

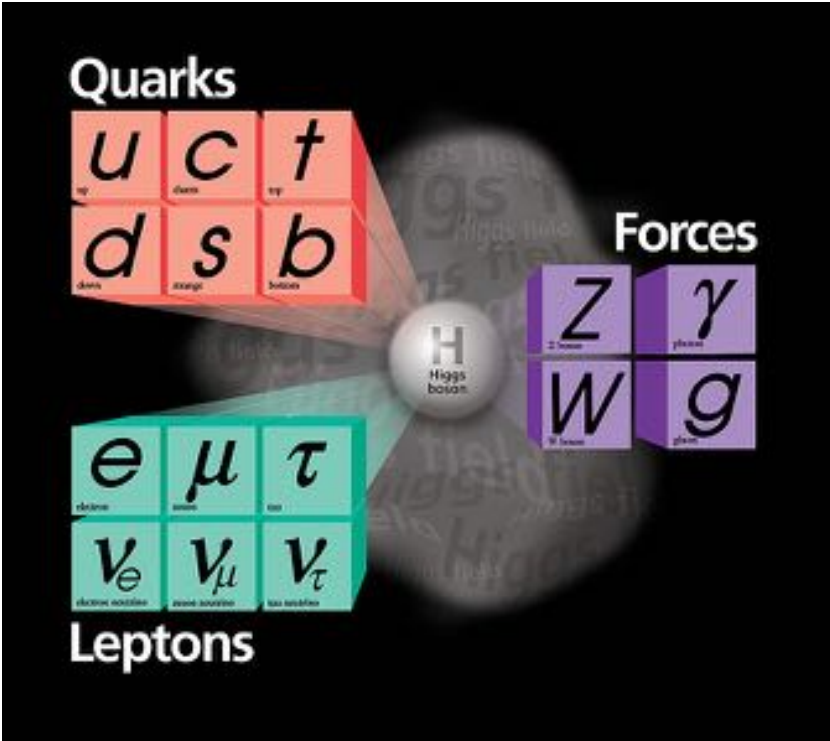
First results from the Muon g-2 Experiment at Fermilab

Brendan Kiburg, Fermi National Accelerator Laboratory

University of Warsaw Colloquium

26 April 2021

The Standard Model: Great success, many open questions!



The Standard Model: Great success, many open questions!

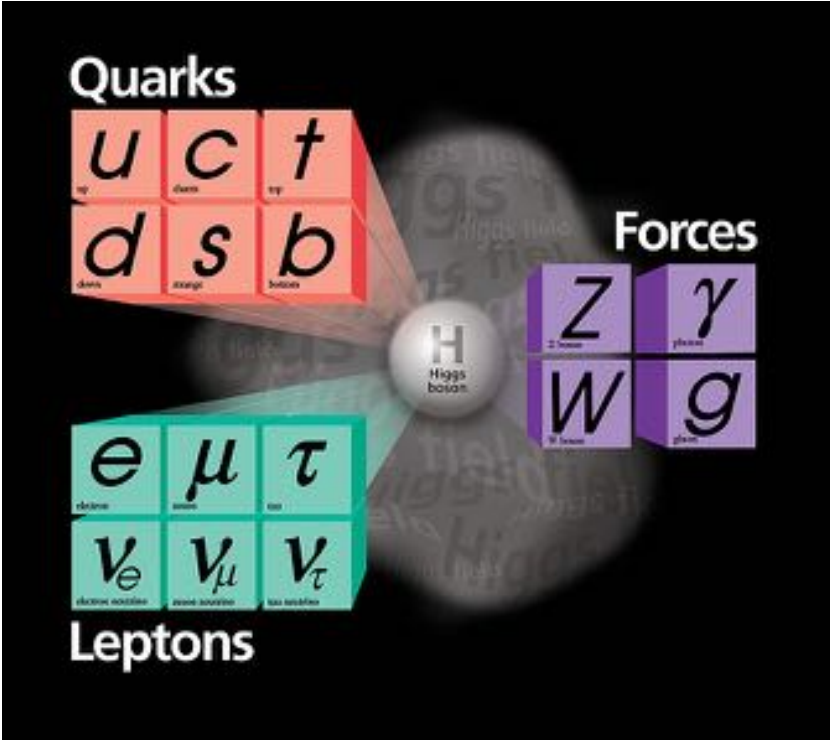
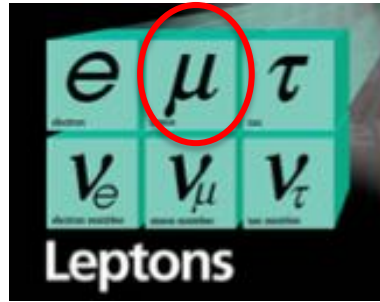


Illustration: © Johan Jarnestad/The Royal Swedish Academy of Sciences

Our favorite probe: The muon



- Fortuitous lifetime = $2.2 \mu\text{s}$
- Spin 1/2 particle
- Encodes information about spin in its decay

$$\vec{\mu} = g \frac{q}{2m} \vec{S}$$

- This g-factor is the “g” in “g-2”
- $g = 2$ + contributions from virtual particles

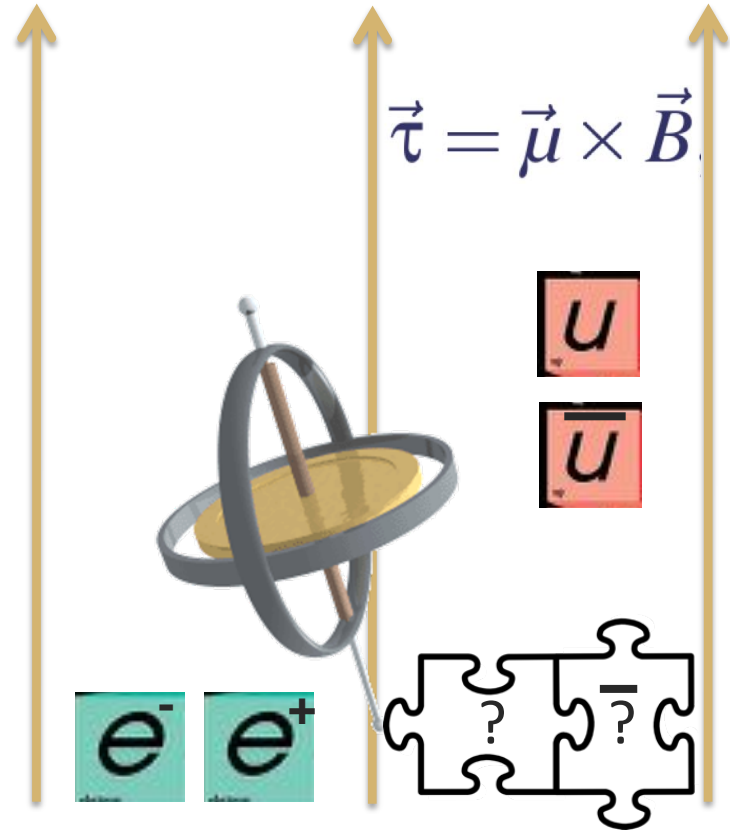
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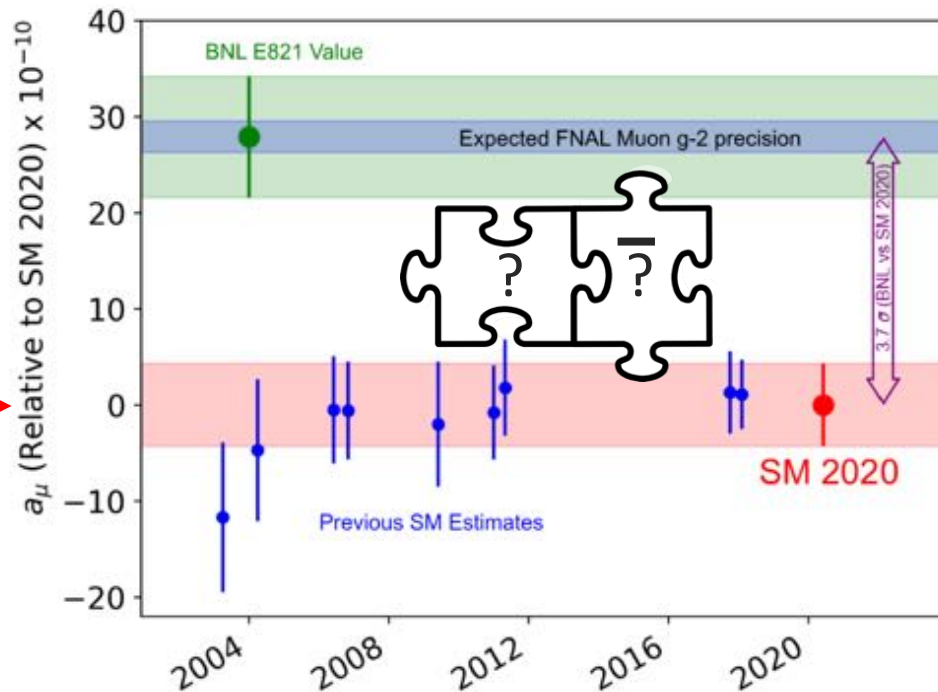
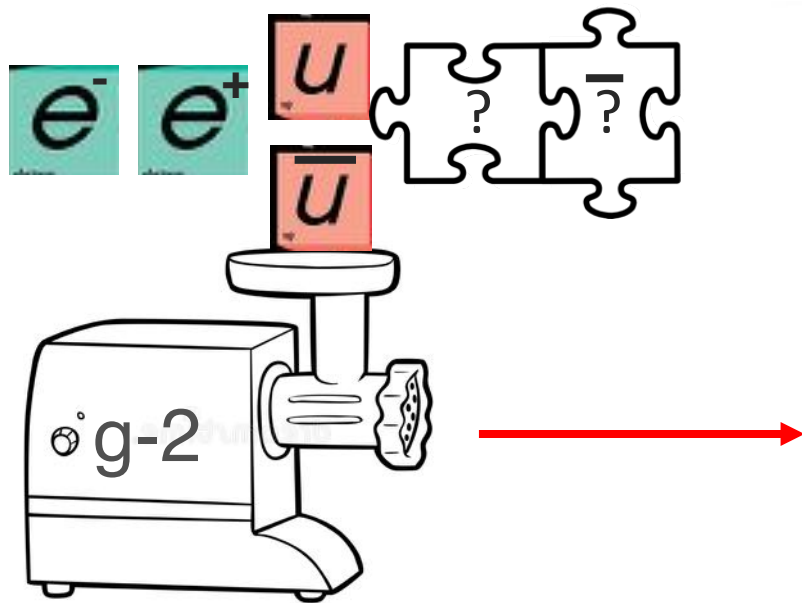
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- $g = 2 +$ contributions from virtual particles

Magnetic Field



Motivation: Status of the muon anomaly before Fermilab Experiment



- Dominik's talk: SM calculation, BSM physics, and possible interpretations

T. Aoyama, N. Asmussen, M. Benayoun et al., The anomalous magnetic moment of the muon in the Standard Model, Physics Reports (2020), <https://doi.org/10.1016/j.physrep.2020.07.006>.

Muon g-2 basics in a storage ring

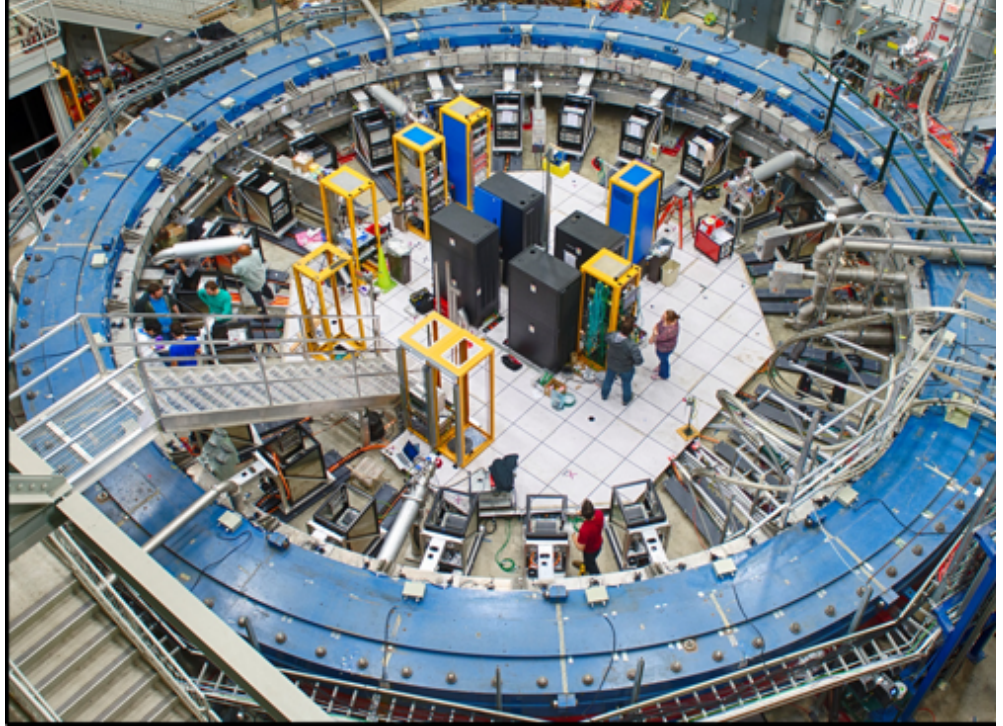
$$\omega_a = \frac{eB}{m} a_\mu$$

A precision measurement of the muon's anomalous spin-precession frequency in a well-measured magnetic field will tell us how muons see the universe.

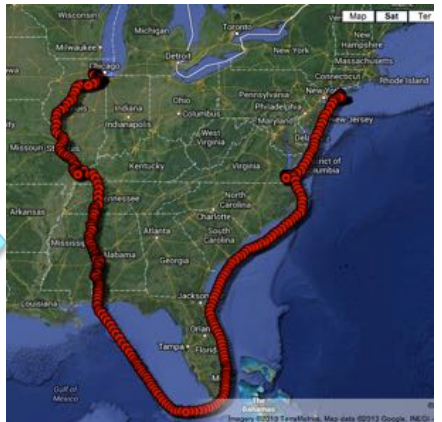
What are the main experimental steps to get a_μ ?

$$\omega_a = \frac{eB}{m} a_\mu$$

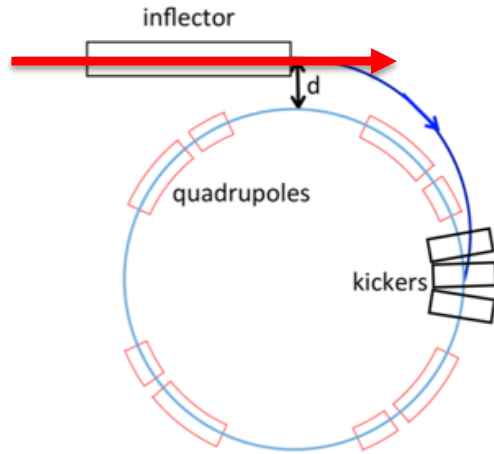
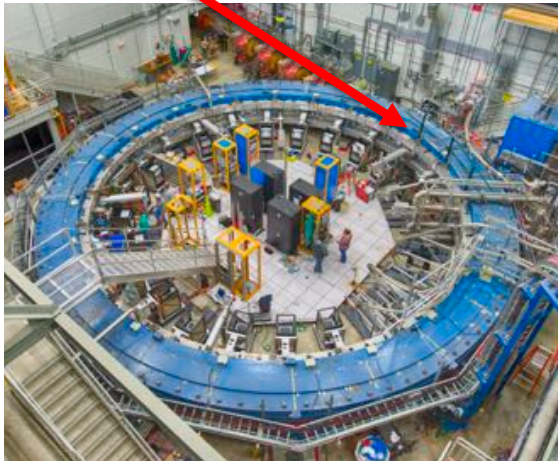
1. Build a racetrack for the muons
2. Inject and store polarized muons
3. Measure the decay electrons to determine the muons' properties
4. Map and track the magnetic field



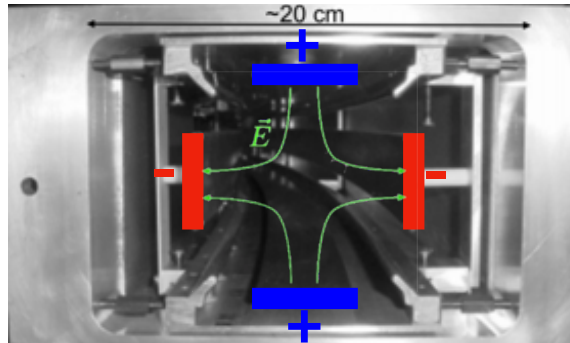
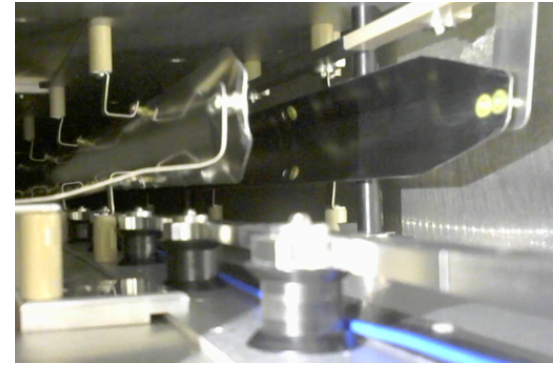
1. Build a racetrack for the muons: Bring the magnet to Fermilab



2. Inject and store polarized muons



Fast **kicker** pulse transfers muons to central orbit



Pulsed **quads** provide vertical focusing (restoring force)

2. Inject and store polarized muons

→ momentum

→ spin

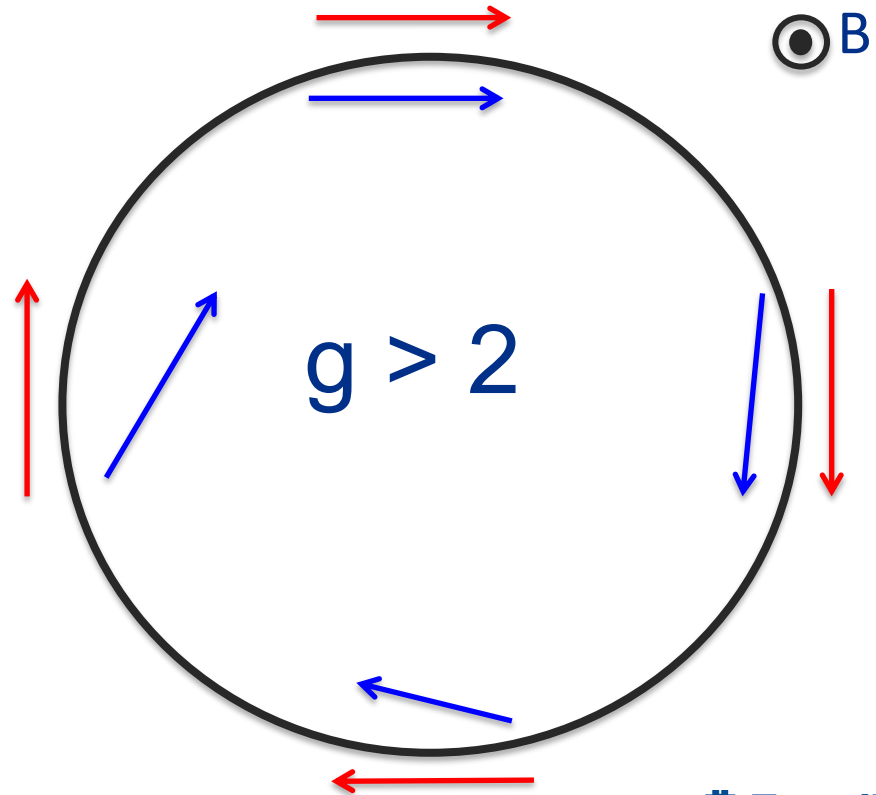
1. Cyclotron frequency:

$$\omega_c = \frac{e}{m\gamma} B$$

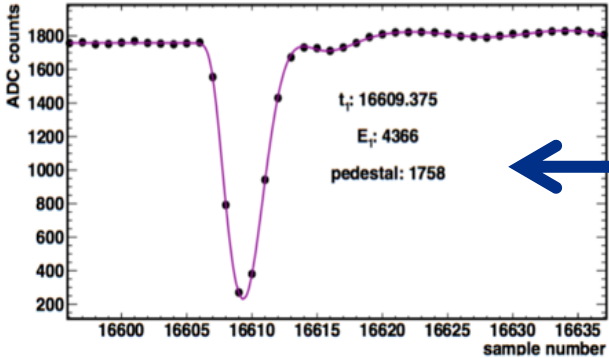
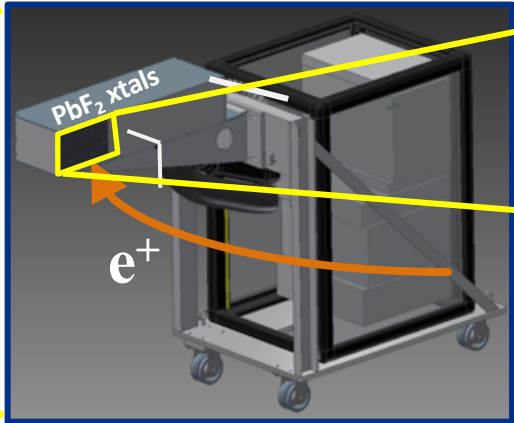
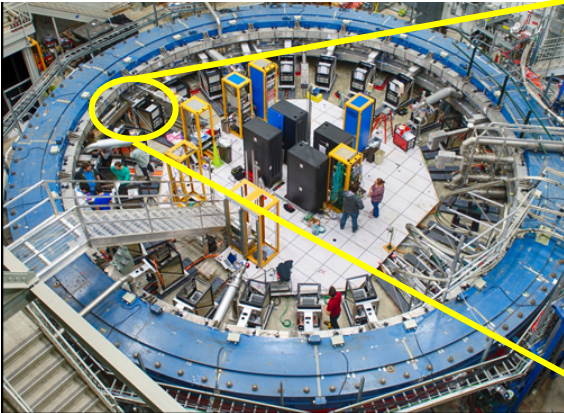
2. Spin precession frequency

$$\omega_s = \frac{e}{m\gamma} B \left(1 + \gamma \frac{g-2}{2} \right)$$

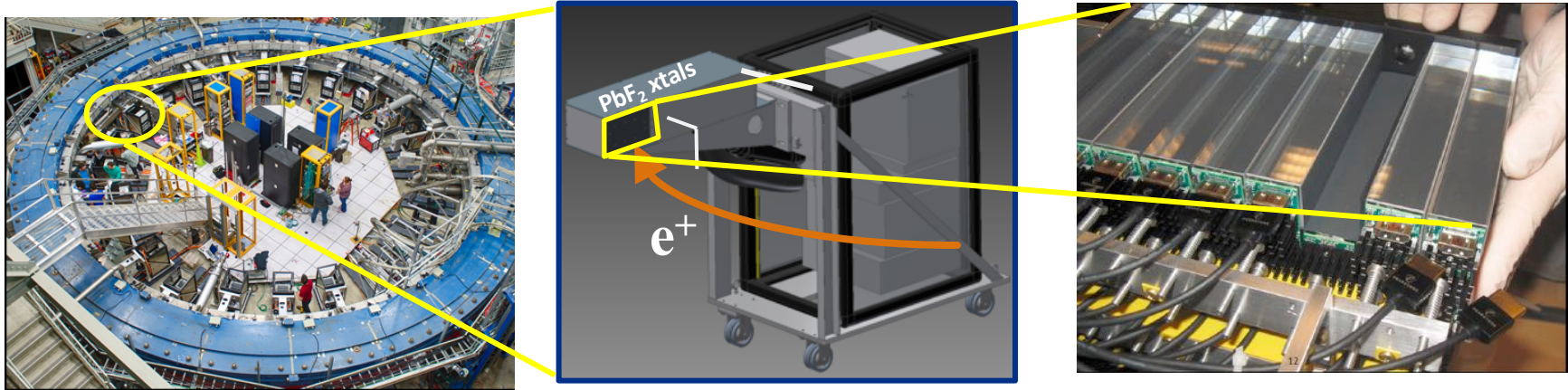
$$\omega_s - \omega_c \equiv \omega_a = \frac{eB}{m} \frac{g-2}{2} = \frac{eB}{m} a_\mu$$



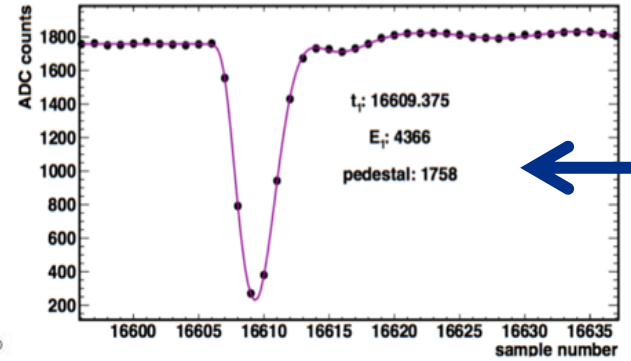
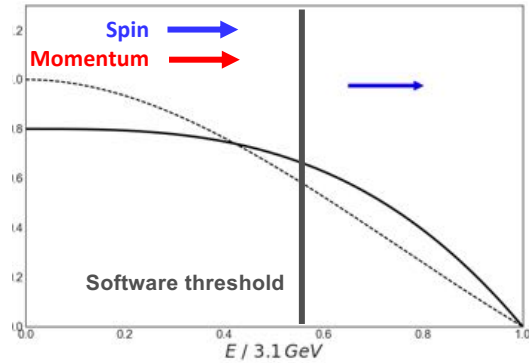
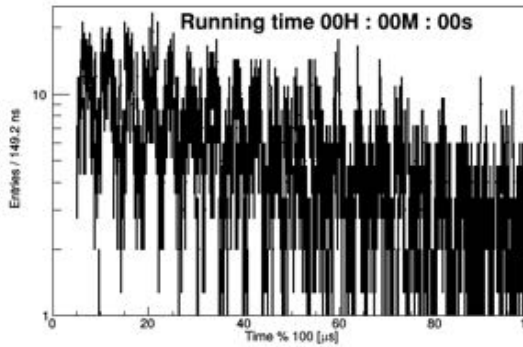
3. Measure decay electrons to determine the muons' properties



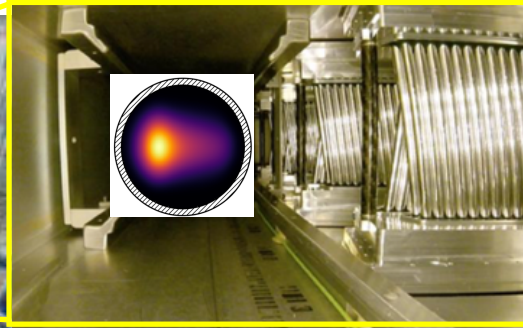
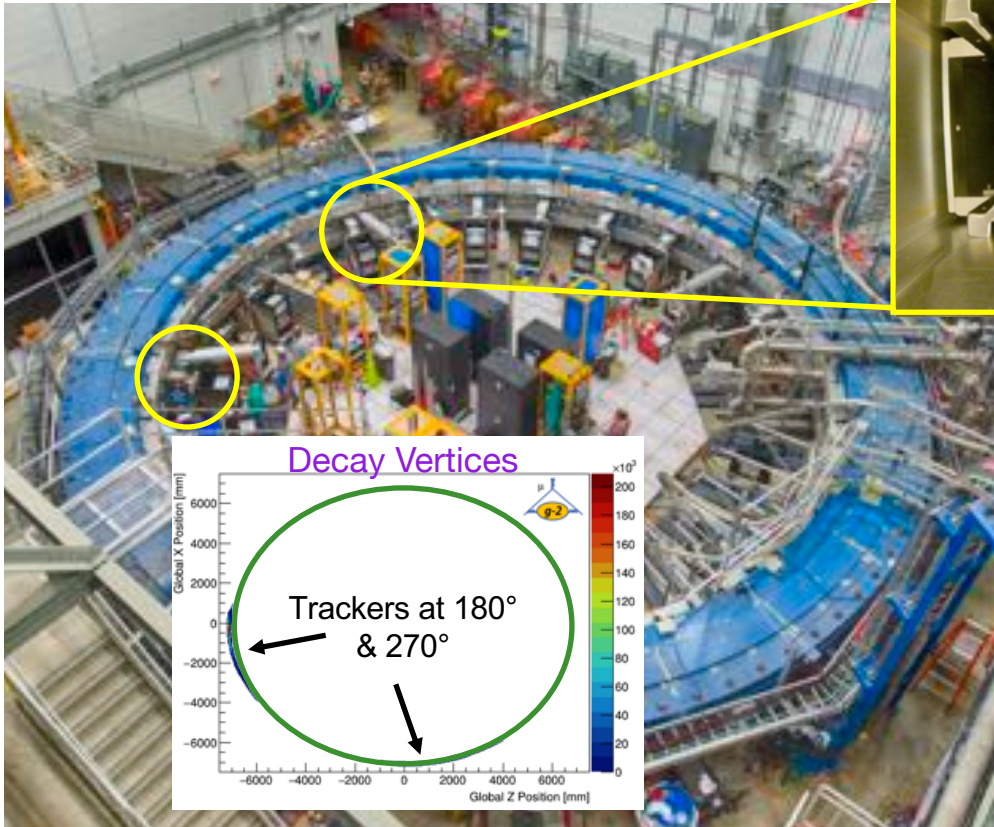
3. Measure decay electrons to determine the muons' properties



Events above threshold



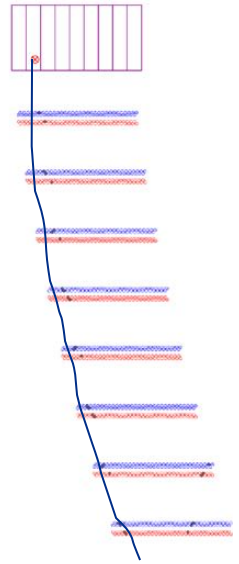
3. Measure decay electrons to determine the muons' properties



Muon's view of the storage region

Trackers

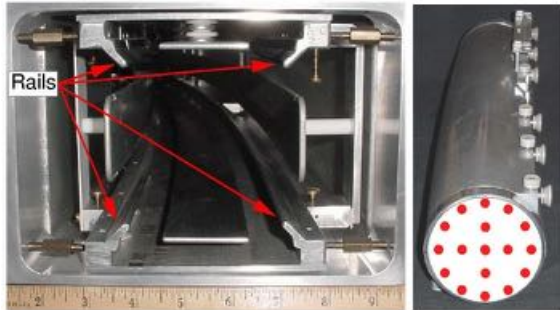
- Decay positron detected
- Reconstruction of muon beam distribution
- Measurement of beam dynamics properties



4. Map and track the magnetic field

- Use Nuclear Magnetic Resonance (NMR)
 - Tip spins of NMR probe sample's protons
 - Determine the field in terms of the proton precession frequency ω_p

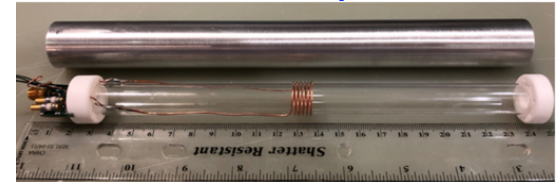
NMR trolley **maps** field
every 3 days



378 fixed probes **monitor**
continuously



Trolley cross-**calibrated**
to absolute probes



We can rewrite a_μ : our observables plus external measurements

$$a_\mu = \frac{\omega_a}{\tilde{\omega}'_p(T_r)} \frac{\mu'_p(T_r)}{\mu_e(H)} \frac{\mu_e(H)}{\mu_e} \frac{m_\mu}{m_e} \frac{g_e}{2}$$

Quantities we measure

ω_a : the **muon** anomalous spin precession frequency

$\tilde{\omega}'_p(T_r)$: precession of protons in water sample mapping the **field** and weighted by the muon distribution

Ultimate Goal: 140 ppb =
100 ppb (stat) \oplus 100 ppb (syst)

Determined externally to 25 ppb

$\tilde{\omega}'_p(T)$ Proton Larmor precession frequency in a spherical water sample. Temperature dependence known to < 1ppb/°C.
[Metrologia 13, 179 \(1977\)](#), [Metrologia 51, 54 \(2014\)](#),
[Metrologia 20, 81 \(1984\)](#)

$\frac{\mu_e(H)}{\mu'_p(T)}$ Measured to 10.5 ppb accuracy at T = 34.7°C
[Metrologia 13, 179 \(1977\)](#)

$\frac{\mu_e}{\mu_e(H)}$ Bound-state QED (exact)
[Rev. Mod. Phys. 88 035009 \(2016\)](#)

$\frac{m_\mu}{m_e}$ Known to 22 ppb from muonium hyperfine splitting
[Phys. Rev. Lett. 82, 711 \(1999\)](#)

$\frac{g_e}{2}$ Measured to 0.28 ppt
[Phys. Rev. A 83, 052122 \(2011\)](#)

We relate our observables to the quantities that determine a_μ

$$a_\mu \propto \frac{\omega_a}{\tilde{\omega}'_p} = \frac{f_{\text{clock}} \omega_a^{\text{meas}} (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{\text{calib}} \langle \omega_p(x, y, \phi) \times M(x, y, \phi) \rangle (1 + B_k + B_q)}$$

- f_{clock} • Blinded clock
- ω_a^m • Measured precession frequency
- C_e • Electric field correction
- C_p • Pitch correction
- C_{ml} • Muon loss correction
- C_{pa} • Phase-acceptance correction
- f_{calib} • Absolute magnetic field calibration
- $\omega_p(x, y, \phi)$ • Tracked field map distribution
- $M(x, y, \phi)$ • Tracked muon spatial distribution
- B_k • Transient field from the kicker
- B_q • Transient field from the quad charging

Systems used

Calorimeters

Trackers and
simulations

NMR

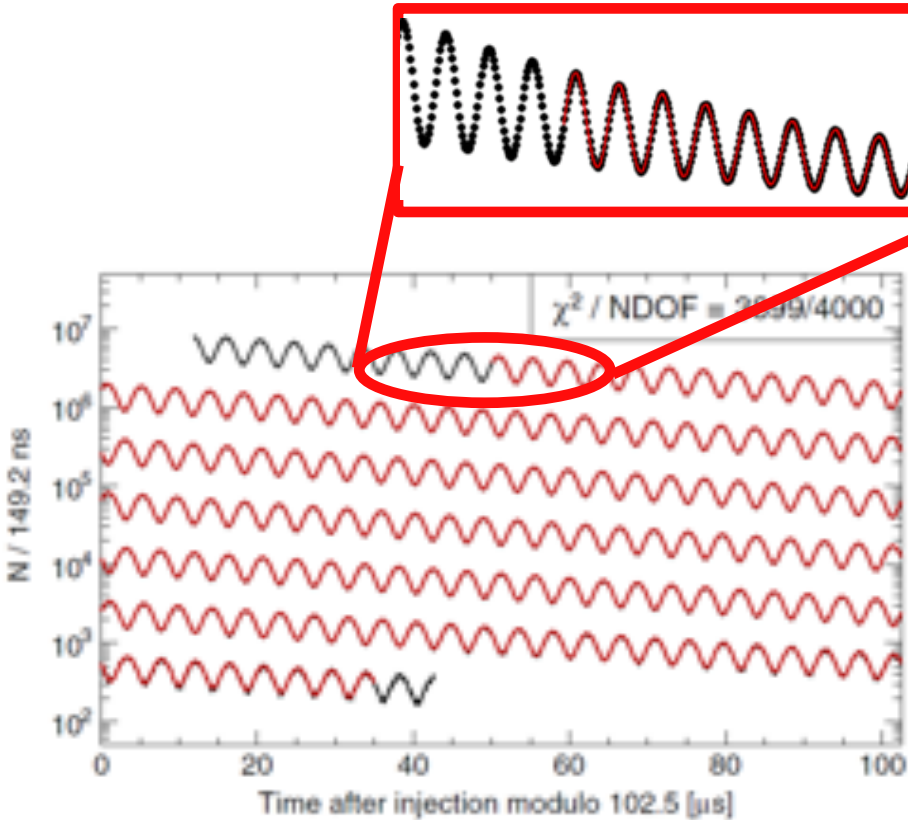
Trackers

Magnetometer
& dedicated
NMR

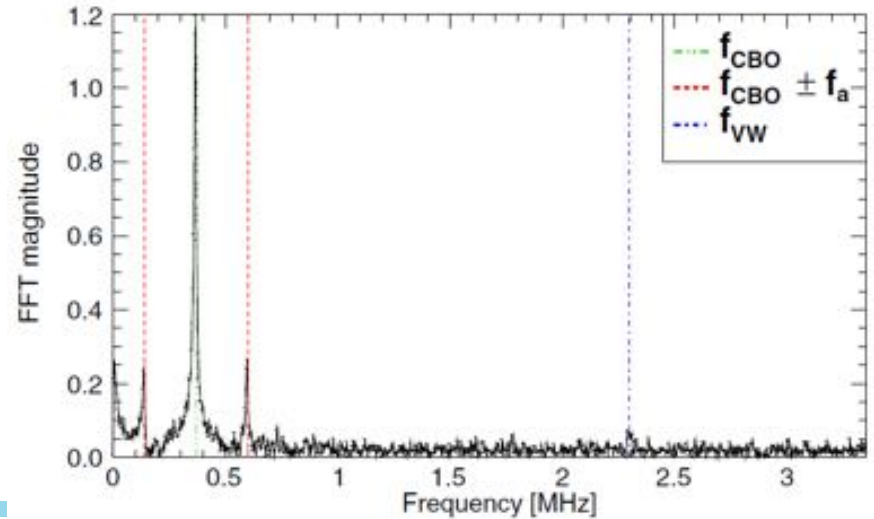


Muon Precession Frequency

Start with simple 5 parameter fit: $F(t) = N_0 e^{-t/\gamma\tau_\mu} [1 + A_0 \cos(\omega_a^m t + \phi_0)]$



FFT of fit residuals



Muon Precession Frequency

- Account for
 - beam dynamics effects (transverse oscillations)
 - muons that escape in a time-dependent manner, etc..

22 parameter fit

$$N_0 e^{-\frac{t}{\tau}} (1 + A \cdot A_{BO}(t) \cos(\omega_a t + \phi \cdot \phi_{BO}(t))) \cdot N_{CBO}(t) \cdot N_{VW}(t) \cdot N_y(t) \cdot N_{2CBO}(t) \cdot J(t)$$

$$A_{BO}(t) = 1 + A_A \cos(\omega_{CBO}(t) + \phi_A) e^{-\frac{t}{\tau_{CBO}}}$$

$$\phi_{BO}(t) = 1 + A_\phi \cos(\omega_{CBO}(t) + \phi_\phi) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{CBO}(t) = 1 + A_{CBO} \cos(\omega_{CBO}(t) + \phi_{CBO}) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{2CBO}(t) = 1 + A_{2CBO} \cos(2\omega_{CBO}(t) + \phi_{2CBO}) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{VW}(t) = 1 + A_{VW} \cos(\omega_{VW}(t) + \phi_{VW}) e^{-\frac{t}{\tau_{VW}}}$$

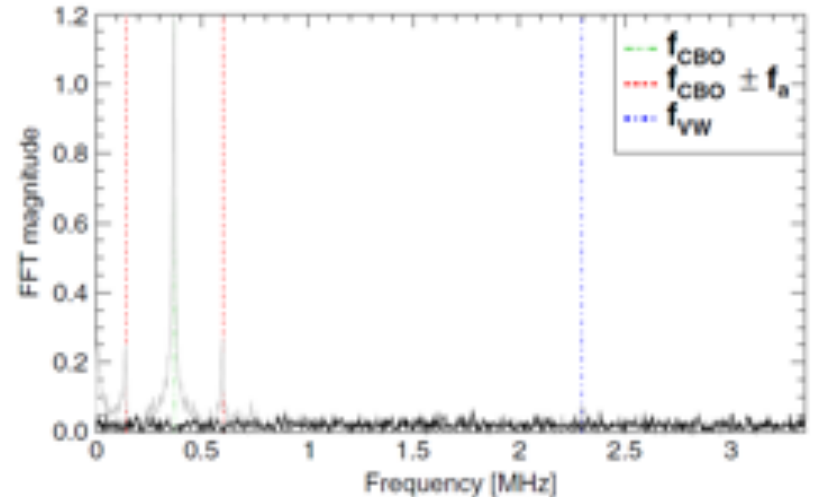
$$N_y(t) = 1 + A_y \cos(\omega_y(t) + \phi_y) e^{-\frac{t}{\tau_y}}$$

$$J(t) = 1 - k_{LM} \int_{t_0}^t \Lambda(t) dt$$

$$\omega_{CBO}(t) = \omega_0 t + A e^{-\frac{t}{\tau_A}} + B e^{-\frac{t}{\tau_B}}$$

$$\omega_y(t) = F \omega_{CBO}(t) \sqrt{2\omega_c / F \omega_{CBO}(t) - 1}$$

$$\omega_{VW}(t) = \omega_c - 2\omega_y(t)$$



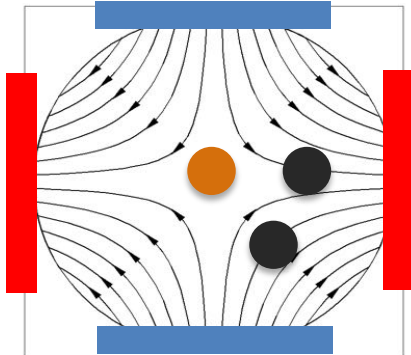
Beam Dynamics: E-field

Quads E-field transforms as motional B

$$\vec{\omega}_a = -\frac{e}{mc} \left[a_\mu \vec{B} - \underbrace{\left(a_\mu - \frac{1}{\gamma^2 - 1} \right)}_{\text{Term vanishes for appropriate choice of } \gamma} \vec{\beta} \times \vec{E} \right]$$

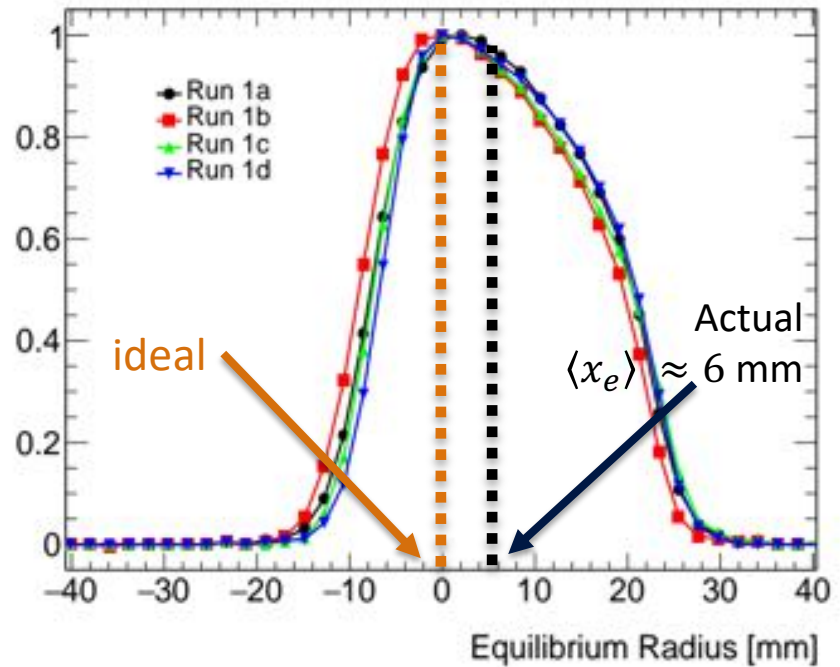
Term vanishes for appropriate choice of $\gamma = 29.3$

Momentum spread in beam of 0.15%



- Ideal muon
- Other muons

Arbitrary Units



$$C_e \approx 2n(1 - n)\beta_0^2 \frac{\langle x_e^2 \rangle}{R_0^2}$$

$$C_e = 489 \text{ ppb}, \delta_{C_e} = 53 \text{ ppb}$$

Muon Precession Frequency ω_a and Beam Dynamics Results

Quantity	Correction terms (ppb)	Uncertainty (ppb)
ω_a^m (statistical)	...	434
ω_a^m (systematic)	...	56
C_e	489	53
C_p	180	13
C_{ml}	-11	5
C_{pa}	-158	75
$f_{\text{calib}} \langle \omega_p(x, y, \phi) \times M(x, y, \phi) \rangle$...	56
B_k	-27	37
B_q	-17	92
$\mu'_p(34.7^\circ)/\mu_e$...	10
m_μ/m_e	...	22
$g_e/2$...	0
Total systematic	...	157
Total fundamental factors	...	25
Totals	544	462

- Statistically dominated (434 ppb)
- Muon precession systematic effects (56 ppb)
- Some large corrections (< 500 ppb) from beam dynamics effects → uncertainties understood and will improve in subsequent runs
- Beam Dynamics:
<https://arxiv.org/abs/2104.03240>
- Muon Precession:
<https://journals.aps.org/prd/abstract/10.1103/PhysRevD.103.072002>

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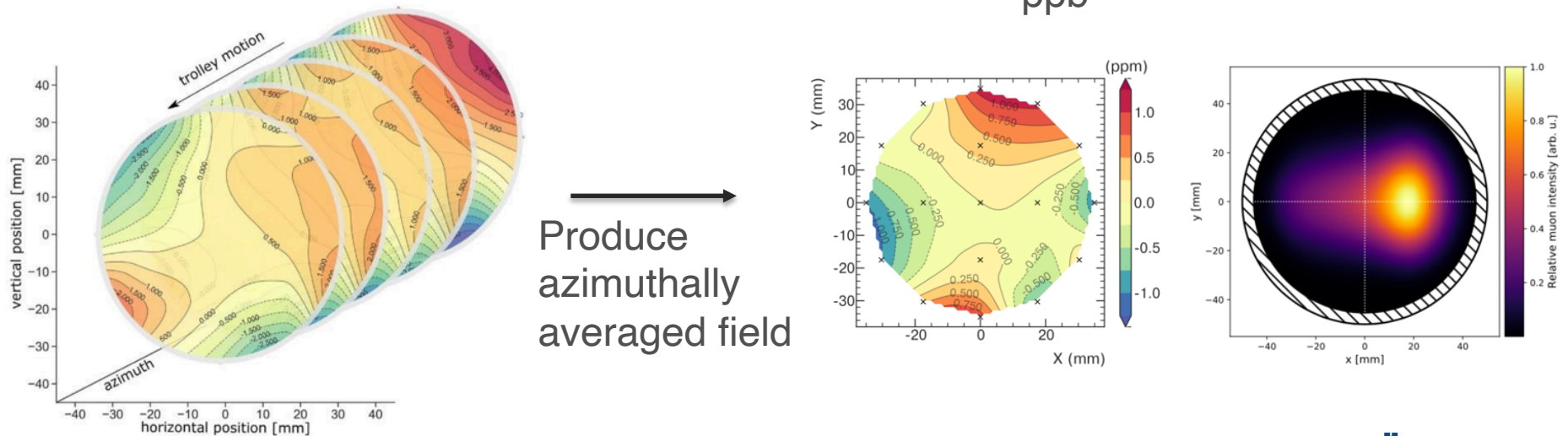
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Trolley Magnetic Field Maps

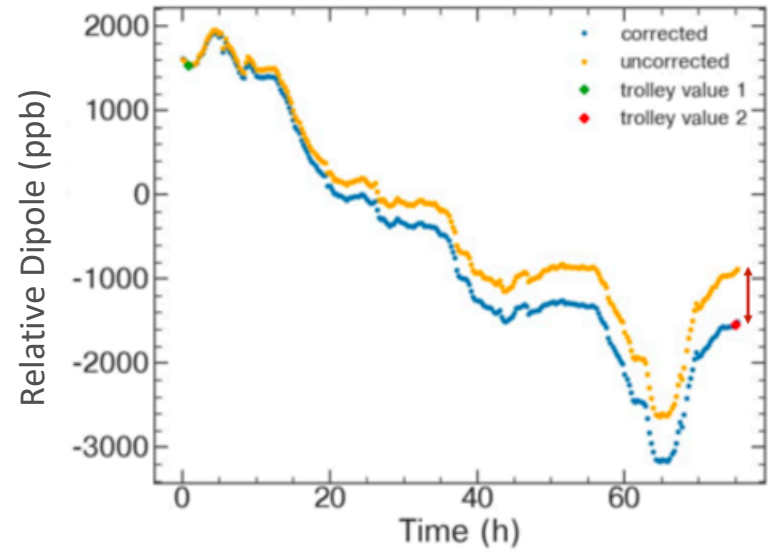
- Create a highly uniform field
- Trolley has 17 probes, produces map at 8000 azimuthal locations
- Determines strength of the field vs space

- Field maps are weighted by muon distribution
- Gradients shift the $\langle B \rangle$ by ~ 100 ppb, uncertainties ~ 20 ppb

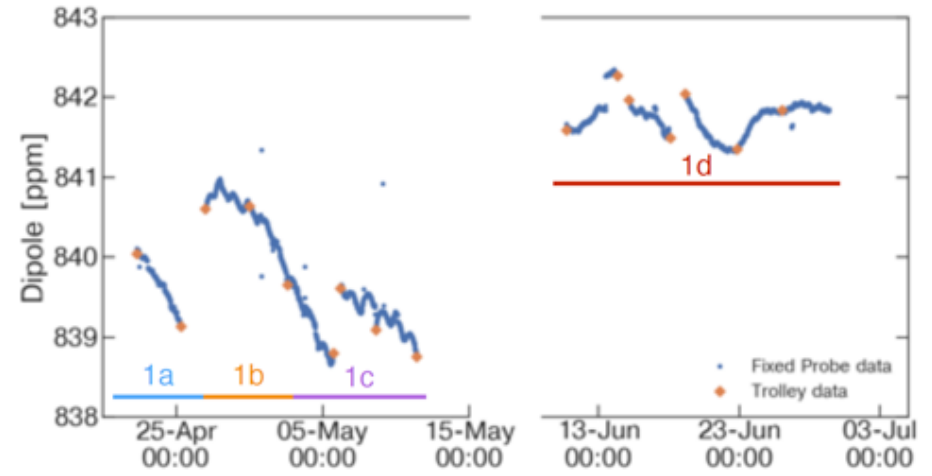


Field Tracking

- Trolley measures when beam is off
- Fixed probes monitor while beam is on
- Magnet temperature drifts
- Drifts in higher-order field gradients untracked \rightarrow tracking error



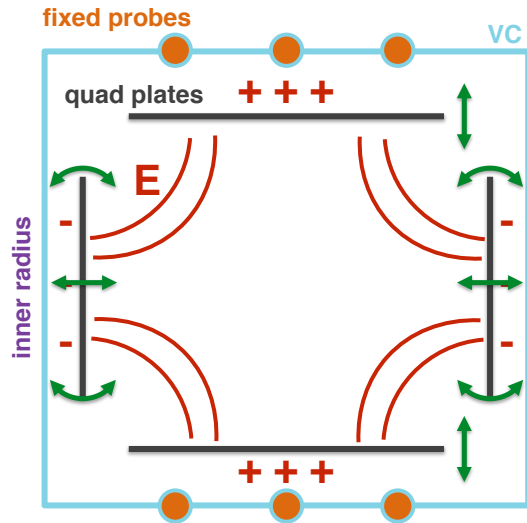
Field tracked in run 1



Data subset	Number of trolley pairs	Tracking Error Δ (ppb)
Run-1a	1	43
Run-1b	2	34
Run-1c	3	25
Run-1d	5	22

Transient Fields affect the muons

- Quads are pulsed synchronously with muon injection
- We observed a motion of the quad plates associated with these pulses
- Affects field observed by muons, but **not** the field mapped by trolley (quads off)



Pulsing Quads

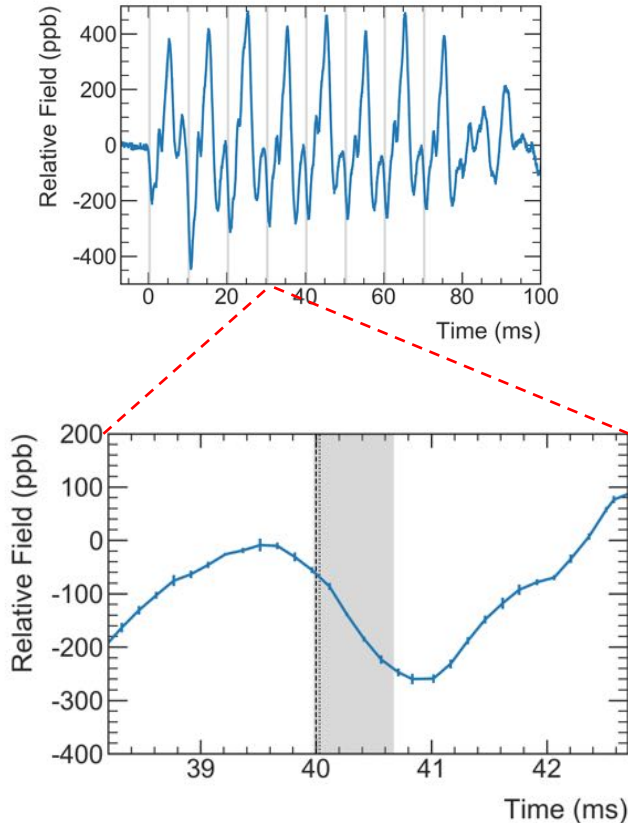
- Side plates oscillate radially
- Oscillating conductor perturbs B-field
- **Fixed probes** sensitive to oscillation

Dedicated measurement



B_q – Quad transients

- Map effect along the quad for all beam pulses and account for the quad
- Correction = -17 ppb
- Conservative Uncertainty 82 ppb
- More detailed maps exist →
 - Will quantify long term stability
 - Further map quad region



Systematic Source	Uncertainty (ppb)
Time and Azimuthal Structure	77
Second Pulse Train	14
Repeatability	13
Skin Depth	13
Field Drift	10
Frequency Extraction	5
Radial Dependence	4
Probe Positioning	2
Total ESQ-Transient Uncertainty	82

Magnetic Field Results

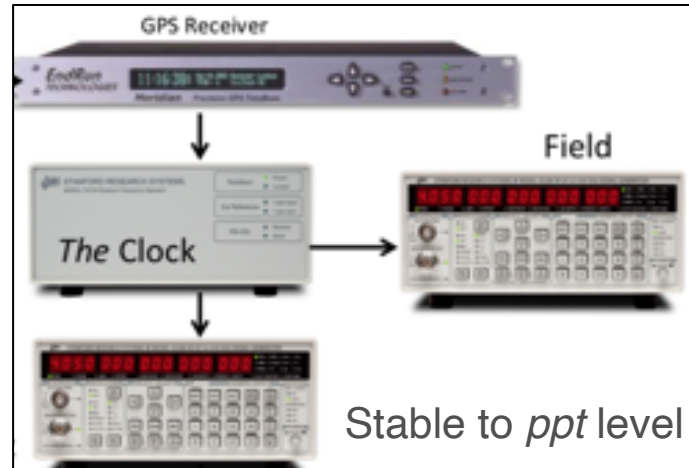
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- Magnetic field measurement 56 ppb includes field mapping, tracking, weighting absolute calibration
- Dedicated measurements for transient field yield 99 ppb → improvements for future runs
- Magnetic Field Analysis:
<https://journals.aps.org/pr/abstract/10.1103/PhysRevA.103.042208>

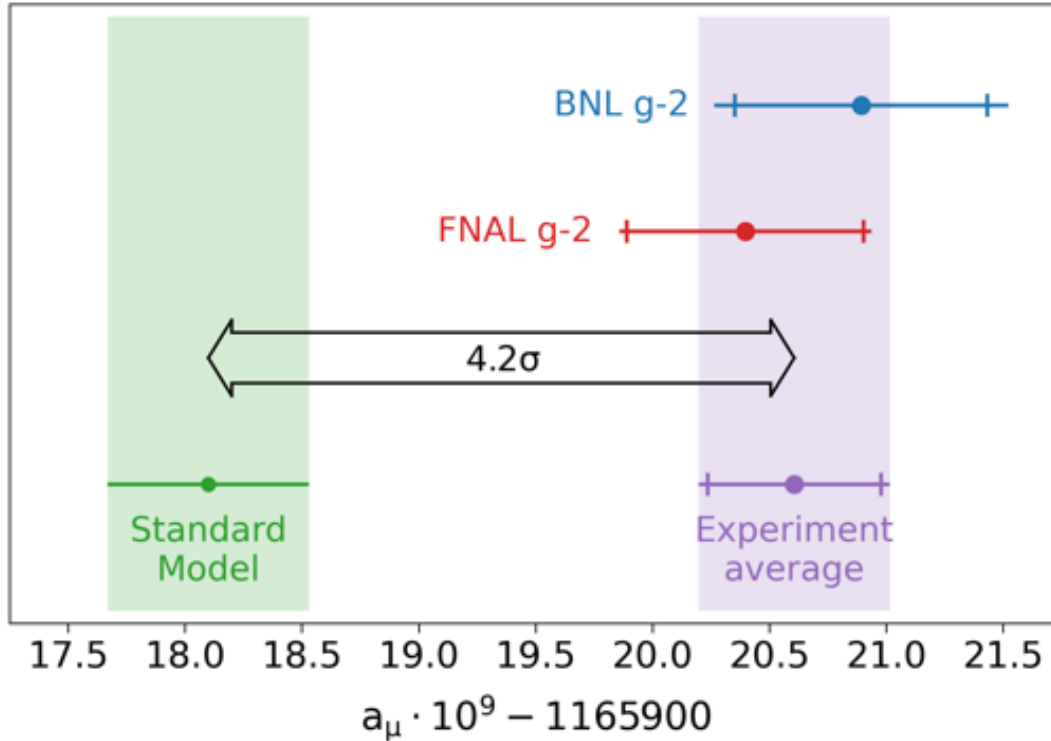
Clock and Unblinding

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- Muon clock is hardware blinded +/- 25 ppm
- Sets the *metric* for the wiggle plot
- Once analysis was completed → collaboration unblinded and learned the clock frequency and a_μ



First Results



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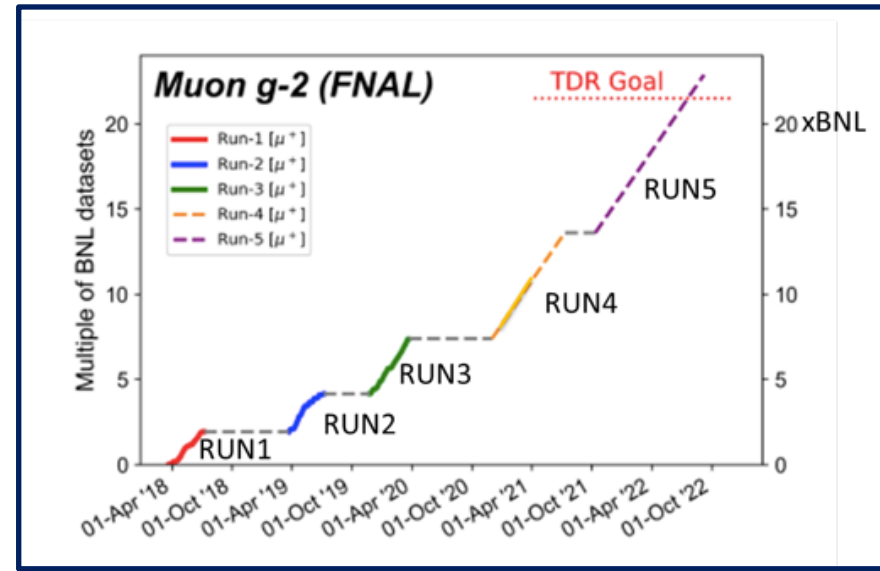
$$a_\mu(\text{FNAL}) = 116\,592\,040(54) \times 10^{-11} \quad (0.46 \text{ ppm})$$

$$a_\mu(\text{Exp}) = 116\,592\,061(41) \times 10^{-11} \quad (0.35 \text{ ppm})$$

$$a_\mu(\text{Exp}) - a_\mu(\text{SM}) = (251 \pm 59) \times 10^{-11}$$

Summary and Outlook

- FNAL measurement agrees well with past experiment
 - Experiment on solid footing
- Analyzed 6% of the planned data
 - Statistically limited: 434 ppb
 - Systematics: 157 ppb
- Collected more than 50% of our planned data
 - Aim to analyze Run 2-3 for summer of 2022
- Meanwhile ... theory steps in: What could it all mean?



Measurement of the Positive Muon Anomalous Magnetic Moment to 0.46 ppm

Muon $g-2$ Collaboration • B. Abi (Oxford U.) [Show All\(237\)](#)

Apr 7, 2021

11 pages

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DOI: [10.1103/PhysRevLett.126.141801](#) (publication)

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Experiments: FNAL-E-0989

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