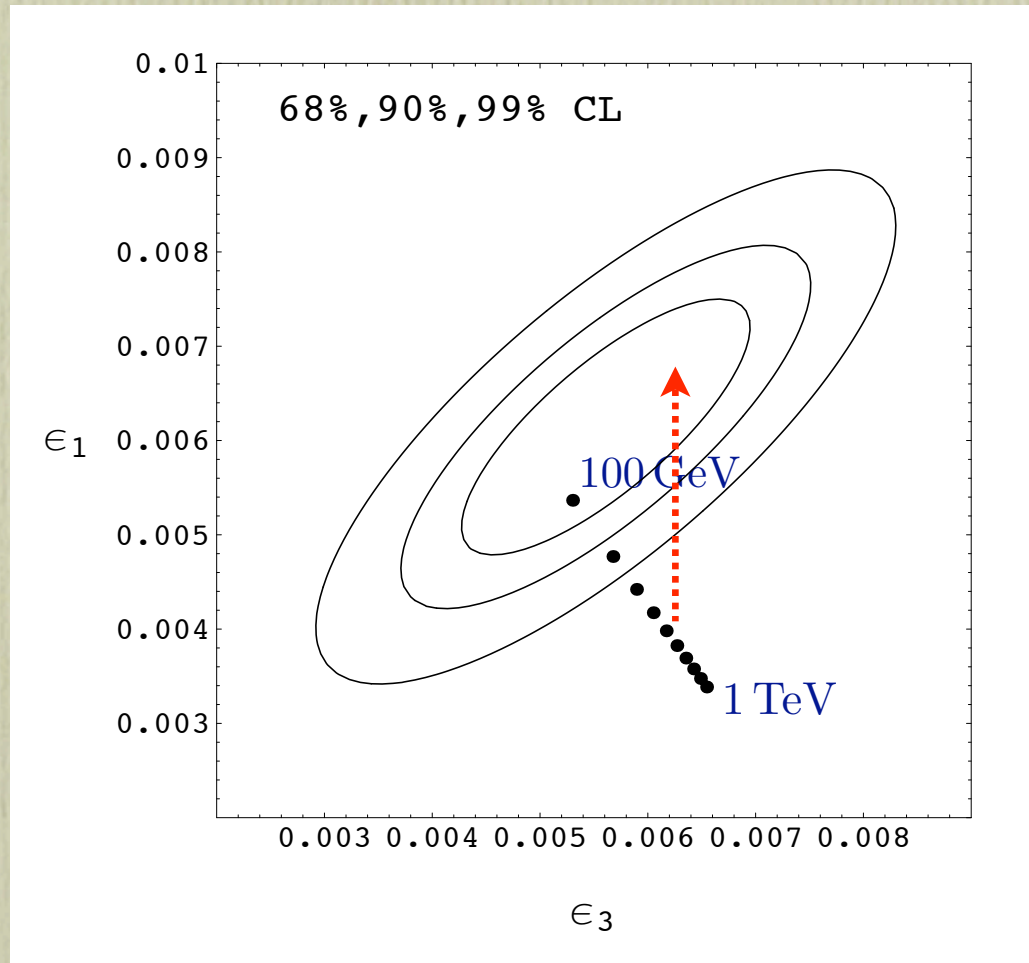
The fit improves allowing for a (large) δg_{Rb} from New Physics



However: very few examples of New Physics leading to a large δg_{Rb} and very small positive δg_{Lb}

Moral:

The Higgs boson is **light**, unless New Physics is of a very special kind



If the Higgs is light:

bound on each individual coefficient is **strong**

[LEP “paradox”]

| Dimensions six operators | $m_h = 115 \text{ GeV}$ | |
|---|-------------------------|------------|
| | $c_i = -1$ | $c_i = +1$ |
| $\mathcal{O}_{WB} = (H^\dagger \tau^a H) W_{\mu\nu}^a B_{\mu\nu}$ | 9.7 | 10 |
| $\mathcal{O}_H = H^\dagger D_\mu H ^2$ | 4.6 | 5.6 |
| $\mathcal{O}_{LL} = \frac{1}{2} (\bar{L} \gamma_\mu \tau^a L)^2$ | 7.9 | 6.1 |
| $\mathcal{O}'_{HL} = i(H^\dagger D_\mu \tau^a H) (\bar{L} \gamma_\mu \tau^a L)$ | 8.4 | 8.8 |
| $\mathcal{O}'_{HQ} = i(H^\dagger D_\mu \tau^a H) (\bar{Q} \gamma_\mu \tau^a Q)$ | 6.6 | 6.8 |
| $\mathcal{O}_{HL} = i(H^\dagger D_\mu H) (\bar{L} \gamma_\mu L)$ | 7.3 | 9.2 |
| $\mathcal{O}_{HQ} = i(H^\dagger D_\mu H) (\bar{Q} \gamma_\mu Q)$ | 5.8 | 3.4 |
| $\mathcal{O}_{HE} = i(H^\dagger D_\mu H) (\bar{E} \gamma_\mu E)$ | 8.2 | 7.7 |
| $\mathcal{O}_{HU} = i(H^\dagger D_\mu H) (\bar{U} \gamma_\mu U)$ | 2.4 | 3.3 |
| $\mathcal{O}_{HD} = i(H^\dagger D_\mu H) (\bar{D} \gamma_\mu D)$ | 2.1 | 2.5 |



Possible conclusions:

1. more than one operator contribute
2. coefficients c_i are small (= New Physics is weakly coupled)

III. Curing the UV sensitivity of the Higgs model

Fact:

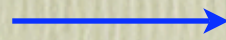
mass of fermions and gauge bosons are UV-stable
because protected by a **symmetry**

Strategy:

relating the Higgs to fermions or gauge fields
to gain the symmetry protection

CHIRAL SYMMETRY

(fermion protection)

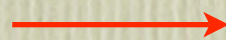


SUSY

$$h \subset \begin{pmatrix} \tilde{h} \\ h \end{pmatrix}$$

GAUGE SYMMETRY

(gauge protection)



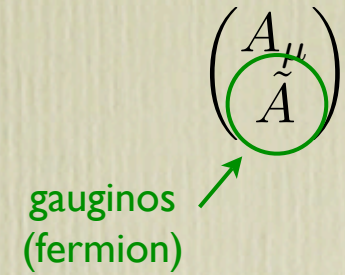
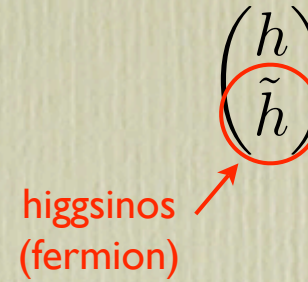
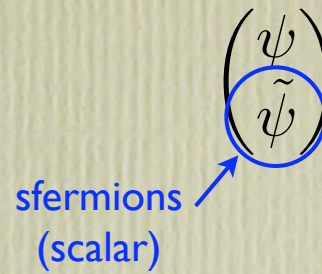
GAUGE-HIGGS
UNIFICATION

$$h = A_5$$

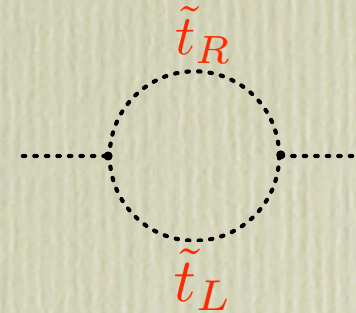
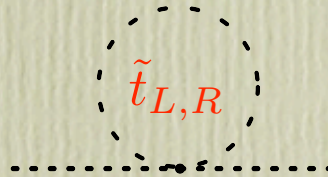
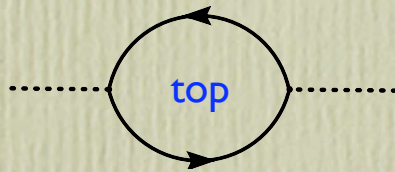
[requires extra dimensions]

SUSY in a nutshell:

- each SM particle has a superpartner with opposite statistics



- UV instability canceled by the superpartners



- internal consistency + anomaly cancellation require 2 Higgs doublets

h comes along with: H^\pm, H, A

- dynamical explanation for EWSB: m_H^2 driven negative by top loops via RG evolution

- Higgs **must** be **light**:

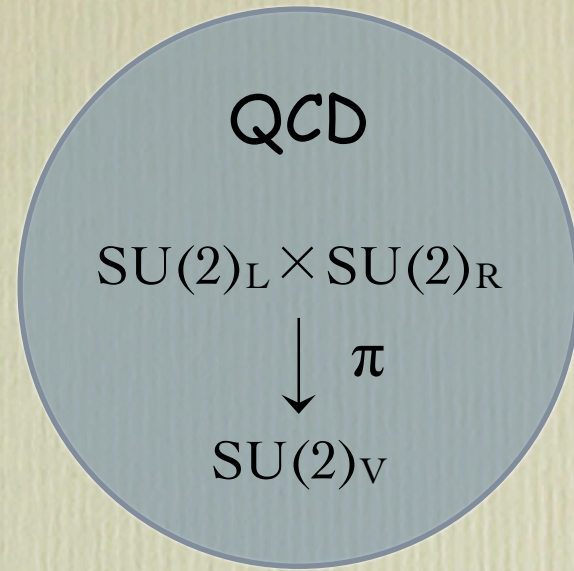
$$m_h^2 \simeq M_Z^2 \cos^2 2\beta + \frac{N_c}{2\pi^2} \frac{m_t^4}{v^2} \log \left(\frac{\tilde{m}_t^2}{m_t^2} \right)^2$$

$$m_h \lesssim 135 \text{ GeV}$$

IV. Restoring unitarity by adding
an infinite number of new states

The QCD analogy:

QCD is a remarkable example of a (strongly-interacting) sector which leads to a chiral Lagrangian in the low-energy limit



- For $m_q=0$ QCD with 2 flavors has an $SU(2)_L \times SU(2)_R$ invariance
- $SU(2)_L \times SU(2)_R$ spontaneously broken to $SU(2)_V$ at low energy by the $\langle \bar{q}q \rangle$ condensate
- the three pions π^a are the composite Goldstone bosons of the chiral symmetry breaking

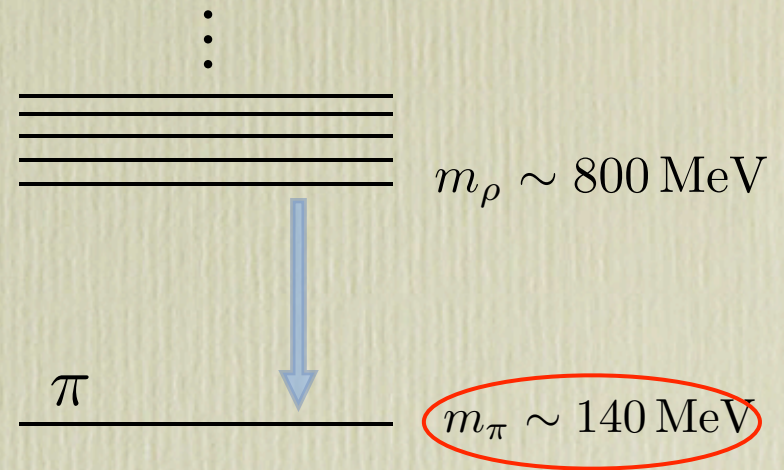
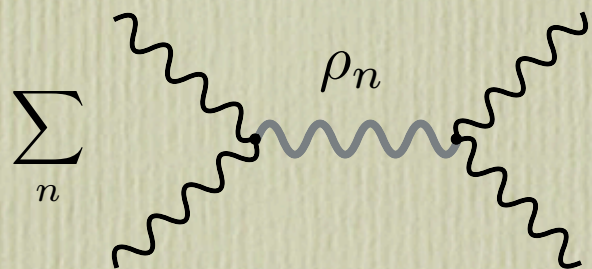
$$\mathcal{L}_{QCD} = \sum_{q=u,d} \bar{q} \gamma^\mu (i\partial_\mu - g_3 \lambda^a G_\mu^a) q$$



$$\mathcal{L}_\chi = \frac{f_\pi^2}{4} \text{Tr} [\partial_\mu \Sigma^\dagger \partial^\mu \Sigma]$$

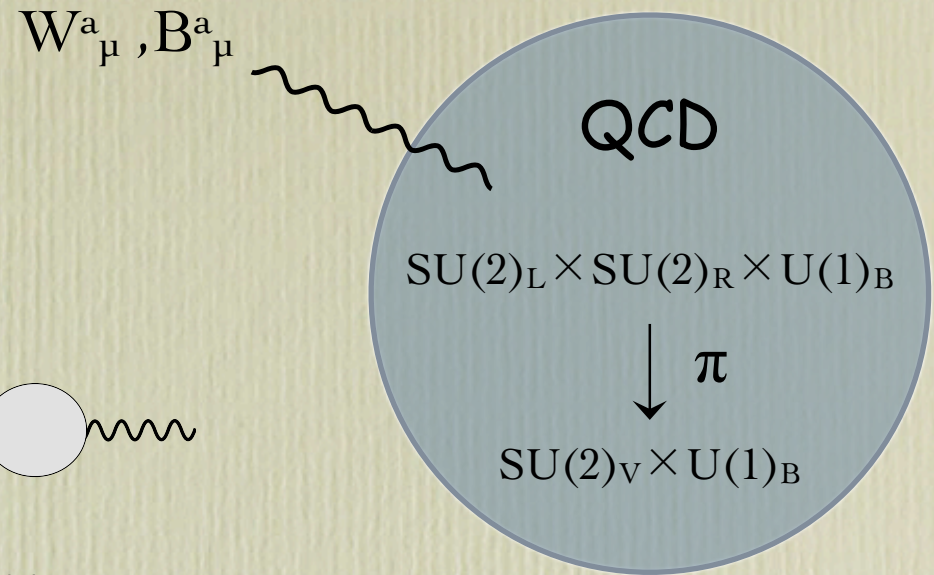
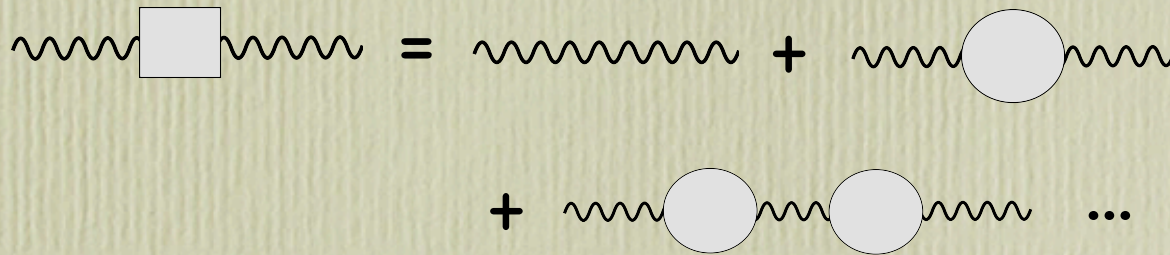
$$\Sigma(x) = e^{i\sigma^a \pi^a(x)/f_\pi} \quad f_\pi = 92 \text{ MeV}$$

Unitarity of $\pi\pi$ scattering is enforced by the contribution of the heavier vector and axial resonances :



the pion lighter because
is a (pseudo)-Goldstone

After turning on the $SU(2)_L \times U(1)_Y$ gauging, the pions are in fact eaten to give mass to the W and Z:



$$G^{\mu\nu}(q) = \frac{-i}{q^2} \frac{1}{1 - g_2^2 \Pi(q^2)} \left(\eta^{\mu\nu} - \frac{q^\mu q^\nu}{q^2} \right)$$

✓ $U(1)_Q$ unbroken: massless photon

✓ custodial symmetry $\Rightarrow \rho=1$

$$i\Pi^{\mu\nu}(q) = - \int d^4q e^{-iqx} \langle T \{ J^\mu(x) J^\nu(0) \} \rangle$$

☹ Problems:

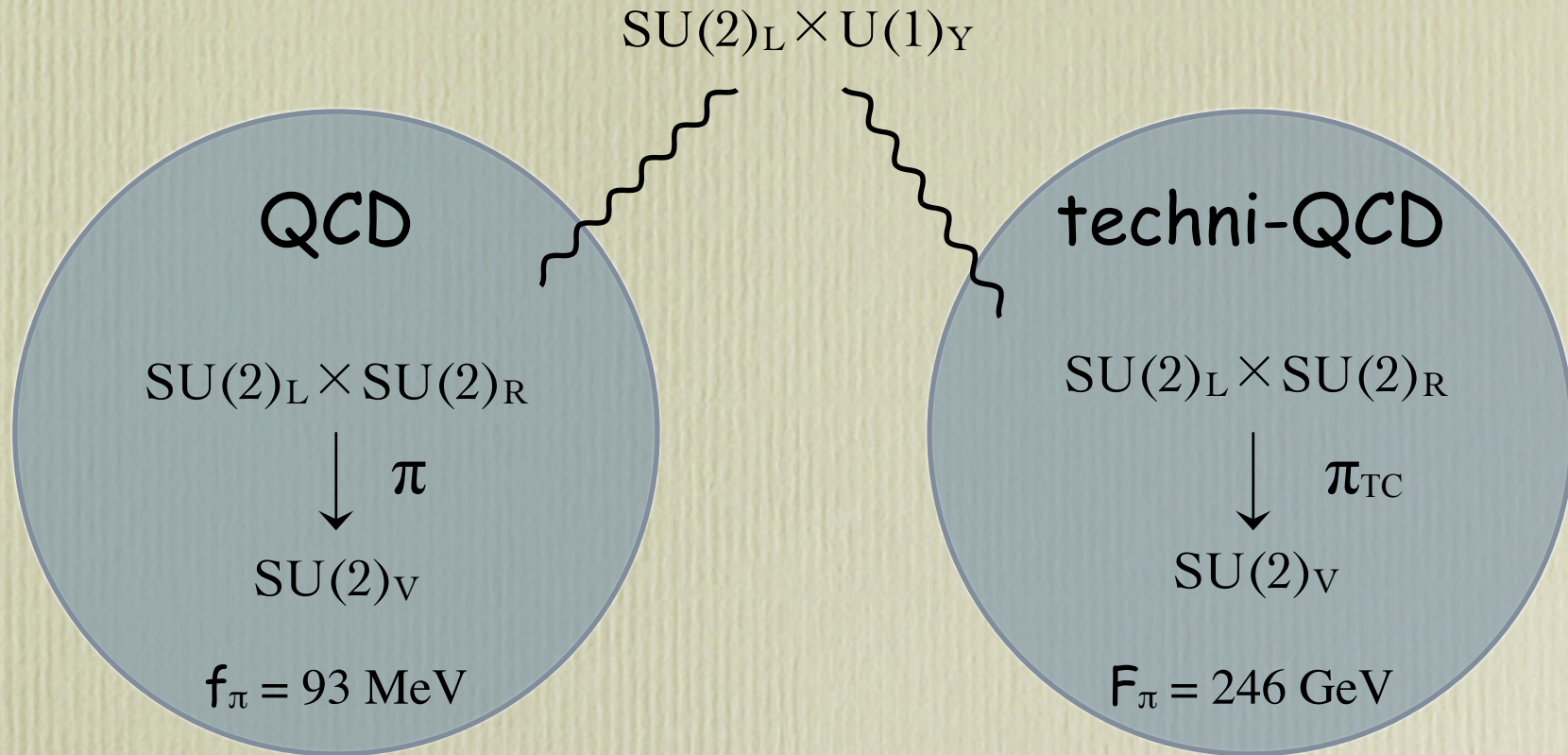
$$\Pi^{\mu\nu}(q) = \Pi(q^2) (q^2 \eta^{\mu\nu} - q^\mu q^\nu)$$

1) $f_\pi = 92 \text{ MeV} \Rightarrow M_W = g f_\pi / 2 = 30 \text{ MeV} !$

2) we do observe the pions !

The technicolor paradigm:

[Weinberg, Susskind]



✓ $F_{\pi} \gg f_{\pi} \Rightarrow$

1) $W_{\text{long}}, Z_{\text{long}}$ mostly from π_{TC} : $M_W \simeq g F_{\pi} / 2 = 80 \text{ GeV}$

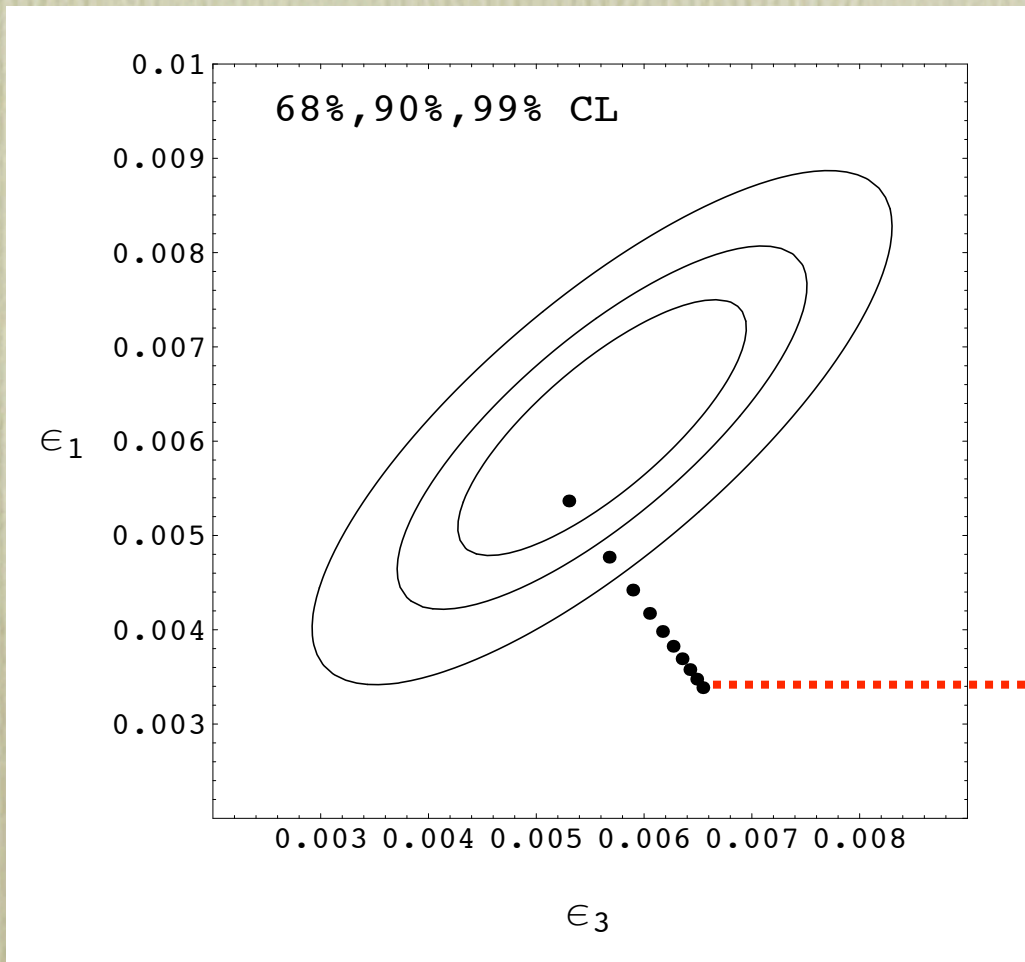
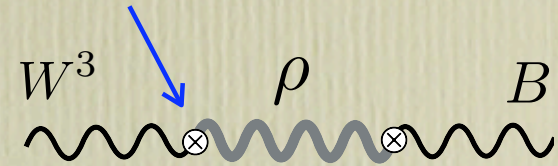
2) still a physical pion in the spectrum, mostly π

Naive Technicolor does not work

Large corrections to the S parameter

$$\Delta\mathcal{L} = \frac{S}{32\pi} W_{\mu\nu}^3 B_{\mu\nu} \quad S \sim 16\pi \left(\frac{v}{m_\rho} \right)^2 \sim \frac{N}{\pi}$$

$$\langle 0 | J_\mu | \rho \rangle = \epsilon_\mu^r f_\rho m_\rho$$



naive estimate for a scaled-up
QCD-like dynamics

👉 A possible solution to the EWPT problem:

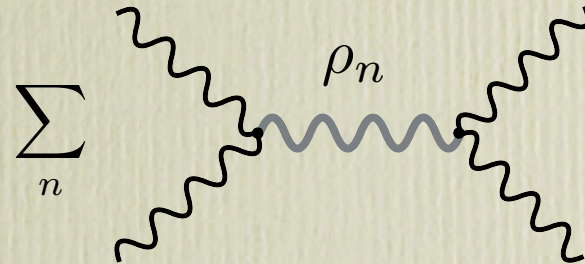
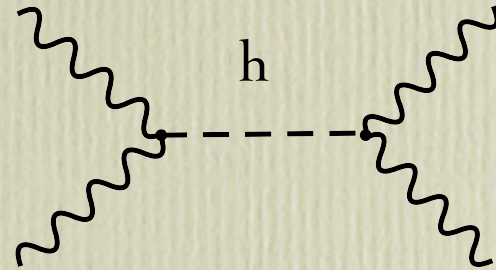
suppose the strong dynamics has also a light scalar bound state playing the role of the Higgs

the composite Higgs partially unitarize

the WW scattering until a scale $\Lambda' = \frac{\Lambda}{\sqrt{\xi}}$

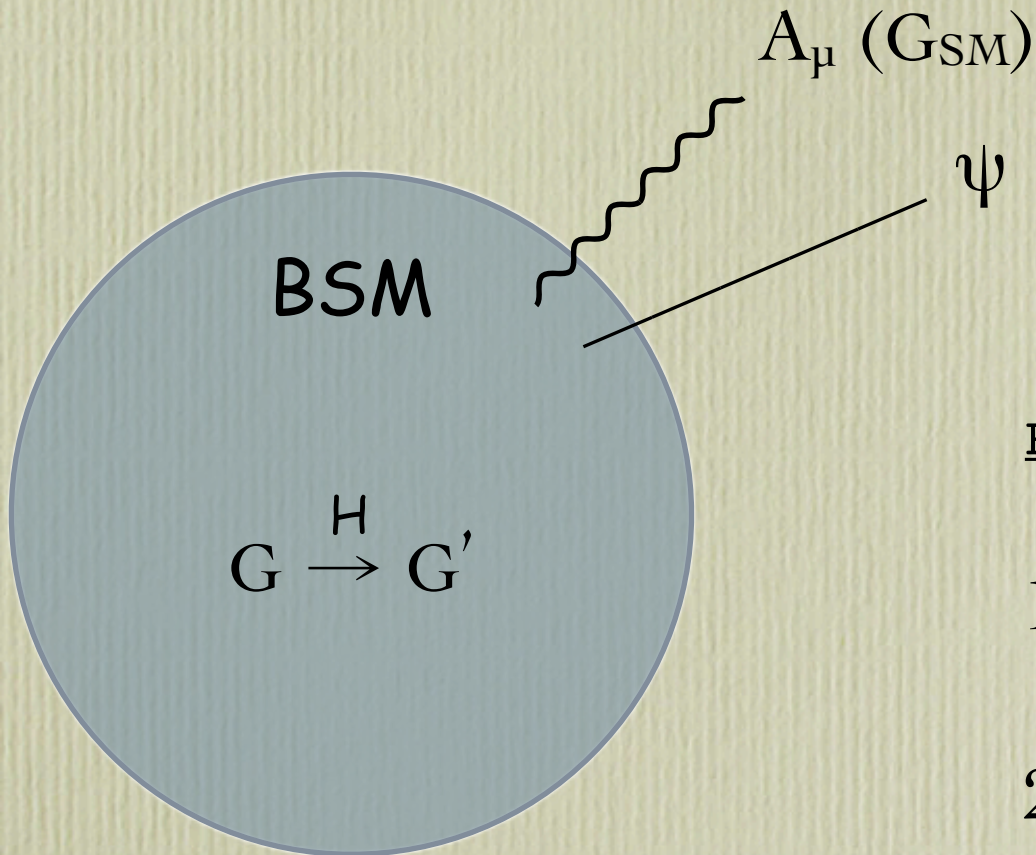
$$g_{hWW} = g_{hWW}^{SM}(1 + O(\xi))$$

... until the vector resonances take on



Composite Higgs models

[Georgi & Kaplan, '80s]



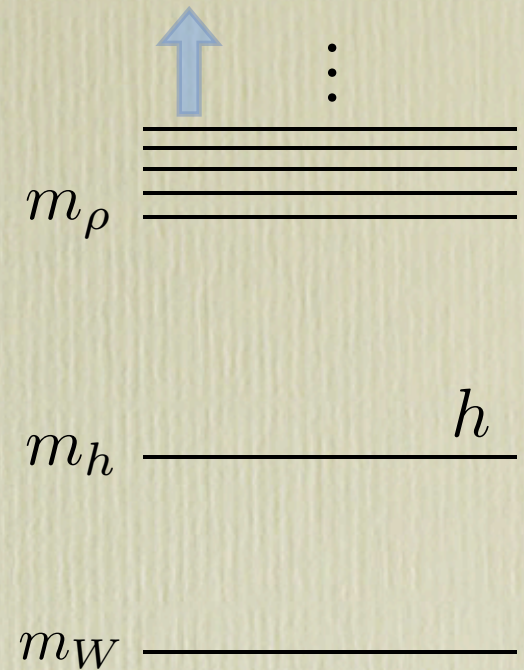
Requirements:

1) $G_{SM} \subset G'$

2) H is a doublet of $SU(2)_L$

Example: $SO(5) \rightarrow SO(4) \sim SU(2)_L \times SU(2)_R$

gives 4 real Goldstones: one $SU(2)_L$ doublet H



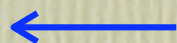
● vector resonances can be heavier:

→ smaller corrections to EWPO

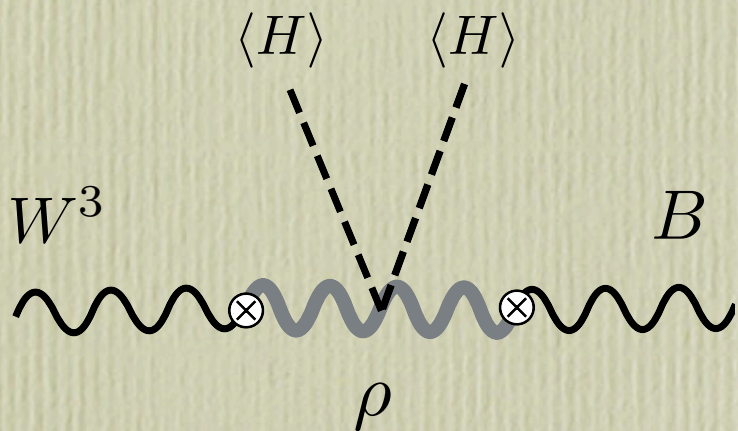
● the Higgs is composite:

→ Planck/TeV Hierarchy solved

$$\xi = \left(\frac{v}{f} \right)^2$$



new parameter compared to TC
(fixed by the dynamics)



$$S \sim 16\pi \left(\frac{v}{m_\rho} \right)^2 \sim \xi \frac{N}{\pi}$$

$m_\rho \sim \frac{4\pi f}{\sqrt{N}}$

$$\xi \rightarrow 0$$

$$[f \rightarrow \infty]$$

decoupling limit:

All ρ 's become heavy and
one re-obtains the SM

LHC will tell us which path

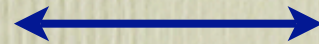
Nature has chosen !

(The End)

Extra Slides

Field theories with a curved
fifth dimension give an explicit realization
of 4D composite Higgs models

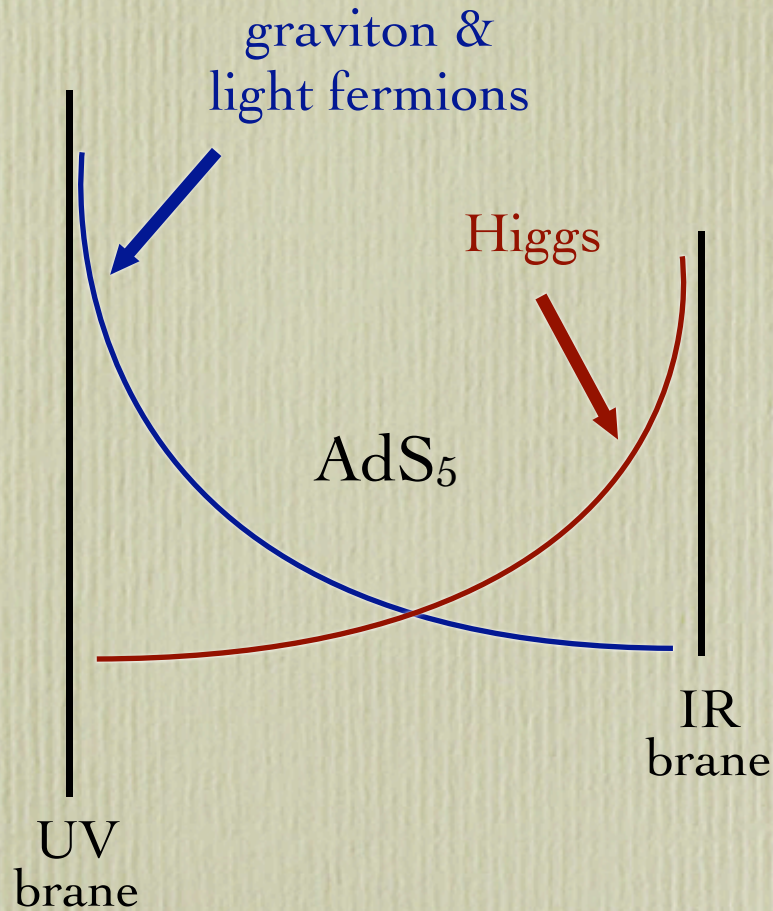
Resonances of the
strong sector



Kaluza-Klein
excitations

Example of strong dynamics:

a Randall-Sundrum setup



- Scales depend on the position:

translation in $y \Leftrightarrow$ 4D rescaling

- Solution to the Hierarchy Problem

geography of wave functions in the bulk

$$k \sim M_{\text{Pl}}$$

$$k e^{-2k\pi R} \sim \text{TeV}$$

warp factor

$$ds^2 = e^{-2ky} dx^\mu dx^\nu \eta_{\mu\nu} - dy^2$$
$$0 \leq y \leq \pi R$$

The holographic description

